# Shapely Documentation 

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Manipulation and analysis of geometric objects in the Cartesian plane.


Shapely is a BSD-licensed Python package for manipulation and analysis of planar geometric objects. It is using the widely deployed open-source geometry library GEOS (the engine of PostGIS, and a port of JTS). Shapely wraps GEOS geometries and operations to provide both a feature rich Geometry interface for singular (scalar) geometries and higher-performance NumPy ufuncs for operations using arrays of geometries. Shapely is not primarily focused on data serialization formats or coordinate systems, but can be readily integrated with packages that are.

## WHAT IS A UFUNC?

A universal function (or ufunc for short) is a function that operates on $n$-dimensional arrays on an element-by-element fashion and supports array broadcasting. The underlying for loops are implemented in C to reduce the overhead of the Python interpreter.

## MULTITHREADING

Shapely functions generally support multithreading by releasing the Global Interpreter Lock (GIL) during execution. Normally in Python, the GIL prevents multiple threads from computing at the same time. Shapely functions internally release this constraint so that the heavy lifting done by GEOS can be done in parallel, from a single Python process.

### 2.1 Usage

Here is the canonical example of building an approximately circular patch by buffering a point, using the scalar Geometry interface:

```
>>> from shapely import Point
>>> patch = Point(0.0, 0.0).buffer(10.0)
>>> patch
<POLYGON ((10 0, 9.952 -0.98, 9.808 -1.951, 9.569 -2.903, 9.239 -3.827, 8.81...>
>>> patch.area
313.6548490545941
```

Using the vectorized ufunc interface (instead of using a manual for loop), compare an array of points with a polygon:

```
>>> import shapely
>>> import numpy as np
>>> geoms = np.array([Point(0, 0), Point(1, 1), Point(2, 2)])
>>> polygon = shapely.box(0, 0, 2, 2)
>>> shapely.contains(polygon, geoms)
array([False, True, False])
```

See the documentation for more examples and guidance: https://shapely.readthedocs.io

### 2.2 Requirements

Shapely 2.0 requires

- Python $>=3.7$
- GEOS $>=3.5$
- NumPy >=1.14


### 2.3 Installing Shapely

We recommend installing Shapely using one of the available built distributions, for example using pip or conda:

```
$ pip install shapely
# or using conda
$ conda install shapely --channel conda-forge
```

See the installation documentation for more details and advanced installation instructions.

### 2.4 Integration

Shapely does not read or write data files, but it can serialize and deserialize using several well known formats and protocols. The shapely.wkb and shapely.wkt modules provide dumpers and loaders inspired by Python's pickle module.

```
>>> from shapely.wkt import dumps, loads
>>> dumps(loads('POINT (0 0)'))
'POINT (0.00000000000000000 0.0000000000000000)'
```

Shapely can also integrate with other Python GIS packages using GeoJSON-like dicts.

```
>>> import json
>>> from shapely.geometry import mapping, shape
>>> s = shape(json.loads('{"type": "Point", "coordinates": [0.0, 0.0]}'))
>>> s
<POINT (O O)>
>>> print(json.dumps(mapping(s)))
{"type": "Point", "coordinates": [0.0, 0.0]}
```


### 2.5 Support

Questions about using Shapely may be asked on the GIS StackExchange using the "shapely" tag.
Bugs may be reported at https://github.com/shapely/shapely/issues.

### 2.6 Copyright \& License

Shapely is licensed under BSD 3-Clause license. GEOS is available under the terms of GNU Lesser General Public License (LGPL) 2.1 at https://libgeos.org.

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### 2.8 Frequently asked questions and answers

## I INSTALLED SHAPELY IN A CONDA ENVIRONMENT USING PIP. WHY DOESN'T IT WORK?

Shapely versions < 2.0 load a GEOS shared library using ctypes. It's not uncommon for users to have multiple copies of GEOS libs on their system. Loading the correct one is complicated and shapely has a number of platform-dependent GEOS library loading bugs. The project has particularly poor support for finding the correct GEOS library for a shapely package installed from PyPI into a conda environment. We recommend that conda users always get shapely from conda-forge.

# ARE THERE REFERENCES FOR THE ALGORITHMS USED BY SHAPELY? 

Generally speaking, shapely's predicates and operations are derived from methods of the same name from GEOS and the JTS Topology Suite. See the JTS FAQ for references describing the JTS algorithms.

## I USED .BUFFER() ON A GEOMETRY WITH Z COORDINATES. WHERE DID THE Z COORDINATES GO?

The buffer algorithm in GEOS is purely two-dimensional and discards any Z coordinates. This is generally the case for the GEOS algorithms.

### 5.1 Installation

### 5.1.1 Built distributions

Built distributions don't require compiling Shapely and its dependencies, and can be installed using pip or conda. In addition, Shapely is also available via some system package management tools like apt.

## Installation from PyPI

Shapely is available as a binary distribution (wheel) for Linux, macOS, and Windows platforms on PyPI. The distribution includes the most recent version of GEOS available at the time of the Shapely release. Install the binary wheel with pip as follows:

```
$ pip install shapely
```


## Installation using conda

Shapely is available on the conda-forge channel. Install as follows:

```
$ conda install shapely --channel conda-forge
```


### 5.1.2 Installation from source with custom GEOS libary

You may want to use a specific GEOS version or a GEOS distribution that is already present on your system (for compatibility with other modules that depend on GEOS, such as cartopy or osgeo.ogr). In such cases you will need to ensure the GEOS library is installed on your system and then compile Shapely from source yourself, by directing pip to ignore the binary wheels.

On Linux:

```
$ sudo apt install libgeos-dev # skip this if you already have GEOS
$ pip install shapely --no-binary shapely
```

On macoS:
\$ brew install geos \# skip this if you already have GEOS
\$ pip install shapely --no-binary shapely
If you've installed GEOS to a standard location on Linux or macOS, the installation will automatically find it using geos-config. See the notes below on GEOS discovery at compile time to configure this.
We do not have a recipe for Windows platforms. The following steps should enable you to build Shapely yourself:

- Get a C compiler applicable to your Python version (https://wiki.python.org/moin/WindowsCompilers)
- Download and install a GEOS binary (https://trac.osgeo.org/osgeo4w/)
- Set GEOS_INCLUDE_PATH and GEOS_LIBRARY_PATH environment variables (see below for notes on GEOS discovery)
- Run pip install shapely --no-binary
- Make sure the GEOS .dll files are available on the PATH


### 5.1.3 Installation for local development

This is similar to installing with a custom GEOS binary, but then instead of installing Shapely with pip from PyPI, you clone the package from Github:

```
$ git clone git@github.com:shapely/shapely.git
$ cd shapely/
```

Install it in development mode using pip:

```
$ pip install -e .[test]
```

For development, use of a virtual environment is strongly recommended. For example using venv:

```
$ python3 -m venv .
$ source bin/activate
(env) $ pip install -e .[test]
```

Or using conda:

```
$ conda create -n env python=3 geos numpy cython pytest
$ conda activate env
(env) $ pip install -e .
```


### 5.1.4 Testing Shapely

Shapely can be tested using pytest:

```
$ pip install pytest # or shapely[test]
$ pytest --pyargs shapely.tests
```


### 5.1.5 GEOS discovery (compile time)

If GEOS is installed on Linux or macOS, the geos-config command line utility should be available and pip will find GEOS automatically. If the correct geos-config is not on the PATH, you can add it as follows (on Linux/macOS):

```
$ export PATH=/path/to/geos/bin:$PATH
```

Alternatively, you can specify where Shapely should look for GEOS library and header files using environment variables (on Linux/macOS):

```
$ export GEOS_INCLUDE_PATH=/path/to/geos/include
$ export GEOS_LIBRARY_PATH=/path/to/geos/lib
```

On Windows, there is no geos-config and the include and lib folders need to be specified manually in any case:

```
$ set GEOS_INCLUDE_PATH=C:\path\to\geos\include
$ set GEOS_LIBRARY_PATH=C:\path\to\geos\lib
```

Common locations of GEOS (to be suffixed by lib, include or bin):

- Anaconda (Linux/macOS): \$CONDA_PREFIX/Library
- Anaconda (Windows): \%CONDA_PREFIX\%\Library
- OSGeo4W (Windows): C: \OSGeo4W64


### 5.1.6 GEOS discovery (runtime)

Shapely is dynamically linked to GEOS. This means that the same GEOS library that was used during Shapely compilation is required on your system at runtime. When using Shapely that was distributed as a binary wheel or through conda, this is automatically the case and you can stop reading.

In other cases this can be tricky, especially if you have multiple GEOS installations next to each other. We only include some guidelines here to address this issue as this document is not intended as a general guide of shared library discovery.

If you encounter exceptions like:
ImportError: libgeos_c.so.1: cannot open shared object file: No such file or directory
You will have to make the shared library file available to the Python interpreter. There are in general four ways of making Python aware of the location of shared library:

1. Copy the shared libraries into the shapely module directory (this is how Windows binary wheels work: they are distributed with the correct dlls in the shapely module directory)
2. Copy the shared libraries into the library directory of the Python interpreter (this is how Anaconda environments work)
3. Copy the shared libraries into some system location (C: \Windows $\backslash$ System 32 ; /usr/local/lib, this happens if you installed GEOS through apt or brew)
4. Add the shared library location to a the dynamic linker path variable at runtime. (Advanced usage; Linux and macOS only; on Windows this method was deprecated in Python 3.8)

The filenames of the GEOS shared libraries are:

- On Linux: libgeos-*.so.*, libgeos_c-*.so.*
- On macOS: libgeos.dylib, libgeos_c.dylib
- On Windows: geos-*.dll, geos_c-*.dll

Note that Shapely does not make use of any RUNPATH (RPATH) header. The location of the GEOS shared library is not stored inside the compiled Shapely library.

### 5.2 The Shapely User Manual

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Copyright This work is licensed under a Creative Commons Attribution 3.0 United States License.
Abstract This document explains how to use the Shapely Python package for computational geometry.

### 5.2.1 Introduction

Deterministic spatial analysis is an important component of computational approaches to problems in agriculture, ecology, epidemiology, sociology, and many other fields. What is the surveyed perimeter/area ratio of these patches of animal habitat? Which properties in this town intersect with the 50 -year flood contour from this new flooding model? What are the extents of findspots for ancient ceramic wares with maker's marks " A " and " B ", and where do the extents overlap? What's the path from home to office that best skirts identified zones of location based spam? These are just a few of the possible questions addressable using non-statistical spatial analysis, and more specifically, computational geometry.
Shapely is a Python package for set-theoretic analysis and manipulation of planar features using functions from the well known and widely deployed GEOS library. GEOS, a port of the Java Topology Suite (JTS), is the geometry engine of the PostGIS spatial extension for the PostgreSQL RDBMS. The designs of JTS and GEOS are largely guided by the Open Geospatial Consortium's Simple Features Access Specification ${ }^{1}$ and Shapely adheres mainly to the same set of standard classes and operations. Shapely is thereby deeply rooted in the conventions of the geographic information systems (GIS) world, but aspires to be equally useful to programmers working on non-conventional problems.

The first premise of Shapely is that Python programmers should be able to perform PostGIS type geometry operations outside of an RDBMS. Not all geographic data originate or reside in a RDBMS or are best processed using SQL. We can load data into a spatial RDBMS to do work, but if there's no mandate to manage (the "M" in "RDBMS") the data over time in the database we're using the wrong tool for the job. The second premise is that the persistence, serialization, and map projection of features are significant, but orthogonal problems. You may not need a hundred GIS format readers and writers or the multitude of State Plane projections, and Shapely doesn't burden you with them. The third premise is that Python idioms trump GIS (or Java, in this case, since the GEOS library is derived from JTS, a Java project) idioms.
If you enjoy and profit from idiomatic Python, appreciate packages that do one thing well, and agree that a spatially enabled RDBMS is often enough the wrong tool for your computational geometry job, Shapely might be for you.

[^0]
## Spatial Data Model

The fundamental types of geometric objects implemented by Shapely are points, curves, and surfaces. Each is associated with three sets of (possibly infinite) points in the plane. The interior, boundary, and exterior sets of a feature are mutually exclusive and their union coincides with the entire plane ${ }^{2}$.

- A Point has an interior set of exactly one point, a boundary set of exactly no points, and an exterior set of all other points. A Point has a topological dimension of 0 .
- A Curve has an interior set consisting of the infinitely many points along its length (imagine a Point dragged in space), a boundary set consisting of its two end points, and an exterior set of all other points. A Curve has a topological dimension of 1 .
- A Surface has an interior set consisting of the infinitely many points within (imagine a Curve dragged in space to cover an area), a boundary set consisting of one or more Curves, and an exterior set of all other points including those within holes that might exist in the surface. A Surface has a topological dimension of 2.

That may seem a bit esoteric, but will help clarify the meanings of Shapely's spatial predicates, and it's as deep into theory as this manual will go. Consequences of point-set theory, including some that manifest themselves as "gotchas", for different classes will be discussed later in this manual.

The point type is implemented by a Point class; curve by the LineString and LinearRing classes; and surface by a Polygon class. Shapely implements no smooth (i.e. having continuous tangents) curves. All curves must be approximated by linear splines. All rounded patches must be approximated by regions bounded by linear splines.

Collections of points are implemented by a MultiPoint class, collections of curves by a MultiLineString class, and collections of surfaces by a MultiPolygon class. These collections aren't computationally significant, but are useful for modeling certain kinds of features. A Y-shaped line feature, for example, is well modeled as a whole by a MultiLineString.

The standard data model has additional constraints specific to certain types of geometric objects that will be discussed in following sections of this manual.

See also https://web.archive.org/web/20160719195511/http://www.vividsolutions.com/jts/discussion.htm for more illustrations of this data model.

## Relationships

The spatial data model is accompanied by a group of natural language relationships between geometric objects - contains, intersects, overlaps, touches, etc. - and a theoretical framework for understanding them using the $3 \times 3$ matrix of the mutual intersections of their component point sets ${ }^{3}$ : the DE-9IM. A comprehensive review of the relationships in terms of the DE-9IM is found in ${ }^{4}$ and will not be reiterated in this manual.

[^1]
## Operations

Following the JTS technical specs ${ }^{5}$, this manual will make a distinction between constructive (buffer, convex hull) and set-theoretic operations (intersection, union, etc.). The individual operations will be fully described in a following section of the manual.

## Coordinate Systems

Even though the Earth is not flat - and for that matter not exactly spherical - there are many analytic problems that can be approached by transforming Earth features to a Cartesian plane, applying tried and true algorithms, and then transforming the results back to geographic coordinates. This practice is as old as the tradition of accurate paper maps.
Shapely does not support coordinate system transformations. All operations on two or more features presume that the features exist in the same Cartesian plane.

### 5.2.2 Geometric Objects

Geometric objects are created in the typical Python fashion, using the classes themselves as instance factories. A few of their intrinsic properties will be discussed in this sections, others in the following sections on operations and serializations.

Instances of Point, LineString, and LinearRing have as their most important attribute a finite sequence of coordinates that determines their interior, boundary, and exterior point sets. A line string can be determined by as few as 2 points, but contains an infinite number of points. Coordinate sequences are immutable. A third $z$ coordinate value may be used when constructing instances, but has no effect on geometric analysis. All operations are performed in the $x-y$ plane.

In all constructors, numeric values are converted to type float. In other words, Point ( $\boldsymbol{\theta}, \boldsymbol{0}$ ) and Point ( $\boldsymbol{\theta} . \boldsymbol{\theta}, \boldsymbol{0} . \boldsymbol{\theta}$ ) produce geometrically equivalent instances. Shapely does not check the topological simplicity or validity of instances when they are constructed as the cost is unwarranted in most cases. Validating factories are easily implemented using the :attr:is_valid predicate by users that require them.

Note: Shapely is a planar geometry library and $z$, the height above or below the plane, is ignored in geometric analysis. There is a potential pitfall for users here: coordinate tuples that differ only in $z$ are not distinguished from each other and their application can result in surprisingly invalid geometry objects. For example, LineString ( $[(\boldsymbol{\theta}, 0,0)$, $(0,0,1)])$ does not return a vertical line of unit length, but an invalid line in the plane with zero length. Similarly, Polygon $([(\theta, 0,0),(\theta, 0,1),(1,1,1)])$ is not bounded by a closed ring and is invalid.

## General Attributes and Methods

## object.area

Returns the area (float) of the object.

## object.bounds

Returns a (minx, miny, maxx, maxy) tuple (float values) that bounds the object.

## object.length

Returns the length (float) of the object.

[^2]
## object.minimum_clearance

Returns the smallest distance by which a node could be moved to produce an invalid geometry.
This can be thought of as a measure of the robustness of a geometry, where larger values of minimum clearance indicate a more robust geometry. If no minimum clearance exists for a geometry, such as a point, this will return math.infinity.

New in Shapely 1.7.1
Requires GEOS 3.6 or higher.

```
>>> from shapely import Polygon
>>> Polygon([[0, 0], [1, 0], [1, 1], [0, 1], [0, 0]]).minimum_clearance
1.0
```

object.geom_type
Returns a string specifying the Geometry Type of the object in accordance with?

```
>>> from shapely import Point, LineString
>>> Point(0, 0).geom_type
'Point'
```

object.distance (other)

Returns the minimum distance (float) to the other geometric object.

```
>>> Point(0,0).distance(Point(1,1))
1.4142135623730951
```

object.hausdorff_distance(other)
Returns the Hausdorff distance (float) to the other geometric object. The Hausdorff distance between two geometries is the furthest distance that a point on either geometry can be from the nearest point to it on the other geometry.

New in Shapely 1.6.0

```
>>> point = Point(1, 1)
>>> line = LineString([(2, 0), (2, 4), (3, 4)])
>>> point.hausdorff_distance(line)
3.605551275463989
>>> point.distance(Point(3, 4))
3.605551275463989
```

object.representative_point()

Returns a cheaply computed point that is guaranteed to be within the geometric object.

Note: This is not in general the same as the centroid.

```
>>> donut = Point(0, 0).buffer(2.0).difference(Point(0, 0).buffer(1.0))
>>> donut.centroid
<POINT (0 0)>
>>> donut.representative_point()
<POINT (1.498 0.049)>
```


## Points

```
class Point(coordinates)
```

The Point constructor takes positional coordinate values or point tuple parameters.

```
>>> from shapely import Point
>> point = Point(0.0, 0.0)
>> q = Point((0.0, 0.0))
```

A Point has zero area and zero length.

```
>>> point.area
0.0
>>> point.length
0.0
```

Its $x-y$ bounding box is a ( $\operatorname{minx}, \operatorname{miny}, \operatorname{maxx}, \operatorname{maxy}$ ) tuple.

```
>>> point.bounds
(0.0, 0.0, 0.0, 0.0)
```

Coordinate values are accessed via coords, $x, y$, and $z$ properties.

```
>>> list(point.coords)
[(0.0, 0.0)]
>>> point.x
0.0
>>> point.y
0.0
```

Coordinates may also be sliced. New in version 1.2.14.

```
>>> point.coords[:]
[(0.0, 0.0)]
```

The Point constructor also accepts another Point instance, thereby making a copy.

```
>>> Point(point)
<POINT (O 0)>
```


## LineStrings

## class LineString (coordinates)

The LineString constructor takes an ordered sequence of 2 or more ( $x, y[, z]$ ) point tuples.
The constructed LineString object represents one or more connected linear splines between the points. Repeated points in the ordered sequence are allowed, but may incur performance penalties and should be avoided. A LineString may cross itself (i.e. be complex and not simple).

Figure 1. A simple LineString on the left, a complex LineString on the right. The (MultiPoint) boundary of each is shown in black, the other points that describe the lines are shown in grey.

A LineString has zero area and non-zero length.


```
>>> from shapely import LineString
>>> line = LineString([(0, 0), (1, 1)])
>>> line.area
0.0
>>> line.length
1.4142135623730951
```

Its $x-y$ bounding box is a ( $\operatorname{minx}, \operatorname{miny}, \operatorname{maxx}, \operatorname{maxy}$ ) tuple.

```
>>> line.bounds
(0.0, 0.0, 1.0, 1.0)
```

The defining coordinate values are accessed via the coords property.

```
>>> len(line.coords)
2
>>> list(line.coords)
[(0.0, 0.0), (1.0, 1.0)]
```

Coordinates may also be sliced. New in version 1.2.14.

```
>>> line.coords[:]
[(0.0, 0.0), (1.0, 1.0)]
>>> line.coords[1:]
[(1.0, 1.0)]
```

The constructor also accepts another LineString instance, thereby making a copy.

```
>>> LineString(line)
<LINESTRING (0 0, 1 1)>
```

A LineString may also be constructed using a sequence of mixed Point instances or coordinate tuples. The individual coordinates are copied into the new object.

```
>>> LineString([Point(0.0, 1.0), (2.0, 3.0), Point(4.0, 5.0)])
<LINESTRING (0 1, 2 3, 4 5)>
```


## LinearRings

## class LinearRing(coordinates)

The LinearRing constructor takes an ordered sequence of (x, y[, z]) point tuples.
The sequence may be explicitly closed by passing identical values in the first and last indices. Otherwise, the sequence will be implicitly closed by copying the first tuple to the last index. As with a LineString, repeated points in the ordered sequence are allowed, but may incur performance penalties and should be avoided. A LinearRing may not cross itself, and may not touch itself at a single point.


Figure 2. A valid LinearRing on the left, an invalid self-touching LinearRing on the right. The points that describe the rings are shown in grey. A ring's boundary is empty.

Note: Shapely will not prevent the creation of such rings, but exceptions will be raised when they are operated on.

A LinearRing has zero area and non-zero length.

```
>>> from shapely import LinearRing
>>> ring = LinearRing([(0, 0), (1, 1), (1, 0)])
>>> ring.area
0.0
>>> ring.length
3.414213562373095
```

Its $x-y$ bounding box is a ( $\operatorname{minx}, \operatorname{miny}, \operatorname{maxx}, \operatorname{maxy}$ ) tuple.

```
>>> ring.bounds
(0.0, 0.0, 1.0, 1.0)
```

Defining coordinate values are accessed via the coords property.

```
>>> len(ring.coords)
4
>>> list(ring.coords)
[(0.0, 0.0), (1.0, 1.0), (1.0, 0.0), (0.0, 0.0)]
```

The LinearRing constructor also accepts another LineString or LinearRing instance, thereby making a copy.

```
>>> LinearRing(ring)
<LINEARRING (0 0, 1 1, 1 0, 0 0)>
```

As with LineString, a sequence of Point instances is not a valid constructor parameter.

## Polygons

```
class Polygon(shell[,holes=None ])
```

The Polygon constructor takes two positional parameters. The first is an ordered sequence of ( $x, y[, z]$ ) point tuples and is treated exactly as in the LinearRing case. The second is an optional unordered sequence of ring-like sequences specifying the interior boundaries or "holes" of the feature.

Rings of a valid Polygon may not cross each other, but may touch at a single point only. Again, Shapely will not prevent the creation of invalid features, but exceptions will be raised when they are operated on.


Figure 3. On the left, a valid Polygon with one interior ring that touches the exterior ring at one point, and on the right a Polygon that is invalid because its interior ring touches the exterior ring at more than one point. The points that describe the rings are shown in grey.

Figure 4. On the left, a Polygon that is invalid because its exterior and interior rings touch along a line, and on the right, a Polygon that is invalid because its interior rings touch along a line.

A Polygon has non-zero area and non-zero length.


```
>>> from shapely import Polygon
>>> polygon = Polygon([(0, 0), (1, 1), (1, 0)])
>>> polygon.area
0.5
>>> polygon.length
3.414213562373095
```

Its $x$ - $y$ bounding box is a (minx, miny, maxx, maxy) tuple.
>>> polygon.bounds
(0.0, 0.0, 1.0, 1.0)

Component rings are accessed via exterior and interiors properties.

```
>>> list(polygon.exterior.coords)
[(0.0, 0.0), (1.0, 1.0), (1.0, 0.0), (0.0, 0.0)]
>>> list(polygon.interiors)
[]
```

The Polygon constructor also accepts instances of LineString and LinearRing.

```
>>> coords = [(0, 0), (1, 1), (1, 0)]
>>> r = LinearRing(coords)
>>> s = Polygon(r)
>>> s.area
0.5
>>> t = Polygon(s.buffer(1.0).exterior, [r])
>>> t.area
6.5507620529190325
```

Rectangular polygons occur commonly, and can be conveniently constructed using the shapely.geometry.box() function.
shapely.geometry. box (minx, miny, maxx, maxy, ccw=True)
Makes a rectangular polygon from the provided bounding box values, with counter-clockwise order by default.
New in version 1.2.9.
For example:

```
>>> from shapely import box
>> b = box(0.0, 0.0, 1.0, 1.0)
>>> b
<POLYGON ((1 0, 1 1, 0 1, 0 0, 1 0))>
>>> list(b.exterior.coords)
[(1.0, 0.0), (1.0, 1.0), (0.0, 1.0), (0.0, 0.0), (1.0, 0.0)]
```

This is the first appearance of an explicit polygon handedness in Shapely.
To obtain a polygon with a known orientation, use shapely.geometry.polygon.orient():
shapely.geometry.polygon.orient (polygon, sign=1.0)
Returns a properly oriented copy of the given polygon. The signed area of the result will have the given sign. A sign of 1.0 means that the coordinates of the product's exterior ring will be oriented counter-clockwise and the interior rings (holes) will be oriented clockwise.

New in version 1.2.10.

## Collections

Heterogeneous collections of geometric objects may result from some Shapely operations. For example, two LineStrings may intersect along a line and at a point. To represent these kind of results, Shapely provides frozenset-like, immutable collections of geometric objects. The collections may be homogeneous (MultiPoint etc.) or heterogeneous.

```
>>> a = LineString([(0, 0), (1, 1), (1,2), (2,2)])
>>> b = LineString([(0, 0), (1, 1), (2,1), (2,2)])
>>> x = a.intersection(b)
>>> x
<GEOMETRYCOLLECTION (LINESTRING (Q 0, 1 1), POINT (2 2))>
>>> list(x.geoms)
[<LINESTRING (0 0, 1 1)>, <POINT (2 2)>]
```

Figure 5. a) a green and a yellow line that intersect along a line and at a single point; b) the intersection (in blue) is a collection containing one LineString and one Point.

Members of a GeometryCollection are accessed via the geoms property.

```
>>> list(x.geoms)
[<LINESTRING (0 0, 1 1)>, <POINT (2 2)>]
```

Note: When possible, it is better to use one of the homogeneous collection types described below.


## Collections of Points

## class MultiPoint (points)

The MultiPoint constructor takes a sequence of ( $\mathrm{x}, \mathrm{y}[\mathrm{l}, \mathrm{z}]$ ) point tuples.
A MultiPoint has zero area and zero length.

```
>>> from shapely import MultiPoint
>>> points = MultiPoint([(0.0, 0.0), (1.0, 1.0)])
>>> points.area
0.0
>>> points.length
0.0
```

Its $x-y$ bounding box is a (minx, miny, maxx, maxy) tuple.

```
>>> points.bounds
(0.0, 0.0, 1.0, 1.0)
```

Members of a multi-point collection are accessed via the geoms property.

```
>>> list(points.geoms)
[<POINT (0 0)>, <POINT (1 1)>]
```

The constructor also accepts another MultiPoint instance or an unordered sequence of Point instances, thereby making copies.

```
>>> MultiPoint([Point(0, 0), Point(1, 1)])
<MULTIPOINT (0 0, 1 1)>
```


## Collections of Lines

```
class MultiLineString(lines)
```

The MultiLineString constructor takes a sequence of line-like sequences or objects.


Figure 6. On the left, a simple, disconnected MultiLineString, and on the right, a non-simple MultiLineString. The points defining the objects are shown in gray, the boundaries of the objects in black.

A MultiLineString has zero area and non-zero length.

```
>>> from shapely import MultiLineString
>> coords = [((0, 0), (1, 1)), ((-1, 0), (1, 0))]
>>> lines = MultiLineString(coords)
>>> lines.area
0.0
>>> lines.length
3.414213562373095
```

Its $x-y$ bounding box is a (minx, miny, maxx, maxy) tuple.

```
>>> lines.bounds
(-1.0, 0.0, 1.0, 1.0)
```

Its members are instances of LineString and are accessed via the geoms property.

```
>>> len(lines.geoms)
2
>>> print(list(lines.geoms))
[<LINESTRING (0 0, 1 1)>, <LINESTRING (-1 0, 1 0)>]
```

The constructor also accepts another instance of MultiLineString or an unordered sequence of LineString instances, thereby making copies.

```
>>> MultiLineString(lines)
<MULTILINESTRING ((0 0, 1 1), (-1 0, 1 0))>
>>> MultiLineString(lines.geoms)
<MULTILINESTRING ((0 0, 1 1), (-1 0, 1 0))>
```


## Collections of Polygons

## class MultiPolygon(polygons)

The MultiPolygon constructor takes a sequence of exterior ring and hole list tuples: $[((\mathrm{a} 1, \ldots, \mathrm{aM}),[(\mathrm{b} 1, \ldots$, bN), ...]), ...].

More clearly, the constructor also accepts an unordered sequence of Polygon instances, thereby making copies.

```
>>> from shapely import MultiPolygon
>>> polygons = MultiPolygon([polygon, s, t])
>>> len(polygons.geoms)
3
```



Figure 7. On the left, a valid MultiPolygon with 2 members, and on the right, a MultiPolygon that is invalid because its members touch at an infinite number of points (along a line).

Its $x$ - $y$ bounding box is a (minx, miny, maxx, maxy) tuple.

```
>>> polygons.bounds
(-1.0, -1.0, 2.0, 2.0)
```

Its members are instances of Polygon and are accessed via the geoms property.

```
>>> len(polygons.geoms)
3
```


## Empty features

An "empty" feature is one with a point set that coincides with the empty set; not None, but like set([]). Empty features can be created by calling the various constructors with no arguments. Almost no operations are supported by empty features.

```
>>> line = LineString()
>>> line.is_empty
True
>>> line.length
0.0
>>> line.bounds
(nan, nan, nan, nan)
>>> list(line.coords)
[]
```


## Coordinate sequences

The list of coordinates that describe a geometry are represented as the CoordinateSequence object. These sequences should not be initialised directly, but can be accessed from an existing geometry as the Geometry. coords property.

```
>>> line = LineString([(0, 1), (2, 3), (4, 5)])
>>> line.coords
<shapely.coords.CoordinateSequence object at ...>
```

Coordinate sequences can be indexed, sliced and iterated over as if they were a list of coordinate tuples.

```
>>> line.coords[0]
(0.0, 1.0)
>>> line.coords[1:]
[(2.0, 3.0), (4.0, 5.0)]
>>> for x, y in line.coords:
... print("x={}, y={}".format(x, y))
...
x=0.0, y=1.0
x=2.0, y=3.0
x=4.0, y=5.0
```

Polygons have a coordinate sequence for their exterior and each of their interior rings.

```
>>> poly = Polygon([(0, 0), (0, 1), (1, 1), (0, 0)])
>>> poly.exterior.coords
<shapely.coords.CoordinateSequence object at ...>
```

Multipart geometries do not have a coordinate sequence. Instead the coordinate sequences are stored on their component geometries.

```
>>> p = MultiPoint([(0, 0), (1, 1), (2, 2)])
>>> p.geoms[2].coords
<shapely.coords.CoordinateSequence object at ...>
```


## Linear Referencing Methods

It can be useful to specify position along linear features such as LineStrings and MultiLineStrings with a 1-dimensional referencing system. Shapely supports linear referencing based on length or distance, evaluating the distance along a geometric object to the projection of a given point, or the point at a given distance along the object.
object.interpolate(distance[, normalized=False])
Return a point at the specified distance along a linear geometric object.
If the normalized arg is True, the distance will be interpreted as a fraction of the geometric object's length.

```
>>> ip = LineString([(0, 0), (0, 1), (1, 1)]).interpolate(1.5)
>>> ip
<POINT (0.5 1)>
>>> LineString([(0, 0), (0, 1), (1, 1)]).interpolate(0.75, normalized=True)
<POINT (0.5 1)>
```

object.project (other [, normalized=False])

Returns the distance along this geometric object to a point nearest the other object.
If the normalized $\arg$ is True, return the distance normalized to the length of the object. The project() method is the inverse of interpolate().

```
>>> LineString([(0, 0), (0, 1), (1, 1)]).project(ip)
1.5
>>> LineString([(0, 0), (0, 1), (1, 1)]).project(ip, normalized=True)
0.75
```

For example, the linear referencing methods might be used to cut lines at a specified distance.

```
def cut(line, distance):
    # Cuts a line in two at a distance from its starting point
    if distance <= 0.0 or distance >= line.length:
        return [LineString(line)]
    coords = list(line.coords)
    for i, p in enumerate(coords):
        pd = line.project(Point(p))
        if pd == distance:
            return [
                LineString(coords[:i+1]),
                LineString(coords[i:])]
        if pd > distance:
            cp = line.interpolate(distance)
            return [
                LineString(coords[:i] + [(cp.x, cp.y)]),
                LineString([(cp.x, cp.y)] + coords[i:])]
```

```
>>> line = LineString([(0, 0), (1, 0), (2, 0), (3, 0), (4, 0), (5, 0)])
>>> print([list(x.coords) for x in cut(line, 1.0)])
[[(0.0, 0.0), (1.0, 0.0)],
    [(1.0, 0.0), (2.0, 0.0), (3.0, 0.0), (4.0, 0.0), (5.0, 0.0)]]
>>> print([list(x.coords) for x in cut(line, 2.5)])
[[(0.0, 0.0), (1.0, 0.0), (2.0, 0.0), (2.5, 0.0)],
    [(2.5, 0.0), (3.0, 0.0), (4.0, 0.0), (5.0, 0.0)]]
```


### 5.2.3 Predicates and Relationships

Objects of the types explained in Geometric Objects provide standard? predicates as attributes (for unary predicates) and methods (for binary predicates). Whether unary or binary, all return True or False.

## Unary Predicates

Standard unary predicates are implemented as read-only property attributes. An example will be shown for each.
object.has_z
Returns True if the feature has not only $x$ and $y$, but also $z$ coordinates for 3D (or so-called, 2.5D) geometries.

```
>>> Point(0, 0).has_z
False
>>> Point(0, 0, 0).has_z
True
```

object.is_ccw
Returns True if coordinates are in counter-clockwise order (bounding a region with positive signed area). This method applies to LinearRing objects only.
New in version 1.2.10.

```
>>> LinearRing([(1,0), (1,1), (0,0)]).is_ccw
True
```

A ring with an undesired orientation can be reversed like this:

```
>>> ring = LinearRing([(0,0), (1,1), (1,0)])
>>> ring.is_ccw
False
>>> ring2 = LinearRing(list(ring.coords)[::-1])
>>> ring2.is_ccw
True
```

object.is_empty

Returns True if the feature's interior and boundary (in point set terms) coincide with the empty set.

```
>>> Point().is_empty
True
>>> Point(0, 0).is_empty
False
```

Note: With the help of the operator module's attrgetter () function, unary predicates such as is_empty can be easily used as predicates for the built in filter().

```
>>> from operator import attrgetter
>>> empties = filter(attrgetter('is_empty'), [Point(), Point(0, 0)])
>>> len(list(empties))
1
```

```
object.is_ring
```

Returns True if the feature is a closed and simple LineString. A closed feature's boundary coincides with the empty set.

```
>>> LineString([(0, 0), (1, 1), (1, -1)]).is_ring
False
>>> LinearRing([(0, 0), (1, 1), (1, -1)]).is_ring
True
```

This property is applicable to LineString and LinearRing instances, but meaningless for others.

```
object.is_simple
```

Returns True if the feature does not cross itself.

Note: The simplicity test is meaningful only for LineStrings and LinearRings.

```
>>> LineString([(0, 0), (1, 1), (1, -1), (0, 1)]).is_simple
False
```

Operations on non-simple LineStrings are fully supported by Shapely.

```
object.is_valid
```

Returns True if a feature is "valid" in the sense of?.

Note: The validity test is meaningful only for Polygons and MultiPolygons. True is always returned for other types of geometries.

A valid Polygon may not possess any overlapping exterior or interior rings. A valid MultiPolygon may not collect any overlapping polygons. Operations on invalid features may fail.

```
>>> MultiPolygon([Point(0, 0).buffer(2.0), Point(1, 1).buffer(2.0)]).is_valid
False
```

The two points above are close enough that the polygons resulting from the buffer operations (explained in a following section) overlap.

Note: The is_valid predicate can be used to write a validating decorator that could ensure that only valid objects are returned from a constructor function.

```
from functools import wraps
def validate(func):
    @wraps(func)
    def wrapper(*args, **kwargs):
        ob = func(*args, **kwargs)
        if not ob.is_valid:
            raise TopologicalError(
                            "Given arguments do not determine a valid geometric object")
        return ob
    return wrapper
```

```
>>> @validate
... def ring(coordinates):
... return LinearRing(coordinates)
*.
>> coords = [(0, 0), (1, 1), (1, -1), (0, 1)]
>>> ring(coords)
Traceback (most recent call last):
    File "<stdin>", line 1, in <module>
    File "<stdin>", line 7, in wrapper
shapely.geos.TopologicalError: Given arguments do not determine a valid geometric object
```


## Binary Predicates

Standard binary predicates are implemented as methods. These predicates evaluate topological, set-theoretic relationships. In a few cases the results may not be what one might expect starting from different assumptions. All take another geometric object as argument and return True or False.
object.__eq__(other)
Returns True if the two objects are of the same geometric type, and the coordinates of the two objects match precisely.

```
object.equals(other)
```

Returns True if the set-theoretic boundary, interior, and exterior of the object coincide with those of the other.
The coordinates passed to the object constructors are of these sets, and determine them, but are not the entirety of the sets. This is a potential "gotcha" for new users. Equivalent lines, for example, can be constructed differently.

```
>>> a = LineString([(0, 0), (1, 1)])
>>> b = LineString([(0, 0), (0.5, 0.5), (1, 1)])
>>> c = LineString([(0, 0), (0, 0), (1, 1)])
>>> a.equals(b)
True
>>> a == b
False
>>> b.equals(c)
True
>>> b == c
False
```

object.equals_exact (other, tolerance)
Returns True if the object is within a specified tolerance.

```
object.contains(other)
```

Returns True if no points of other lie in the exterior of the object and at least one point of the interior of other lies in the interior of object.

This predicate applies to all types, and is inverse to within(). The expression a.contains(b) == b.within(a) always evaluates to True.

```
>>> coords = [(0, 0), (1, 1)]
>>> LineString(coords).contains(Point(0.5, 0.5))
True
>>> Point(0.5, 0.5).within(LineString(coords))
True
```

A line's endpoints are part of its boundary and are therefore not contained.

```
>>> LineString(coords).contains(Point(1.0, 1.0))
False
```

Note: Binary predicates can be used directly as predicates for filter() or itertools.ifilter().

```
>>> line = LineString(coords)
>>> contained = list(filter(line.contains, [Point(), Point(0.5, 0.5)]))
>>> len(contained)
1
>>> contained
[<POINT (0.5 0.5)>]
```

object. covers (other)
Returns True if every point of other is a point on the interior or boundary of object. This is similar to object. contains (other) except that this does not require any interior points of other to lie in the interior of object.

```
object.covered_by(other)
```

Returns True if every point of object is a point on the interior or boundary of other. This is equivalent to other. covers (object).

New in version 1.8.

```
object.crosses(other)
```

Returns True if the interior of the object intersects the interior of the other but does not contain it, and the dimension of the intersection is less than the dimension of the one or the other.

```
>>> LineString(coords).crosses(LineString([(0, 1), (1, 0)]))
True
```

A line does not cross a point that it contains.

```
>>> LineString(coords).crosses(Point(0.5, 0.5))
False
```

object.disjoint(other)

Returns True if the boundary and interior of the object do not intersect at all with those of the other.

```
>>> Point(0, 0).disjoint(Point(1, 1))
True
```

This predicate applies to all types and is the inverse of intersects().

```
object.intersects(other)
```

Returns True if the boundary or interior of the object intersect in any way with those of the other.
In other words, geometric objects intersect if they have any boundary or interior point in common.
object. overlaps (other)
Returns True if the geometries have more than one but not all points in common, have the same dimension, and the intersection of the interiors of the geometries has the same dimension as the geometries themselves.

```
object.touches(other)
```

Returns True if the objects have at least one point in common and their interiors do not intersect with any part of the other.

Overlapping features do not therefore touch, another potential "gotcha". For example, the following lines touch at (1, 1), but do not overlap.

```
>>> a = LineString([(0, 0), (1, 1)])
>>> b = LineString([(1, 1), (2, 2)])
>>> a.touches(b)
True
```

object.within(other)
Returns True if the object's boundary and interior intersect only with the interior of the other (not its boundary or exterior).

This applies to all types and is the inverse of contains().
Used in a sorted() key, within() makes it easy to spatially sort objects. Let's say we have 4 stereotypic features: a point that is contained by a polygon which is itself contained by another polygon, and a free spirited point contained by none

```
>>> a = Point(2, 2)
>> b = Polygon([[1, 1], [1, 3], [3, 3], [3, 1]])
>>> c = Polygon([[0, 0], [0, 4], [4, 4], [4, 0]])
>>> d = Point(-1, -1)
```

and that copies of these are collected into a list

```
>>> features = [c, a, d, b, c]
```

that we'd prefer to have ordered as [d, c, c, b, a] in reverse containment order. As explained in the Python Sorting HowTo, we can define a key function that operates on each list element and returns a value for comparison. Our key function will be a wrapper class that implements __lt__() using Shapely's binary within() predicate.

```
>>> class Within:
... def __init__(self, o):
... self.o = o
... def __lt__(self, other):
... return self.o.within(other.o)
```

As the howto says, the less than comparison is guaranteed to be used in sorting. That's what we'll rely on to spatially sort. Trying it out on features $d$ and $c$, we see that it works.

```
>>> Within(d) < Within(c)
False
```

It also works on the list of features, producing the order we want.

```
>>> [d, c, c, b, a] == sorted(features, key=Within, reverse=True)
True
```


## DE-9IM Relationships

The relate() method tests all the DE-9IM ${ }^{\text {Page 21,4 }}$ relationships between objects, of which the named relationship predicates above are a subset.
object.relate (other)
Returns a string representation of the DE-9IM matrix of relationships between an object's interior, boundary, exterior and those of another geometric object.

The named relationship predicates (contains(), etc.) are typically implemented as wrappers around relate().
Two different points have mainly F (false) values in their matrix; the intersection of their external sets (the 9th element) is a 2 dimensional object (the rest of the plane). The intersection of the interior of one with the exterior of the other is a 0 dimensional object (3rd and 7th elements of the matrix).

```
>>> Point(Q, 0).relate(Point(1, 1))
'FFOFFFQF2'
```

The matrix for a line and a point on the line has more "true" (not F) elements.

```
>>> Point(0, 0).relate(LineString([(0, 0), (1, 1)]))
'FOFFFF102'
```

object.relate_pattern(other, pattern)

Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, otherwise False.

The relate_pattern() compares the DE-9IM code string for two geometries against a specified pattern. If the string matches the pattern then True is returned, otherwise False. The pattern specified can be an exact match ( 0,1 or 2 ), a


```
>>> point = Point(0.5, 0.5)
>>> square = Polygon([(0, 0), (0, 1), (1, 1), (1, 0)])
>>> square.relate_pattern(point, 'T*****FF*')
True
>>> point.within(square)
True
```

Note that the order or the geometries is significant, as demonstrated below. In this example the square contains the point, but the point does not contain the square.

```
>>> point.relate(square)
'0FFFFF212'
>>> square.relate(point)
'0F2FF1FF2'
```

Further discussion of the DE-9IM matrix is beyond the scope of this manual. See ${ }^{\text {Page } 21,4}$ and https://pypi.org/project/ de9im/.

### 5.2.4 Spatial Analysis Methods

As well as boolean attributes and methods, Shapely provides analysis methods that return new geometric objects.

## Set-theoretic Methods

Almost every binary predicate method has a counterpart that returns a new geometric object. In addition, the settheoretic boundary of an object is available as a read-only attribute.

Note: These methods will always return a geometric object. An intersection of disjoint geometries for example will return an empty GeometryCollection, not None or False. To test for a non-empty result, use the geometry's is_empty property.

## object.boundary

Returns a lower dimensional object representing the object's set-theoretic boundary.
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty collection.

```
>>> coords = [((0, 0), (1, 1)), ((-1, 0), (1, 0))]
>>> lines = MultiLineString(coords)
>>> lines.boundary
<MULTIPOINT (-1 0, 0 0, 1 0, 1 1)>
>>> list(lines.boundary.geoms)
[<POINT (-1 0)>, <POINT (0 0)>, <POINT (1 0)>, <POINT (1 1)>]
>>> lines.boundary.boundary
<GEOMETRYCOLLECTION EMPTY>
```

See the figures in LineStrings and Collections of Lines for the illustration of lines and their boundaries.

```
object.centroid
```

Returns a representation of the object's geometric centroid (point).

```
>>> LineString([(0, 0), (1, 1)]).centroid
<POINT (0.5 0.5)>
```

Note: The centroid of an object might be one of its points, but this is not guaranteed.

```
object.difference(other)
```

Returns a representation of the points making up this geometric object that do not make up the other object.

```
>>> a = Point(1, 1).buffer(1.5)
>>> b = Point(2, 1).buffer(1.5)
>>> a.difference(b)
<POLYGON ((1.435-0.435, 1.293-0.471, 1.147-0.493, 1 -0.5, 0.853-0.493, 0...>
```

Note: The buffer () method is used to produce approximately circular polygons in the examples of this section; it will be explained in detail later in this manual.

Figure 8. Differences between two approximately circular polygons.


Note: Shapely can not represent the difference between an object and a lower dimensional object (such as the difference between a polygon and a line or point) as a single object, and in these cases the difference method returns a copy of the object named self.
object.intersection(other)
Returns a representation of the intersection of this object with the other geometric object.

```
>>> a = Point(1, 1).buffer(1.5)
>> b = Point(2, 1).buffer(1.5)
>>> a.intersection(b)
<POLYGON ((2.493 0.853, 2.471 0.707, 2.435 0.565, 2.386 0.426, 2.323 0.293, ...>
```

See the figure under symmetric_difference() below.

```
object.symmetric_difference(other)
```

Returns a representation of the points in this object not in the other geometric object, and the points in the other not in this geometric object.

```
>>> a = Point(1, 1).buffer(1.5)
>>> b = Point(2, 1).buffer(1.5)
>>> a.symmetric_difference(b)
<MULTIPOLYGON (( (1.574-0.386, 1.707 -0.323, 1.833-0.247, 1.952 -0.16, 2.06...>
```

object.union(other)
Returns a representation of the union of points from this object and the other geometric object.
The type of object returned depends on the relationship between the operands. The union of polygons (for example) will be a polygon or a multi-polygon depending on whether they intersect or not.

```
>>> a = Point(1, 1).buffer(1.5)
>>> b = Point(2, 1).buffer(1.5)
>>> a.union(b)
<POLYGON ((1.435-0.435, 1.293-0.471, 1.147-0.493, 1 -0.5, 0.853-0.493, 0...>
```



The semantics of these operations vary with type of geometric object. For example, compare the boundary of the union of polygons to the union of their boundaries.

```
>>> a.union(b).boundary
<LINESTRING (1.435 -0.435, 1.293-0.471, 1.147-0.493, 1 -0.5, 0.853 -0.493,...>
>>> a.boundary.union(b.boundary)
<MULTILINESTRING ((2.5 1, 2.493 0.853, 2.471 0.707, 2.435 0.565, 2.386 0.426...>
```



Note: union() is an expensive way to find the cumulative union of many objects. See shapely.unary_union() for a more effective method.

Several of these set-theoretic methods can be invoked using overloaded operators:

- intersection can be accessed with and, \&
- union can be accessed with or, |
- difference can be accessed with minus, -
- symmetric_difference can be accessed with xor, $\wedge$

```
>>> from shapely import wkt
>>> p1 = wkt.loads('POLYGON((0 0, 1 0, 1 1, 0 1, 0 0))')
>>> p2 = wkt.loads('POLYGON((0.5 0, 1.5 0, 1.5 1, 0.5 1, 0.5 0))')
>>> p1 & p2
<POLYGON ((0.5 0, 0.5 1, 1 1, 1 0, 0.5 0))>
>>> p1 | p2
<POLYGON ((0 0, 0 1, 0.5 1, 1 1, 1.5 1, 1.5 0, 1 0, 0.5 0, 0 0))>
>>> p1 - p2
<POLYGON ((Q 0, 0 1, 0.5 1, 0.5 0, 0 0))>
>> (p1 ^ p2).wkt
'MULTIPOLYGON (((0 0, 0 1, 0.5 1, 0.5 0, 0 0)), ((1 1, 1.5 1, 1.5 0, 1 0, 1 1)))'
```


## Constructive Methods

Shapely geometric object have several methods that yield new objects not derived from set-theoretic analysis.
object. buffer (distance, quad_segs=16, cap_style=1, join_style=1, mitre_limit=5.0, single_sided=False)
Returns an approximate representation of all points within a given distance of the this geometric object.
The styles of caps are specified by integer values: 1 (round), 2 (flat), 3 (square). These values are also enumerated by the object shapely. BufferCapStyle (see below).

The styles of joins between offset segments are specified by integer values: 1 (round), 2 (mitre), and 3 (bevel). These values are also enumerated by the object shapely. BufferJoinStyle (see below).

```
shapely.BufferCapStyle
```

| Attribute | Value |
| :--- | :--- |
| round | 1 |
| flat | 2 |
| square | 3 |

shapely.BufferJoinStyle

| Attribute | Value |
| :--- | :--- |
| round | 1 |
| mitre | 2 |
| bevel | 3 |

```
>>> from shapely import BufferCapStyle, BufferJoinStyle
>>> BufferCapStyle.flat.value
2
>>> BufferJoinStyle.bevel.value
3
```

A positive distance has an effect of dilation; a negative distance, erosion. The optional quad_segs argument determines the number of segments used to approximate a quarter circle around a point.

```
>>> line = LineString([(0, 0), (1, 1), (0, 2), (2, 2), (3, 1), (1, 0)])
>>> dilated = line.buffer(0.5)
>>> eroded = dilated.buffer(-0.3)
```



Figure 9. Dilation of a line (left) and erosion of a polygon (right). New object is shown in blue.
The default (quad_segs of 16) buffer of a point is a polygonal patch with $99.8 \%$ of the area of the circular disk it approximates.

```
>>> p = Point(0, 0).buffer(10.0)
>>> len(p.exterior.coords)
65
>>> p.area
313.6548490545941
```

With a quad_segs of 1 , the buffer is a square patch.

```
>>> q = Point(0, 0).buffer(10.0, 1)
>>> len(q.exterior.coords)
5
>>> q.area
200.0
```

You may want a buffer only on one side. You can achieve this effect with single_sided option.
The side used is determined by the sign of the buffer distance:

- a positive distance indicates the left-hand side
- a negative distance indicates the right-hand side

```
>>> line = LineString([(0, 0), (1, 1), (0, 2), (2, 2), (3, 1), (1, 0)])
>>> left_hand_side = line.buffer(0.5, single_sided=True)
>>> right_hand_side = line.buffer(-0.3, single_sided=True)
```

Figure 10. Single sided buffer of 0.5 left hand (left) and of 0.3 right hand (right).
The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of BufferCapStyle.flat.

Passed a distance of 0, buffer () can sometimes be used to "clean" self-touching or self-crossing polygons such as the classic "bowtie". Users have reported that very small distance values sometimes produce cleaner results than 0 . Your mileage may vary when cleaning surfaces.


```
>>> coords = [(0, 0), (0, 2), (1, 1), (2, 2), (2, 0), (1, 1), (0, 0)]
>>> bowtie = Polygon(coords)
>>> bowtie.is_valid
False
>>> clean = bowtie.buffer(0)
>>> clean.is_valid
True
>>> clean
<MULTIPOLYGON (((0 0, 0 2, 1 1, 0 0)), ((1 1, 2 2, 2 0, 1 1)))>
>>> len(clean.geoms)
2
>>> list(clean.geoms[0].exterior.coords)
[(0.0, 0.0), (0.0, 2.0), (1.0, 1.0), (0.0, 0.0)]
>>> list(clean.geoms[1].exterior.coords)
[(1.0, 1.0), (2.0, 2.0), (2.0, 0.0), (1.0, 1.0)]
```

Buffering splits the polygon in two at the point where they touch.

```
object.convex_hull
```

Returns a representation of the smallest convex Polygon containing all the points in the object unless the number of points in the object is less than three. For two points, the convex hull collapses to a LineString; for 1, a Point.

```
>>> Point(0, 0).convex_hull
<POINT (O O)>
>>> MultiPoint([(0, 0), (1, 1)]).convex_hull
<LINESTRING (0 0, 1 1)>
>>> MultiPoint([(0, 0), (1, 1), (1, -1)]).convex_hull
<POLYGON ((1 -1, 0 0, 1 1, 1 -1))>
```

Figure 11. Convex hull (blue) of 2 points (left) and of 6 points (right).

## object.envelope

Returns a representation of the point or smallest rectangular polygon (with sides parallel to the coordinate axes) that contains the object.


```
>>> Point(0, 0).envelope
<POINT (O O)>
>>> MultiPoint([(0, 0), (1, 1)]).envelope
<POLYGON ((0 0, 1 0, 1 1, 0 1, 0 0))>
```

object.minimum_rotated_rectangle

Returns the general minimum bounding rectangle that contains the object. Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

New in Shapely 1.6.0

```
>>> Point(0, 0).minimum_rotated_rectangle
<POINT (O O)>
>>> MultiPoint([(0,0), (1, 1), (2,0.5)]).minimum_rotated_rectangle
<POLYGON ((2 0.5, 1.824 1.206, -0.176 0.706, 0 0, 2 0.5))>
```

Figure 12. Minimum rotated rectangle for a multipoint feature (left) and a linestring feature (right).
object.parallel_offset (distance, side, resolution=16, join_style=1, mitre_limit=5.0)
Returns a LineString or MultiLineString geometry at a distance from the object on its right or its left side.
Older alternative method to the offset_curve() method, but uses resolution instead of quad_segs and a side keyword ('left' or 'right') instead of sign of the distance. This method is kept for backwards compatibility for now, but is is recommended to use offset_curve() instead.
object.offset_curve(distance, quad_segs=16, join_style=1, mitre_limit=5.0)
Returns a LineString or MultiLineString geometry at a distance from the object on its right or its left side.
The distance parameter must be a float value.
The side is determined by the sign of the distance parameter (negative for right side offset, positive for left side offset). Left and right are determined by following the direction of the given geometric points of the LineString.

Note: the behaviour regarding orientation of the resulting line depends on the GEOS version. With GEOS < 3.11, the line retains the same direction for a left offset (positive distance) or has reverse direction for a right offset (negative distance), and this behaviour was documented as such in previous Shapely versions. Starting with GEOS 3.11, the function tries to preserve the orientation of the original line.


The resolution of the offset around each vertex of the object is parameterized as in the buffer() method (using quad_segs).

The join_style is for outside corners between line segments. Accepted integer values are 1 (round), 2 (mitre), and 3 (bevel). See also shapely. BufferJoinStyle.

Severely mitered corners can be controlled by the mitre_limit parameter (spelled in British English, en-gb). The corners of a parallel line will be further from the original than most places with the mitre join style. The ratio of this further distance to the specified distance is the miter ratio. Corners with a ratio which exceed the limit will be beveled.

Note: This method may sometimes return a MultiLineString where a simple LineString was expected; for example, an offset to a slightly curved LineString.

Note: This method is only available for LinearRing and LineString objects.

Figure 13. Three styles of parallel offset lines on the left side of a simple line string (its starting point shown as a circle) and one offset on the right side, a multipart.

The effect of the mitre_limit parameter is shown below.
Figure 14. Large and small mitre_limit values for left and right offsets.
object.simplify(tolerance, preserve_topology=True)
Returns a simplified representation of the geometric object.
All points in the simplified object will be within the tolerance distance of the original geometry. By default a slower algorithm is used that preserves topology. If preserve topology is set to False the much quicker Douglas-Peucker algorithm ${ }^{6}$ is used.

[^3]


```
>>> p = Point(0.0, 0.0)
>>> x = p.buffer(1.0)
>>> x.area
3.1365484905459398
>>> len(x.exterior.coords)
65
>>> s = x.simplify(0.05, preserve_topology=False)
>>> s.area
3.061467458920719
>>> len(s.exterior.coords)
17
```



Figure 15. Simplification of a nearly circular polygon using a tolerance of 0.2 (left) and 0.5 (right).

Note: Invalid geometric objects may result from simplification that does not preserve topology and simplification may be sensitive to the order of coordinates: two geometries differing only in order of coordinates may be simplified differently.

### 5.2.5 Affine Transformations

A collection of affine transform functions are in the shapely. affinity module, which return transformed geometries by either directly supplying coefficients to an affine transformation matrix, or by using a specific, named transform (rotate, scale, etc.). The functions can be used with all geometry types (except GeometryCollection), and 3D types are either preserved or supported by 3D affine transformations.

New in version 1.2.17.
shapely.affinity.affine_transform (geom, matrix)
Returns a transformed geometry using an affine transformation matrix.
The coefficient matrix is provided as a list or tuple with 6 or 12 items for 2D or 3D transformations, respectively.

For 2D affine transformations, the 6 parameter matrix is:
[a, b, d, e, xoff, yoff]
which represents the augmented matrix:

$$
\left[\begin{array}{c}
x^{\prime} \\
y^{\prime} \\
1
\end{array}\right]=\left[\begin{array}{ccc}
a & b & x_{\text {off }} \\
d & e & y_{\text {off }} \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
x \\
y \\
1
\end{array}\right]
$$

or the equations for the transformed coordinates:

$$
\begin{aligned}
& x^{\prime}=a x+b y+x_{\text {off }} \\
& y^{\prime}=d x+e y+y_{\text {off }} .
\end{aligned}
$$

For 3D affine transformations, the 12 parameter matrix is:

$$
[a, b, c, d, e, f, g, h, i, x o f f, y o f f, z o f f]
$$

which represents the augmented matrix:

$$
\left[\begin{array}{c}
x^{\prime} \\
y^{\prime} \\
z^{\prime} \\
1
\end{array}\right]=\left[\begin{array}{lllc}
a & b & c & x_{\mathrm{off}} \\
d & e & f & y_{\text {off }} \\
g & h & i & z_{\mathrm{off}} \\
0 & 0 & 0 & 1
\end{array}\right]\left[\begin{array}{c}
x \\
y \\
z \\
1
\end{array}\right]
$$

or the equations for the transformed coordinates:

$$
\begin{aligned}
x^{\prime} & =a x+b y+c z+x_{\mathrm{off}} \\
y^{\prime} & =d x+e y+f z+y_{\mathrm{off}} \\
z^{\prime} & =g x+h y+i z+z_{\mathrm{off}} .
\end{aligned}
$$

shapely.affinity.rotate (geom, angle, origin='center', use_radians=False)
Returns a rotated geometry on a 2D plane.
The angle of rotation can be specified in either degrees (default) or radians by setting use_radians=True. Positive angles are counter-clockwise and negative are clockwise rotations.
The point of origin can be a keyword 'center' for the bounding box center (default), 'centroid' for the geometry's centroid, a Point object or a coordinate tuple ( $\mathrm{x} \mathcal{Q}, \mathrm{y} 0$ ).
The affine transformation matrix for 2 D rotation with angle $\theta$ is:

$$
\left[\begin{array}{ccc}
\cos \theta & -\sin \theta & x_{\text {off }} \\
\sin \theta & \cos \theta & y_{\text {off }} \\
0 & 0 & 1
\end{array}\right]
$$

where the offsets are calculated from the origin $\left(x_{0}, y_{0}\right)$ :

$$
\begin{aligned}
x_{\mathrm{off}} & =x_{0}-x_{0} \cos \theta+y_{0} \sin \theta \\
y_{\text {off }} & =y_{0}-x_{0} \sin \theta-y_{0} \cos \theta
\end{aligned}
$$

```
>>> from shapely import affinity
>>> line = LineString([(1, 3), (1, 1), (4, 1)])
>>> rotated_a = affinity.rotate(line, 90)
>>> rotated_b = affinity.rotate(line, 90, origin='centroid')
```

Figure 16. Rotation of a LineString (gray) by an angle of $90^{\circ}$ counter-clockwise (blue) using different origins.

shapely.affinity.scale(geom, xfact=1.0, yfact=1.0, zfact=1.0, origin='center')
Returns a scaled geometry, scaled by factors along each dimension.
The point of origin can be a keyword 'center' for the 2D bounding box center (default), ' centroid' for the geometry's 2D centroid, a Point object or a coordinate tuple ( $\mathrm{x} 0, \mathrm{y} 0, \mathrm{z} \boldsymbol{0}$ ).

Negative scale factors will mirror or reflect coordinates.
The general 3D affine transformation matrix for scaling is:

$$
\left[\begin{array}{cccc}
x_{\text {fact }} & 0 & 0 & x_{\text {off }} \\
0 & y_{\text {fact }} & 0 & y_{\text {off }} \\
0 & 0 & z_{\text {fact }} & z_{\text {off }} \\
0 & 0 & 0 & 1
\end{array}\right]
$$

where the offsets are calculated from the origin $\left(x_{0}, y_{0}, z_{0}\right)$ :

$$
\begin{aligned}
x_{\mathrm{off}} & =x_{0}-x_{0} x_{\mathrm{fact}} \\
y_{\mathrm{off}} & =y_{0}-y_{0} y_{\mathrm{fact}} \\
z_{\mathrm{off}} & =z_{0}-z_{0} z_{\mathrm{fact}}
\end{aligned}
$$

```
>>> triangle = Polygon([(1, 1), (2, 3), (3, 1)])
>>> triangle_a = affinity.scale(triangle, xfact=1.5, yfact=-1)
>>> triangle_a.exterior.coords[:]
[(0.5, 3.0), (2.0, 1.0), (3.5, 3.0), (0.5, 3.0)]
>>> triangle_b = affinity.scale(triangle, xfact=2, origin=(1,1))
>>> triangle_b.exterior.coords[:]
[(1.0, 1.0), (3.0, 3.0), (5.0, 1.0), (1.0, 1.0)]
```

Figure 17. Scaling of a gray triangle to blue result: a) by a factor of 1.5 along $x$-direction, with reflection across $y$-axis; b) by a factor of 2 along x-direction with custom origin at $(1,1)$.
shapely.affinity.skew (geom, $x s=0.0, y s=0.0$, origin='center', use_radians=False)
Returns a skewed geometry, sheared by angles along $x$ and $y$ dimensions.
The shear angle can be specified in either degrees (default) or radians by setting use_radians=True.


The point of origin can be a keyword 'center' for the bounding box center (default), 'centroid' for the geometry's centroid, a Point object or a coordinate tuple ( $\mathrm{x} \mathcal{0}, \mathrm{y} 0$ ).
The general 2D affine transformation matrix for skewing is:

$$
\left[\begin{array}{ccc}
1 & \tan x_{s} & x_{\text {off }} \\
\tan y_{s} & 1 & y_{\text {off }} \\
0 & 0 & 1
\end{array}\right]
$$

where the offsets are calculated from the origin $\left(x_{0}, y_{0}\right)$ :

$$
\begin{aligned}
& x_{\mathrm{off}}=-y_{0} \tan x_{s} \\
& y_{\mathrm{off}}=-x_{0} \tan y_{s}
\end{aligned}
$$



Figure 18. Skewing of a gray " R " to blue result: a) by a shear angle of $20^{\circ}$ along the x -direction and an origin at $(1,1)$; b) by a shear angle of $30^{\circ}$ along the y-direction, using default origin.
shapely.affinity.translate (geom, $x o f f=0.0$, yoff $=0.0$, zoff $=0.0$ )
Returns a translated geometry shifted by offsets along each dimension.
The general 3D affine transformation matrix for translation is:

$$
\left[\begin{array}{cccc}
1 & 0 & 0 & x_{\text {off }} \\
0 & 1 & 0 & y_{\text {off }} \\
0 & 0 & 1 & z_{\text {off }} \\
0 & 0 & 0 & 1
\end{array}\right]
$$

### 5.2.6 Other Transformations

Shapely supports map projections and other arbitrary transformations of geometric objects.

## shapely.ops.transform (func, geom)

Applies func to all coordinates of geom and returns a new geometry of the same type from the transformed coordinates.
func maps $\mathrm{x}, \mathrm{y}$, and optionally z to output $\mathrm{xp}, \mathrm{yp}, \mathrm{zp}$. The input parameters may be iterable types like lists or arrays or single values. The output shall be of the same type: scalars in, scalars out; lists in, lists out.
transform tries to determine which kind of function was passed in by calling func first with n iterables of coordinates, where n is the dimensionality of the input geometry. If func raises a TypeError when called with iterables as arguments, then it will instead call func on each individual coordinate in the geometry.

New in version 1.2.18.
For example, here is an identity function applicable to both types of input (scalar or array).

```
def id_func(x, y, z=None):
    return tuple(filter(None, [x, y, z]))
g2 = transform(id_func, g1)
```

If using pyproj>=2.1.0, the preferred method to project geometries is:

```
import pyproj
from shapely import Point
from shapely.ops import transform
wgs84_pt = Point(-72.2495, 43.886)
wgs84 = pyproj.CRS('EPSG:4326')
utm = pyproj.CRS('EPSG:32618')
project = pyproj.Transformer.from_crs(wgs84, utm, always_xy=True).transform
utm_point = transform(project, wgs84_pt)
```

It is important to note that in the example above, the always_xy kwarg is required as Shapely only supports coordinates in X,Y order, and in PROJ 6 the WGS84 CRS uses the EPSG-defined Lat/Lon coordinate order instead of the expected Lon/Lat.

If using pyproj $<2.1$, then the canonical example is:

```
from functools import partial
import pyproj
from shapely.ops import transform
wgs84 = pyproj.Proj(init='epsg:4326')
utm = pyproj.Proj(init='epsg:32618')
project = partial(
    pyproj.transform,
    wgs84,
    utm)
utm_point = transform(project, wgs84_pt)
```

Lambda expressions such as the one in

```
g2 = transform(lambda x, y, z=None: (x+1.0, y+1.0), g1)
```

also satisfy the requirements for func.

### 5.2.7 Other Operations

## Merging Linear Features

Sequences of touching lines can be merged into MultiLineStrings or Polygons using functions in the shapely.ops module.
shapely.ops.polygonize(lines)
Returns an iterator over polygons constructed from the input lines.
As with the MultiLineString constructor, the input elements may be any line-like object.

```
>>> from shapely.ops import polygonize
>>> lines = [
#. ((0, 0), (1, 1)),
# ((0, 0), (0, 1)),
# ((0, 1), (1, 1)),
# ((1, 1), (1, 0)),
# ((1, 0), (0, 0))
... ]
>>> list(polygonize(lines))
[<POLYGON ((O 0, 1 1, 1 0, O 0))>, <POLYGON ((1 1, 0 0, 0 1, 1 1))>]
```

shapely.ops.polygonize_full(lines)
Creates polygons from a source of lines, returning the polygons and leftover geometries.
The source may be a MultiLineString, a sequence of LineString objects, or a sequence of objects than can be adapted to LineStrings.

Returns a tuple of objects: (polygons, cut edges, dangles, invalid ring lines). Each are a geometry collection.
Dangles are edges which have one or both ends which are not incident on another edge endpoint. Cut edges are connected at both ends but do not form part of polygon. Invalid ring lines form rings which are invalid (bowties, etc).

New in version 1.2.18.

```
>>> from shapely.ops import polygonize_full
>>> lines = [
#..}((0,0),(1, 1))
# ((0, 0), (0, 1)),
# ((0, 1), (1, 1)),
# ((1, 1), (1, 0)),
# ((1, 0), (0, 0)),
# ((5, 5), (6, 6)),
#.. ((1, 1), (100, 100)),
... ]
>>> result, cuts, dangles, invalids = polygonize_full(lines)
>>> len(result.geoms)
2
>>> list(result.geoms)
[<POLYGON ((O 0, 1 1, 1 0, O 0))>, <POLYGON ((1 1, 0 0, 0 1, 1 1))>]
>>> list(dangles.geoms)
[<LINESTRING (1 1, 100 100)>, <LINESTRING (5 5, 6 6)>]
```

shapely.ops.linemerge(lines)
Returns a LineString or MultiLineString representing the merger of all contiguous elements of lines.
As with shapely.ops.polygonize(), the input elements may be any line-like object.

```
>>> from shapely.ops import linemerge
>>> linemerge(lines)
<MULTILINESTRING ((1 1, 1 0, 0 0), (0 0, 1 1), (0 0, 0 1, 1 1), (1 1, 100 10...>
>>> list(linemerge(lines).geoms)
[<LINESTRING (1 1, 1 0, 0 0)>,
<LINESTRING (0 0, 1 1)>,
<LINESTRING (Q 0, 0 1, 1 1)>,
<LINESTRING (1 1, 100 100)>,
<LINESTRING (5 5, 6 6)>]
```


## Efficient Rectangle Clipping

The clip_by_rect () function in shapely.ops returns the portion of a geometry within a rectangle.
shapely.ops.clip_by_rect(geom, xmin, ymin, xmax, ymax)
The geometry is clipped in a fast but possibly dirty way. The output is not guaranteed to be valid. No exceptions will be raised for topological errors.

New in version 1.7.
Requires GEOS 3.5.0 or higher

```
>>> from shapely.ops import clip_by_rect
>>> polygon = Polygon(
# shell=[(0, 0), (0, 30), (30, 30), (30, 0), (0, 0)],
# holes=[[(10, 10), (20, 10), (20, 20), (10, 20), (10, 10)]],
...)
>>> clipped_polygon = clip_by_rect(polygon, 5, 5, 15, 15)
>>> clipped_polygon
<POLYGON ((5 5, 5 15, 10 15, 10 10, 15 10, 15 5, 5 5))>
```


## Efficient Unions

The unary_union() function in shapely.ops is more efficient than accumulating with union().

shapely.ops.unary_union(geoms)
Returns a representation of the union of the given geometric objects.
Areas of overlapping Polygons will get merged. LineStrings will get fully dissolved and noded. Duplicate Points will get merged.

```
>>> from shapely.ops import unary_union
>>> polygons = [Point(i, 0).buffer(0.7) for i in range(5)]
>>> unary_union(polygons)
<POLYGON (C0.444-0.541, 0.389-0.582, 0.33-0.617, 0.268-0.647, 0.203 -0.6...>
```

Because the union merges the areas of overlapping Polygons it can be used in an attempt to fix invalid MultiPolygons. As with the zero distance buffer() trick, your mileage may vary when using this.

```
>>> m = MultiPolygon(polygons)
>>> m.area
7.684543801837549
>>> m.is_valid
False
>>> unary_union(m).area
6.610301355116799
>>> unary_union(m).is_valid
True
```

shapely.ops.cascaded_union(geoms)
Returns a representation of the union of the given geometric objects.

Note: In 1.8.0 shapely.ops.cascaded_union() is deprecated, as it was superseded by shapely.ops. unary_union().

## Delaunay triangulation

The triangulate() function in shapely.ops calculates a Delaunay triangulation from a collection of points.


```
shapely.ops.triangulate(geom,tolerance=0.0, edges=False)
```

Returns a Delaunay triangulation of the vertices of the input geometry.
The source may be any geometry type. All vertices of the geometry will be used as the points of the triangulation.
The tolerance keyword argument sets the snapping tolerance used to improve the robustness of the triangulation computation. A tolerance of 0.0 specifies that no snapping will take place.

If the edges keyword argument is False a list of Polygon triangles will be returned. Otherwise a list of LineString edges is returned.

New in version 1.4.0

```
>>> from shapely.ops import triangulate
>>> points = MultiPoint([(0, 0), (1, 1), (0, 2), (2, 2), (3, 1), (1, 0)])
>>> triangulate(points)
[<POLYGON ((0 2, 0 0, 1 1, 0 2))>,
<POLYGON ((0 2, 1 1, 2 2, 0 2))>,
<POLYGON ((2 2, 1 1, 3 1, 2 2))>,
<POLYGON ((3 1, 1 1, 1 0, 3 1))>,
<POLYGON ((1 0, 1 1, 0 0, 1 0))>]
```


## Voronoi Diagram

The voronoi_diagram() function in shapely.ops constructs a Voronoi diagram from a collection points, or the vertices of any geometry.

shapely.ops.voronoi_diagram(geom, envelope $=$ None, tolerance $=0.0$, edges=False)
Constructs a Voronoi diagram from the vertices of the input geometry.
The source may be any geometry type. All vertices of the geometry will be used as the input points to the diagram.
The envelope keyword argument provides an envelope to use to clip the resulting diagram. If None, it will be calculated automatically. The diagram will be clipped to the larger of the provided envelope or an envelope surrounding the sites.

The tolerance keyword argument sets the snapping tolerance used to improve the robustness of the computation. A tolerance of 0.0 specifies that no snapping will take place. The tolerance argument can be finicky and is known to cause the algorithm to fail in several cases. If you're using tolerance and getting a failure, try removing it. The test cases in tests/test_voronoi_diagram.py show more details.

If the edges keyword argument is False a list of Polygon `s will be returned. Otherwise a list of LineString edges is returned.

```
>>> from shapely.ops import voronoi_diagram
>>> points = MultiPoint([(0, 0), (1, 1), (0, 2), (2, 2), (3, 1), (1, 0)])
>>> regions = voronoi_diagram(points)
>>> list(regions.geoms)
[<POLYGON ((2 1, 2 0.5, 0.5 0.5, 0 1, 1 2, 2 1))>,
<POLYGON ((6 -3, 3.75-3, 2 0.5, 2 1, 6 5, 6 -3))>,
```

(continues on next page)

```
<POLYGON ((-3 -3, -3 1, 0 1, 0.5 0.5, 0.5 -3, -3 -3))>,
<POLYGON ((0.5 -3, 0.5 0.5, 2 0.5, 3.75 -3, 0.5 -3))>,
<POLYGON ((-3 5, 1 5, 1 2, 0 1, -3 1, -3 5))>,
<POLYGON ((6 5, 2 1, 1 2, 1 5, 6 5))>]
```


## Nearest points

The nearest_points() function in shapely.ops calculates the nearest points in a pair of geometries.
shapely.ops.nearest_points(geom1, geom2)
Returns a tuple of the nearest points in the input geometries. The points are returned in the same order as the input geometries.

New in version 1.4.0.

```
>>> from shapely.ops import nearest_points
>>> triangle = Polygon([(0, 0), (1, 0), (0.5, 1), (0, 0)])
>>> square = Polygon([(0, 2), (1, 2), (1, 3), (0, 3), (0, 2)])
>>> list(nearest_points(triangle, square))
[<POINT (0.5 1)>, <POINT (0.5 2)>]
```

Note that the nearest points may not be existing vertices in the geometries.

## Snapping

The snap() function in shapely.ops snaps the vertices in one geometry to the vertices in a second geometry with a given tolerance.
shapely.ops.snap (geom1, geom2, tolerance)
Snaps vertices in geoml to vertices in the geom2. A copy of the snapped geometry is returned. The input geometries are not modified.

The tolerance argument specifies the minimum distance between vertices for them to be snapped.
New in version 1.5.0

```
>>> from shapely.ops import snap
>>> square = Polygon([(1,1), (2, 1), (2, 2), (1, 2), (1, 1)])
>>> line = LineString([(0.0), (0.8, 0.8), (1.8, 0.95), (2.6, 0.5)])
>>> result = snap(line, square, 0.5)
>>> result
<LINESTRING (0 0, 1 1, 2 1, 2.6 0.5)>
```


## Shared paths

The shared_paths() function in shapely.ops finds the shared paths between two linear geometries.

```
shapely.ops.shared_paths(geom1, geom2)
```

Finds the shared paths between geom1 and geom2, where both geometries are LineStrings.
A GeometryCollection is returned with two elements. The first element is a MultiLineString containing shared paths with the same direction for both inputs. The second element is a MultiLineString containing shared paths with the opposite direction for the two inputs.
New in version 1.6.0

```
>>> from shapely.ops import shared_paths
>>> g1 = LineString([(0, 0), (10, 0), (10, 5), (20, 5)])
>>> g2 = LineString([(5, 0), (30, 0), (30, 5), (0, 5)])
>>> forward, backward = shared_paths(g1, g2).geoms
>>> forward
<MULTILINESTRING ((5 0, 10 0))>
>>> backward
<MULTILINESTRING ((10 5, 20 5))>
```


## Splitting

The split() function in shapely.ops splits a geometry by another geometry.
shapely.ops.split(geom, splitter)
Splits a geometry by another geometry and returns a collection of geometries. This function is the theoretical opposite of the union of the split geometry parts. If the splitter does not split the geometry, a collection with a single geometry equal to the input geometry is returned.
The function supports:

- Splitting a (Multi)LineString by a (Multi)Point or (Multi)LineString or (Multi)Polygon boundary
- Splitting a (Multi)Polygon by a LineString

It may be convenient to snap the splitter with low tolerance to the geometry. For example in the case of splitting a line by a point, the point must be exactly on the line, for the line to be correctly split. When splitting a line by a polygon, the boundary of the polygon is used for the operation. When splitting a line by another line, a ValueError is raised if the two overlap at some segment.
New in version 1.6.0

```
>>> from shapely.ops import split
>>> pt = Point((1, 1))
>>> line = LineString([(0,0), (2,2)])
>>> result = split(line, pt)
>>> result
<GEOMETRYCOLLECTION (LINESTRING (0 0, 1 1), LINESTRING (1 1, 2 2))>
```


## Substring

The substring() function in shapely. ops returns a line segment between specified distances along a LineString.
shapely.ops.substring(geom, start_dist, end_dist[, normalized=False])
Return the LineString between start_dist and end_dist or a Point if they are at the same location
Negative distance values are taken as measured in the reverse direction from the end of the geometry. Out-ofrange index values are handled by clamping them to the valid range of values.
If the start distance equals the end distance, a point is being returned.
If the start distance is actually past the end distance, then the reversed substring is returned such that the start distance is at the first coordinate.

If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length
New in version 1.7.0
Here are some examples that return LineString geometries.

```
>>> from shapely.ops import substring
>> ls = LineString((i, 0) for i in range(6))
>>> ls
<LINESTRING (0 0, 1 0, 2 0, 3 0, 4 0, 50)>
>>> substring(ls, start_dist=1, end_dist=3)
<LINESTRING (1 0, 2 0, 3 0)>
>>> substring(ls, start_dist=3, end_dist=1)
<LINESTRING (3 0, 2 0, 1 0)>
>>> substring(ls, start_dist=1, end_dist=-3)
<LINESTRING (1 0, 2 0)>
>>> substring(ls, start_dist=0.2, end_dist=-0.6, normalized=True)
<LINESTRING (1 0, 2 0)>
```

And here is an example that returns a Point.

```
>>> substring(ls, start_dist=2.5, end_dist=-2.5)
<POINT (2.5 0)>
```


## Prepared Geometry Operations

Shapely geometries can be processed into a state that supports more efficient batches of operations.

```
prepared.prep(ob)
```

Creates and returns a prepared geometric object.
To test one polygon containment against a large batch of points, one should first use the prepared.prep() function.

```
>>> from shapely.prepared import prep
>>> points = [...] # large list of points
>>> polygon = Point(0.0, 0.0).buffer(1.0)
>>> prepared_polygon = prep(polygon)
>>> prepared_polygon
<shapely.prepared.PreparedGeometry object at 0x...>
>>> hits = filter(prepared_polygon.contains, points)
```

Prepared geometries instances have the following methods: contains, contains_properly, covers, and intersects. All have exactly the same arguments and usage as their counterparts in non-prepared geometric objects.

## Diagnostics

validation.explain_validity(ob):
Returns a string explaining the validity or invalidity of the object.
New in version 1.2.1.
The messages may or may not have a representation of a problem point that can be parsed out.

```
>> coords = [(0, 0), (0, 2), (1, 1), (2, 2), (2, 0), (1, 1), (0, 0)]
>>> p = Polygon(coords)
>>> from shapely.validation import explain_validity
>>> explain_validity(p)
'Ring Self-intersection[1 1]'
```

```
validation.make_valid(ob)
```

Returns a valid representation of the geometry, if it is invalid. If it is valid, the input geometry will be returned.
In many cases, in order to create a valid geometry, the input geometry must be split into multiple parts or multiple geometries. If the geometry must be split into multiple parts of the same geometry type, then a multi-part geometry (e.g. a MultiPolygon) will be returned. if the geometry must be split into multiple parts of different types, then a GeometryCollection will be returned.

For example, this operation on a geometry with a bow-tie structure:

```
>>> from shapely.validation import make_valid
>>> coords = [(0, 0), (0, 2), (1, 1), (2, 2), (2, 0), (1, 1), (0, 0)]
>>> p = Polygon(coords)
>>> make_valid(p)
<MULTIPOLYGON (((1 1, 0 0, 0 2, 1 1)), ((2 0, 1 1, 2 2, 2 0)))>
Yields a MultiPolygon with two parts:
```

```
>>> from shapely.validation import make_valid
>> coords = [(0, 2), (0, 1), (2, 0), (0, 0), (0, 2)]
>>> p = Polygon(coords)
>>> make_valid(p)
<GEOMETRYCOLLECTION (POLYGON ((2 0, 0 0, 0 1, 2 0)), LINESTRING (0 2, 0 1))>
Yields a GeometryCollection with a Polygon and a LineString:
```

The Shapely version, GEOS library version, and GEOS C API version are accessible via shapely.__version__, shapely.geos_version_string, and shapely.geos_capi_version.

```
>>> import shapely
>>> shapely.__version__
'2.0.0'
>>> shapely.geos_version
(3, 10, 2)
>>> shapely.geos_capi_version_string
'3.10.2-CAPI-1.16.0'
```



Fig. 1: While this operation:


Fig. 2: New in version 1.8 Requires GEOS $>3.8$

## Polylabel

shapely.ops.polylabel (polygon, tolerance)
Finds the approximate location of the pole of inaccessibility for a given polygon. Based on Vladimir Agafonkin's polylabel.
New in version 1.6.0

Note: Prior to 1.7 polylabel must be imported from shapely.algorithms.polylabel instead of shapely.ops.

```
>>> from shapely.ops import polylabel
>>> polygon = LineString([(0, 0), (50, 200), (100, 100), (20, 50),
... (-100, -20), (-150, -200)]).buffer(100)
>>> label = polylabel(polygon, tolerance=10)
>>> label
<POINT (59.356 121.839)>
```


### 5.2.8 STR-packed R-tree

Shapely provides an interface to the query-only GEOS R-tree packed using the Sort-Tile-Recursive algorithm. Pass a list of geometry objects to the STRtree constructor to create a spatial index that you can query with another geometric object. Query-only means that once created, the STRtree is immutable. You cannot add or remove geometries.

## class strtree.STRtree(geometries)

The STRtree constructor takes a sequence of geometric objects.
References to these geometric objects are kept and stored in the R-tree.
New in version 1.4.0.
strtree. query (geom)
Returns the integer indices of all geometries in the strtree whose extents intersect the extent of geom. This means that a subsequent search through the returned subset using the desired binary predicate (eg. intersects, crosses, contains, overlaps) may be necessary to further filter the results according to their specific spatial relationships.

```
>>> from shapely import STRtree
>>> points = [Point(i, i) for i in range(10)]
>>> tree = STRtree(points)
>>> query_geom = Point (2,2).buffer(0.99)
>>> [points[idx].wkt for idx in tree.query(query_geom)]
['POINT (2 2)']
>>> query_geom = Point(2, 2).buffer(1.0)
>>> [points[idx].wkt for idx in tree.query(query_geom)]
['POINT (1 1)', 'POINT (2 2)', 'POINT (3 3)']
>>> [points[idx].wkt for idx in tree.query(query_geom, predicate="intersects")]
['POINT (2 2)']
```

strtree. nearest (geom)

Returns the nearest geometry in strtree to geom.

```
>>> points = [Point(i, i) for i in range(10)]
>>> tree = STRtree(points)
>>> idx = tree.nearest(Point(2.2, 2.2))
>>> points[idx]
<POINT (2 2)>
```


### 5.2.9 Interoperation

Shapely provides 4 avenues for interoperation with other software.

## Well-Known Formats

A Well Known Text (WKT) or Well Known Binary (WKB) representation? of any geometric object can be had via its wkt or wkb attribute. These representations allow interchange with many GIS programs. PostGIS, for example, trades in hex-encoded WKB.

```
>>> Point(0, 0).wkt
'POINT (0 0)'
>>> Point(0, 0).wkb
b'\x01\x01\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00'
>>> Point(0, 0).wkb_hex
'0101000000000000000000000000000000000000000'
```

The shapely.wkt and shapely.wkb modules provide dumps() and loads() functions that work almost exactly as their pickle and simplejson module counterparts. To serialize a geometric object to a binary or text string, use dumps (). To deserialize a string and get a new geometric object of the appropriate type, use loads().

The default settings for the wkt attribute and shapely.wkt.dumps() function are different. By default, the attribute's value is trimmed of excess decimals, while this is not the case for dumps(), though it can be replicated by setting trim=True.

```
shapely.wkb.dumps(ob)
```

Returns a WKB representation of $o b$.

```
shapely.wkb.loads(wkb)
```

Returns a geometric object from a WKB representation $w k b$.

```
>>> from shapely import wkb
>>> pt = Point(0, 0)
>>> wkb.dumps(pt)
b'\x01\x01\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00'
>>> pt.wkb
b'\x01\x01\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\ x00\x00\x00\x00\x00\x00'
>>> wkb.loads(pt.wkb).wkt
'POINT (Q Q)'
```

All of Shapely's geometry types are supported by these functions.
shapely.wkt.dumps (ob)
Returns a WKT representation of $o b$. Several keyword arguments are available to alter the WKT which is returned; see the docstrings for more details.

```
shapely.wkt.loads(wkt)
```

Returns a geometric object from a WKT representation wkt.

```
>>> from shapely import wkt
>>> pt = Point(0, 0)
>>> thewkt = wkt.dumps(pt)
>>> thewkt
'POINT (0.00000000000000000 0.0000000000000000)'
>>> pt.wkt
'POINT (0 0)'
>>> wkt.dumps(pt, trim=True)
'POINT (0 Q)'
```


## Numpy and Python Arrays

All geometric objects with coordinate sequences (Point, LinearRing, LineString) provide the Numpy array interface and can thereby be converted or adapted to Numpy arrays.

```
>>> import numpy as np
>>> np.asarray(Point(0, 0).coords)
array([[0., 0.]])
>>> np.asarray(LineString([(0, 0), (1, 1)]).coords)
array([[0., 0.],
    [1., 1.]])
```

The coordinates of the same types of geometric objects can be had as standard Python arrays of $x$ and $y$ values via the xy attribute.

```
>>> Point(0, 0).xy
(array('d', [0.0]), array('d', [0.0]))
>>> LineString([(0, 0), (1, 1)]).xy
(array('d', [0.0, 1.0]), array('d', [0.0, 1.0]))
```


## Python Geo Interface

Any object that provides the GeoJSON-like Python geo interface can be converted to a Shapely geometry using the shapely.geometry.shape() function.
shapely.geometry.shape (context)
Returns a new, independent geometry with coordinates copied from the context.
For example, a dictionary:

```
>>> from shapely.geometry import shape
>>> data = {"type": "Point", "coordinates": (0.0, 0.0)}
>>> geom = shape(data)
>>> geom.geom_type
'Point'
>>> list(geom.coords)
[(0.0, 0.0)]
```

Or a simple placemark-type object:

```
>>> class GeoThing:
... def __init__(self, d):
```

```
#." self.__geo_interface__ = d
>>> thing = GeoThing({"type": "Point", "coordinates": (0.0, 0.0)})
>> geom = shape(thing)
>>> geom.geom_type
'Point'
>>> list(geom.coords)
[(0.0, 0.0)]
```

The GeoJSON-like mapping of a geometric object can be obtained using shapely.geometry.mapping().

```
shapely.geometry.mapping(ob)
```

Returns a GeoJSON-like mapping from a Geometry or any object which implements $\qquad$
New in version 1.2.3.
For example, using the same GeoThing class:

```
>>> from shapely.geometry import mapping
>>> thing = GeoThing({"type": "Point", "coordinates": (0.0, 0.0)})
>>> m = mapping(thing)
>>> m['type']
'Point'
>>> m['coordinates']
(0.0, 0.0)
```


### 5.2.10 Performance

Shapely uses the GEOS library for all operations. GEOS is written in C++ and used in many applications and you can expect that all operations are highly optimized. The creation of new geometries with many coordinates, however, involves some overhead that might slow down your code.

### 5.2.11 Conclusion

We hope that you will enjoy and profit from using Shapely. This manual will be updated and improved regularly. Its source is available at https://github.com/shapely/shapely/tree/main/docs/.

### 5.2.12 References

### 5.3 Migrating to Shapely 1.8 / 2.0

Shapely 1.8 .0 is a transitional version introducing several warnings in preparation of the upcoming changes in 2.0.0.
Shapely 2.0 .0 will be a major release with a refactor of the internals with considerable performance improvements (based on the developments in the PyGEOS package), along with several breaking changes.
This guide gives an overview of the most important changes with details on what will change in 2.0 .0 , how we warn for this in 1.8.0, and how you can update your code to be future-proof.

For more background, see RFC 1: Roadmap for Shapely 2.0.

### 5.3.1 Geometry objects will become immutable

Geometry objects will become immutable in version 2.0.0.
In Shapely 1.x, some of the geometry classes are mutable, meaning that you can change their coordinates in-place. Illustrative code:

```
>>> from shapely.geometry import LineString
>>> line = LineString([(0,0), (2, 2)])
>>> print(line)
LINESTRING (0 0, 2 2)
>> line.coords = [(0, 0), (10, 0), (10, 10)]
>>> print(line)
LINESTRING (0 0, 10 0, 10 10)
```

In Shapely 1.8, this will start raising a warning:

```
>>> line.coords = [(0, 0), (10, 0), (10, 10)]
ShapelyDeprecationWarning: Setting the 'coords' to mutate a Geometry
in place is deprecated, and will not be possible any more in Shapely 2.0
```

and starting with version 2.0.0, all geometry objects will become immutable. As a consequence, they will also become hashable and therefore usable as, for example, dictionary keys.

How do I update my code? There is no direct alternative for mutating the coordinates of an existing geometry, except for creating a new geometry object with the new coordinates.

## Setting custom attributes

Another consequence of the geometry objects becoming immutable is that assigning custom attributes, which currently works, will no longer be possible.

Currently you can do:

```
>>> line.name = "my_geometry"
>>> line.name
'my_geometry'
```

In Shapely 1.8, this will start raising a warning, and will raise an AttributeError in Shapely 2.0.
How do I update my code? There is no direct alternative for adding custom attributes to geometry objects. You can use other Python data structures such as (GeoJSON-like) dictionaries or GeoPandas' GeoDataFrames to store attributes alongside geometry features.

### 5.3.2 Multi-part geometries will no longer be "sequences" (length, iterable, indexable)

In Shapely 1.x, multi-part geometries (MultiPoint, MultiLineString, MultiPolygon and GeometryCollection) implement a part of the "sequence" python interface (making them list-like). This means you can iterate through the object to get the parts, index into the object to get a specific part, and ask for the number of parts with the len() method.

Some examples of this with Shapely 1.x:

```
>>> from shapely.geometry import Point, MultiPoint
>>> mp = MultiPoint([(1, 1), (2, 2), (3, 3)])
>>> print(mp)
MULTIPOINT (1 1, 2 2, 3 3)
>>> for part in mp:
... print(part)
POINT (1 1)
POINT (2 2)
POINT (3 3)
>>> print(mp[1])
POINT (2 2)
>>> len(mp)
3
>>> list(mp)
[<shapely.geometry.point.Point at 0x7f2e0912bf10>,
<shapely.geometry.point.Point at 0x7f2e09fed820>,
<shapely.geometry.point.Point at 0x7f2e09fed4c0>]
```

Starting with Shapely 1.8 , all the examples above will start raising a deprecation warning. For example:

```
>>> for part in mp:
#.. print(part)
ShapelyDeprecationWarning: Iteration over multi-part geometries is deprecated
and will be removed in Shapely 2.0. Use the `geoms` property to access the
constituent parts of a multi-part geometry.
POINT (1 1)
POINT (2 2)
POINT (3 3)
```

In Shapely 2.0, all those examples will raise an error.
How do I update my code? To access the geometry parts of a multi-part geometry, you can use the .geoms attribute, as the warning indicates.

The examples above can be updated to:

```
>>> for part in mp.geoms:
... print(part)
POINT (1 1)
POINT (2 2)
POINT (3 3)
>>> print(mp.geoms[1])
POINT (2 2)
>>> len(mp.geoms)
3
>>> list(mp.geoms)
[<shapely.geometry.point.Point at 0x7f2e0912bf10>,
<shapely.geometry.point.Point at 0x7f2e09fed820>,
<shapely.geometry.point.Point at 0x7f2e09fed4c0>]
```

The single-part geometries (Point, LineString, Polygon) already didn't support those features, and for those classes there is no change in behaviour for this aspect.

### 5.3.3 Interoperability with NumPy and the array interface

## Conversion of the coordinates to (NumPy) arrays

Shapely provides an array interface to have easy access to the coordinates as, for example, NumPy arrays (manual section).

A small example:

```
>>> line = LineString([(0, 0), (1, 1), (2, 2)])
>>> import numpy as np
>>> np.asarray(line)
array([[0., 0.],
    [1., 1.],
    [2., 2.]])
```

In addition, there are also the explicit array_interface() method and ctypes attribute to get access to the coordinates as array data:

```
>>> line.ctypes
<shapely.geometry.linestring.c_double_Array_6 at 0x7f75261eb740>
>>> line.array_interface()
{'version': 3,
    'typestr': '<f8',
    'data': <shapely.geometry.linestring.c_double_Array_6 at 0x7f752664ae40>,
    'shape': (3, 2)}
```

This functionality is available for Point, LineString, LinearRing and MultiPoint.
For more robust interoperability with NumPy, this array interface will be removed from those geometry classes, and limited to the coords.

Starting with Shapely 1.8, converting a geometry object to a NumPy array directly will start raising a warning:

```
>>> np.asarray(line)
ShapelyDeprecationWarning: The array interface is deprecated and will no longer
work in Shapely 2.0. Convert the '.coords' to a NumPy array instead.
array([[0., 0.],
    [1., 1.],
    [2., 2.]])
```

How do I update my code? To convert a geometry to a NumPy array, you can convert the . coords attribute instead:

```
>>> line.coords
<shapely.coords.CoordinateSequence at 0x7f2e09e88d60>
>>> np.array(line.coords)
array([[0., 0.],
    [1., 1.],
    [2., 2.]])
```

The array_interface() method and ctypes attribute will be removed in Shapely 2.0, but since Shapely will start requiring NumPy as a dependency, you can use NumPy or its array interface directly. Check the NumPy docs on the ctypes attribute or the array interface for more details.

## Creating NumPy arrays of geometry objects

Shapely geometry objects can be stored in NumPy arrays using the object dtype. In general, one could create such an array from a list of geometries as follows:

```
>>> from shapely.geometry import Point
>>> arr = np.array([Point(0, 0), Point(1, 1), Point(2, 2)])
>>> arr
array([<shapely.geometry.point.Point object at 0x7fb798407cd0>,
    <shapely.geometry.point.Point object at 0x7fb7982831c0>,
    <shapely.geometry.point.Point object at 0x7fb798283b80>],
    dtype=object)
```

The above works for point geometries, but because in Shapely 1.x, some geometry types are sequence-like (see above), NumPy can try to "unpack" them when creating an array. Therefore, for more robust creation of a NumPy array from a list of geometries, it's generally recommended to this in a two-step way (first creating an empty array and then filling it):

```
geoms = [Point(0, 0), Point(1, 1), Point(2, 2)]
arr = np.empty(len(geoms), dtype="object")
arr[:] = geoms
```

This code snippet results in the same array as the example above, and works for all geometry types and Shapely/NumPy versions.

However, starting with Shapely 1.8, the above code will show deprecation warnings that cannot be avoided (depending on the geometry type, NumPy tries to access the array interface of the objects or check if an object is iterable or has a length, and those operations are all deprecated now. The end result is still correct, but the warnings appear nonetheless). Specifically in this case, it is fine to ignore those warnings (and the only way to make them go away):

```
import warnings
from shapely.errors import ShapelyDeprecationWarning
geoms = [Point(0, 0), Point(1, 1), Point(2, 2)]
arr = np.empty(len(geoms), dtype="object")
with warnings.catch_warnings():
    warnings.filterwarnings("ignore", category=ShapelyDeprecationWarning)
    arr[:] = geoms
```

In Shapely 2.0, the geometry objects will no longer be sequence like and those deprecation warnings will be removed (and thus the filterwarnings will no longer be necessary), and creation of NumPy arrays will generally be more robust.

If you maintain code that depends on Shapely, and you want to have it work with multiple versions of Shapely, the above code snippet provides a context manager that can be copied into your project:

```
import contextlib
import shapely
import warnings
from packaging import version # https://packaging.pypa.io/
SHAPELY_GE_20 = version.parse(shapely.__version__) >= version.parse("2.0a1")
try:
```

```
    from shapely.errors import ShapelyDeprecationWarning as shapely_warning
except ImportError:
    shapely_warning = None
if shapely_warning is not None and not SHAPELY_GE_20:
    @contextlib.contextmanager
    def ignore_shapely2_warnings():
        with warnings.catch_warnings():
            warnings.filterwarnings("ignore", category=shapely_warning)
            yield
else:
    @contextlib.contextmanager
    def ignore_shapely2_warnings():
        yield
```

This can then be used when creating NumPy arrays (be careful to only use it for this specific purpose, and not generally suppress those warnings):

```
geoms = [...]
arr = np.empty(len(geoms), dtype="object")
with ignore_shapely2_warnings():
    arr[:] = geoms
```


### 5.3.4 Consistent creation of empty geometries

Shapely 1.x is inconsistent in creating empty geometries between various creation methods. A small example for an empty Polygon geometry:

```
# Using an empty constructor results in a GeometryCollection
>>> from shapely.geometry import Polygon
>>> g1 = Polygon()
>>> type(g1)
<class 'shapely.geometry.polygon.Polygon'>
>>> g1.wkt
GEOMETRYCOLLECTION EMPTY
# Converting from WKT gives a correct empty polygon
>>> from shapely import wkt
>>> g2 = wkt.loads("POLYGON EMPTY")
>>> type(g2)
<class 'shapely.geometry.polygon.Polygon'>
>>> g2.wkt
POLYGON EMPTY
```

Shapely 1.8 does not yet change this inconsistent behaviour, but starting with Shapely 2.0 , the different methods will always consistently give an empty geometry object of the correct type, instead of using an empty GeometryCollection as "generic" empty geometry object.

How do I update my code? Those cases that will change don't raise a warning, but you will need to update your code if you rely on the fact that empty geometry objects are of the GeometryCollection type. Use the .is_empty attribute for robustly checking if a geometry object is an empty geometry.

In addition, the WKB serialization methods will start supporting empty Points (using "POINT (NaN NaN)" to represent an empty point).

### 5.3.5 Other deprecated functionality

There are some other various functions and methods deprecated in Shapely 1.8 as well:

- The adapters to create geometry-like proxy objects with coordinates stored outside Shapely geometries are deprecated and will be removed in Shapely 2.0 (e.g. created using asShape ()). They have little to no benefit compared to the normal geometry classes, as thus you can convert to your data to a normal geometry object instead. Use the shape () function instead to convert a GeoJSON-like dict to a Shapely geometry.
- The empty () method on a geometry object is deprecated.
- The shapely.ops.cascaded_union function is deprecated. Use shapely.ops.unary_union instead, which internally already uses a cascaded union operation for better performance.


### 5.4 Migrating from PyGEOS

The PyGEOS package was merged with Shapely in December 2021 and will be released as part of Shapely 2.0. No further development will take place for the PyGEOS package (except for providing up to date packages until Shapely 2.0 is released).

Therefore, everybody using PyGEOS is highly recommended to migrate to Shapely 2.0.
Generally speaking, this should be a smooth experience because all functionality of PyGEOS was added to Shapely. All vectorized functions availabe in pygeos have been added to the top-level shapely module, with only minor differences (see below). Migrating from PyGEOS to Shapely 2.0 can thus be done by replacing the pygeos import and module calls:

```
import pygeos
polygon = pygeos.box(0, 0, 2, 2)
points = pygeos.points(...)
pygeos.contains(polygon, points)
```

Using Shapely 2.0, this can now be written as:

```
import shapely
polygon = shapely.box(0, 0, 2, 2)
points = shapely.points(...)
shapely.contains(polygon, points)
```

In addition, you now also have the scalar interface of Shapely which wasn't implemented in PyGEOS.

### 5.4.1 Differences between PyGEOS and Shapely 2.0

## STRtree API changes

Functionality-wise, everything from pygeos.STRtree is available in Shapely 2.0. But while merging into Shapely, some methods have been changed or merged:

- The query () and query_bulk() methods have been merged into a single query() method. The query() method now accepts an array of geometries as well in addition to a single geometry, and in that case it will return 2D array of indices.
It should thus be a matter of replacing query_bulk with query in your code.
See STRtree.query () for more details.
- The nearest () method was changed to return an array of the same shape as the input geometries. Thus, for a scalar geometry it now returns a single integer index (instead of a $(2,1)$ array), and for an array of geometries it now returns a 1D array of indices $((n$,$) array instead of a (2, n)$ array $)$.
See STRtree.nearest () for more details.
- The nearest_all() method has been replaced with query_nearest (). For an array of geometries, the output is the same, but when passing a scalar geometry as input, the method now returns a 1D array instead of a 2D array (consistent with query ()).
In addition, this method gained the new exclusive and all_matches keywords (with defaults preserving existing behaviour from PyGEOS). See STRtree.query_nearest () for more details.


## Other differences

- The pygeos. Geometry (. .) constructor has not been retained in Shapely (the class exists as base class, but the constructor is not callable). Use one of the subclasses, or shapely. from_wkt (. .), instead.
- The apply() function was renamed to transform().
- The tolerance keyword of the segmentize() function was renamed to max_segment_length.
- The quadsegs keyword of the buffer() and offset_curve() functions was renamed to quad_segs.
- The preserve_topology keyword of simplify() now defaults to True instead of False.
- The behaviour of union_all() / intersection_all() / symmetric_difference_all was changed to return an empty GeometryCollection for an empty or all-None sequence as input (instead of returning None).
- The radius keyword of the buffer() funtion was renamed to distance.


### 5.5 Release notes

### 5.5.1 Version 2.x

Version 2.0.1 (2023-01-30)
Bug fixes:

- Fix regression in the Polygon() constructor taking a sequence of Points (\#1662).
- Fix regression in the geometry constructors when passing decimal. Decimal coordinate values (\#1707).
- Fix STRtree() to not make the passed geometry array immutable as side-effect of the constructor (\#1714).
- Fix the directed keyword in shapely.ops.linemerge() (\#1695).

Improvements:

- Expose the function to get a matplotlib Patch object from a (Multi)Polygon (without already plotting it) publicly as shapely.plotting.patch_from_polygon() (\#1704).


## Acknowledgments

Thanks to everyone who contributed to this release! People with a " + " by their names contributed a patch for the first time.

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## Version 2.0.0 (2022-12-12)

Shapely 2.0 version is a major release featuring a complete refactor of the internals and new vectorized (elementwise) array operations, providing considerable performance improvements (based on the developments in the PyGEOS package), along with several breaking API changes and many feature improvements.
For more background, see RFC 1: Roadmap for Shapely 2.0.

## Refactor of the internals

Shapely wraps the GEOS C++ library for use in Python. Before 2.0, Shapely used ctypes to link to GEOS at runtime, but doing so resulted in extra overhead and installation challenges. With 2.0 , the internals of Shapely have been refactored to expose GEOS functionality through a Python C extension module that is compiled in advance.

The pointer to the actual GEOS Geometry object is stored in a lightweight Python extension type. A single Geometry Python extension type is defined in C wrapping a GEOSGeometry pointer. This extension type is further subclassed in Python to provide the geometry type-specific classes from Shapely (Point, LineString, Polygon, etc). The GEOS pointer is accessible from C as a static attribute of the Python object (an attribute of the C struct that makes up a Python object), which enables using vectorized functions within C and thus avoiding Python overhead while looping over an array of geometries (see next section).

## Vectorized (element-wise) geometry operations

Before the 2.0 release, Shapely only provided an interface for scalar (individual) geometry objects. Users had to loop over individual geometries within an array of geometries and call scalar methods or properties, which is both more verbose to use and has a large performance overhead.

Shapely 2.0 exposes GEOS operations as vectorized functions that operate on arrays of geometries using a familiar NumPy interface. Those functions are implemented as NumPy *universal functions* (or ufunc for short). A universal function is a function that operates on $n$-dimensional arrays in an element-by-element fashion and supports array broadcasting. All loops over geometries are implemented in C, which results in substantial performance improvements when performing operations using many geometries. This also allows operations to be less verbose.
NumPy is now a required dependency.
An example of this functionality using a small array of points and a single polygon:

```
>>> import shapely
>>> from shapely import Point, box
>>> import numpy as np
>> geoms = np.array([Point(0, 0), Point(1, 1), Point(2, 2)])
>> polygon = box(0, 0, 2, 2)
```

Before Shapely 2.0, a for loop was required to operate over an array of geometries:

```
>>> [polygon.contains(point) for point in geoms]
[False, True, False]
```

In Shapely 2.0, we can now compute whether the points are contained in the polygon directly with one function call:

```
>>> shapely.contains(polygon, geoms)
array([False, True, False])
```

This results in a considerable speedup, especially for larger arrays of geometries, as well as a nicer user interface that avoids the need to write for loops. Depending on the operation, this can give a performance increase with factors of 4 x to 100 x . In general, the greatest speedups are for lightweight GEOS operations, such as contains, which would previously have been dominated by the high overhead of for loops in Python. See https://caspervdw.github.io/ Introducing-Pygeos/ for more detailed examples.

The new vectorized functions are available in the top-level shapely namespace. All the familiar geospatial methods and attributes from the geometry classes now have an equivalent as top-level function (with some small name deviations, such as the .wkt attribute being available as a to_wkt () function). Some methods from submodules (for example, several functions from the shapely. ops submodule such as polygonize()) are also made available in a vectorized version as top-level function.

A full list of functions can be found in the API docs (see the pages listed under "API REFERENCE" in the left sidebar).

- Vectorized constructor functions
- Optionally output to a user-specified array (out keyword argument) when constructing geometries from indices.
- Enable bulk construction of geometries with different number of coordinates by optionally taking index arrays in all creation functions.


## Shapely 2.0 API changes (deprecated in 1.8)

The Shapely 1.8 release included several deprecation warnings about API changes that would happen in Shapely 2.0 and that can be fixed in your code (making it compatible with both $<=1.8$ and $>=2.0$ ). See Migrating to Shapely 1.8 / 2.0 for more details on how to update your code.

It is highly recommended to first upgrade to Shapely 1.8 and resolve all deprecation warnings before upgrading to Shapely 2.0.

Summary of changes:

- Geometries are now immutable and hashable.
- Multi-part geometries such as MultiPolygon no longer behave as "sequences". This means that they no longer have a length, are not iterable, and are not indexable anymore. Use the .geoms attribute instead to access individual parts of a multi-part geometry.
- Geometry objects no longer directly implement the numpy array interface to expose their coordinates. To convert to an array of coordinates, use the . coords attribute instead (np.asarray (geom. coords)).
- The following attributes and methods on the Geometry classes were previously deprecated and are now removed from Shapely 2.0:
- array_interface() and ctypes
- asShape(), and the adapters classes to create geometry-like proxy objects (use shape() instead).
- empty() method

Some new deprecations have been introduced in Shapely 2.0:

- Directly calling the base class BaseGeometry () constructor or the EmptyGeometry () constructor is deprecated and will raise an error in the future. To create an empty geometry, use one of the subclasses instead, for example GeometryCollection() (\#1022).
- The shapely. speedups module (the enable and disable functions) is deprecated and will be removed in the future. The module no longer has any affect in Shapely $>=2.0$.


## Breaking API changes

Some additional backwards incompatible API changes were included in Shapely 2.0 that were not deprecated in Shapely 1.8:

- Consistent creation of empty geometries (for example Polygon() now actually creates an empty Polygon instead of an empty geometry collection).
- The . bounds attribute of an empty geometry now returns a tuple of NaNs instead of an empty tuple (\#1023).
- The preserve_topology keyword of simplify() now defaults to True (\#1392).
- A GeometryCollection that consists of all empty sub-geometries now returns those empty geometries from its . geoms attribute instead of returning an empty list (\#1420).
- The Point (. . ) constructor no longer accepts a sequence of coordinates consisting of more than one coordinate pair (previously, subsequent coordinates were ignored) (\#1600).
- The unused shape_factory () method and HeterogeneousGeometrySequence class are removed (\#1421).
- The undocumented __geom__ attribute has been removed. If necessary (although not recommended for use beyond experimentation), use the _geom attribute to access the raw GEOS pointer (\#1417).
- The logging functionality has been removed. All error messages from GEOS are now raised as Python exceptions (\#998).
- Several custom exception classes defined in shapely. errors that are no longer used internally have been removed. Errors from GEOS are now raised as GEOSException (\#1306).

The STRtree interface has been substantially changed. See the section below for more details.
Additionally, starting with GEOS 3.11 (which is included in the binary wheels on PyPI), the behaviour of the parallel_offset (offset_curve) method changed regarding the orientation of the resulting line. With GEOS < 3.11, the line retains the same direction for a left offset (positive distance) or has opposite direction for a right offset (negative distance), and this behaviour was documented as such in previous Shapely versions. Starting with GEOS 3.11, the function tries to preserve the orientation of the original line.

## New features

## Geometry subclasses are now available in the top-level namespace

Following the new vectorized functions in the top-level shapely namespace, the Geometry subclasses (Point, LineString, Polygon, etc) are now available in the top-level namespace as well. Thus it is no longer needed to import those from the shapely.geometry submodule.

The following:

```
from shapely.geometry import Point
```

can be replaced with:

```
from shapely import Point
```

or:

```
import shapely
shapely.Point(...)
```

Note: for backwards compatibility (and being able to write code that works for both $<=1.8$ and $>2.0$ ), those classes still remain accessible from the shapely.geometry submodule as well.

## More informative repr with truncated WKT

The repr (__repr__) of Geometry objects has been simplified and improved to include a descriptive Well-Known-Text (WKT) formatting. Instead of showing the class name and id:

```
>>> Point(0, 0)
<shapely.geometry.point.Point at 0x7f0b711f1310>
```

we now get:

```
>>> Point(0, 0)
<POINT (O O)>
```

For large geometries with many coordinates, the output gets truncated to 80 characters.

## Support for fixed precision model for geometries and in overlay functions

GEOS 3.9.0 overhauled the overlay operations (union, intersection, (symmetric) difference). A complete rewrite, dubbed "OverlayNG", provides a more robust implementation (no more TopologyExceptions even on valid input), the ability to specify the output precision model, and significant performance optimizations. When installing Shapely with GEOS $>=3.9$ (which is the case for PyPI wheels and conda-forge packages), you automatically get these improvements (also for previous versions of Shapely) when using the overlay operations.

Shapely 2.0 also includes the ability to specify the precision model directly:

- The set_precision() function can be used to conform a geometry to a certain grid size (may round and reduce coordinates), and this will then also be used by subsequent overlay methods. A get_precision() function is also available to inspect the precision model of geometries.
- The grid_size keyword in the overlay methods can also be used to specify the precision model of the output geometry (without first conforming the input geometries).


## Releasing the GIL for multithreaded applications

Shapely itself is not multithreaded, but its functions generally allow for multithreading by releasing the Global Interpreter Lock (GIL) during execution. Normally in Python, the GIL prevents multiple threads from computing at the same time. Shapely functions internally release this constraint so that the heavy lifting done by GEOS can be done in parallel, from a single Python process.

## STRtree API changes and improvements

The biggest change in the STRtree interface is that all operations now return indices of the input tree or query geometries, instead of the geometries itself. These indices can be used to index into anything associated with the input geometries, including the input geometries themselves, or custom items stored in another object of the same length and order as the geometries.

In addition, Shapely 2.0 includes several improvements to STRtree:

- Directly include predicate evaluation in STRtree. query () by specifying the predicate keyword. If a predicate is provided, tree geometries with bounding boxes that overlap the bounding boxes of the input geometries are further filtered to those that meet the predicate (using prepared geometries under the hood for efficiency).
- Query multiple input geometries (spatial join style) with STRtree .query () by passing an array of geometries. In this case, the return value is a 2D array with shape $(2, n)$ where the subarrays correspond to the indices of the input geometries and indices of the tree geometries associated with each.
- A new STRtree.query_nearest () method was added, returning the index of the nearest geometries in the tree for each input geometry. Compared to STRtree. nearest (), which only returns the index of a single nearest geometry for each input geometry, this new methods allows for:
- returning all equidistant nearest geometries,
- excluding nearest geometries that are equal to the input,
- specifying an max_distance to limit the search radius, potentially increasing the performance,
- optionally returning the distance.
- Fixed STRtree creation to allow querying the tree in a multi-threaded context.


## Bindings for new GEOS functionalities

Several (new) functions from GEOS are now exposed in Shapely:

- hausdorff_distance() and frechet_distance()
- contains_properly()
- extract_unique_points()
- reverse()
- node()
- contains_xy() and intersects_xy()
- build_area() (GEOS >= 3.8)
- minimum_bounding_circle() and minimum_bounding_radius() (GEOS >=3.8)
- coverage_union() and coverage_union_all() (GEOS >=3.8)
- segmentize() (GEOS >= 3.10)
- dwithin() (GEOS >= 3.10)
- remove_repeated_points() (GEOS >= 3.11)
- line_merge() added directed parameter (GEOS > 3.11)
- concave_hull() (GEOS >=3.11)

In addition some aliases for existing methods have been added to provide a method name consistent with GEOS or PostGIS:

- line_interpolate_point() (interpolate)
- line_locate_point() (project)
- offset_curve() (parallel_offset)
- point_on_surface() (representative_point)
- oriented_envelope() (minimum_rotated_rectangle)
- delaunay_triangles() (ops.triangulate)
- voronoi_polygons() (ops.voronoi_diagram)
- shortest_line() (ops.nearest_points)
- is_valid_reason() (validation.explain_validity)


## Getting information / parts / coordinates from geometries

A set of GEOS getter functions are now also exposed to inspect geometries:

- get_dimensions()
- get_coordinate_dimension()
- get_srid()
- get_num_points()
- get_num_interior_rings()
- get_num_geometries()
- get_num_coordinates()
- get_precision()

Several functions are added to extract parts:

- get_geometry() to get a geometry from a GeometryCollection or Multi-part geometry.
- get_exterior_ring() and get_interior_ring() to get one of the rings of a Polygon.
- get_point () to get a point (vertex) of a linestring or linearring.
- get_x (), get_y() and get_z() to get the $x / y / z$ coordinate of a Point.

Methods to extract all parts or coordinates at once have been added:

- The get_parts() function can be used to get individual parts of an array of multi-part geometries.
- The get_rings () function, similar as get_parts but specifically to extract the rings of Polygon geometries.
- The get_coordinates() function to get all coordinates from a geometry or array of goemetries as an array of floats.

Each of those three functions has an optional return_index keyword, which allows to also return the indexes of the original geometries in the source array.

## Prepared geometries

Prepared geometries are now no longer separate objects, but geometry objects themselves can be prepared (this makes the shapely.prepared module superfluous).
The prepare() function generates a GEOS prepared geometry which is stored on the Geometry object itself. All binary predicates (except equals) will make use of this if the input geometry has already been prepared. Helper functions destroy_prepared() and is_prepared() are also available.

## New IO methods (GeoJSON, ragged arrays)

- Added GeoJSON input/output capabilities from_geojson() and to_geojson() for GEOS >=3.10.
- Added conversion to/from ragged array representation using a contiguous array of coordinates and offset arrays: to_ragged_array() and from_ragged_array().


## Other improvements

- Added force_2d() and force_3d() to change the dimensionality of the coordinates in a geometry.
- Addition of a total_bounds() function to return the outer bounds of an array of geometries.
- Added empty () to create a geometry array pre-filled with None or with empty geometries.
- Performance improvement in constructing LineStrings or LinearRings from numpy arrays for GEOS >=3.10.
- Updated the box() ufunc to use internal C function for creating polygon (about 2 x faster) and added ccw parameter to create polygon in counterclockwise (default) or clockwise direction.
- Start of a benchmarking suite using ASV.
- Added shapely.testing.assert_geometries_equal.


## Bug fixes

- Fixed several corner cases in WKT and WKB serialization for varying GEOS versions, including:
- Fixed the WKT serialization of single part 3D empty geometries to correctly include "Z" (for GEOS >= 3.9.0).
- Handle empty points in WKB serialization by conversion to POINT (nan, nan) consistently for all GEOS versions (GEOS started doing this for $>=3.9 .0$ ).


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### 5.5.2 Version 1.x

1.8.4 (2022-08-17)

Bug fixes:

- The new c_geom_p type caused a regression and has been removed (\#1487).


### 1.8.3 (2022-08-16)

Deprecations:
The STRtree class will be changed in 2.0.0 and will not be compatible with the class in versions 1.8.x. This change obsoletes the deprecation announcement in 1.8 a 3 (below).

Packaging:
Wheels for 1.8.3 published on PyPI include GEOS 3.10.3.
Bug fixes:

- The signature for GEOSMinimumClearance has been corrected, fixing an issue affecting aarch64-darwin (\#1480)
- Return and arg types have been corrected and made more strict for area, length, and distance properties.
- A new c_geom_p type has been created to replace c_void_p when calling GEOS functions (\#1479).
- An incorrect polygon-line intersection (\#1427) has been fixed in GEOS 3.10.3, which will be included in wheels published to PyPI.
- GEOS buffer parameters are now destroyed, fixing a memory leak (\#1440).


### 1.8.2 (2022-05-03)

- Make Polygons and MultiPolygons closed by definition, like LinearRings. Resolves \#1246.
- Perform frozen app check for GEOS before conda env check on macos as we already do on linux (\#1301).
- Fix leak of GEOS coordinate sequence in nearest_points reported in \#1098.


### 1.8.1.post1 (2022-02-17)

This post-release addresses a defect in the 1.8 .1 source distribution. No .c files are included in the 1.8.1.post1 sdist and Cython is required to build and install from source.

### 1.8.1 (2022-02-16)

Packaging:
Wheels for 1.8.1 published on PyPI include GEOS 3.10.2. This version is the best version of GEOS yet. Discrepancies in behavior compared to previous versions are considered to be improvements.
For the first time, we will publish wheels for macos_arm64 (see PR \#1310).
Python version support:
Shapely 1.8.1 works with Pythons 3.6-3.10.
Bug fixes:

- Require Cython >=0.29.24 to support Python 3.10 (\#1224).
- Fix array_interface_base (\#1235).


### 1.8.0 (2021-10-25)

This is the final 1.8.0 release. There have been no changes since 1.8 rc 2 .
1.8rc2 (2021-10-19)

Build:
A pyproject.toml file has been added to specify build dependencies for the _vectorized and _speedups modules (\#1128). To install shapely without these build dependencies, use the features of your build tool that disable PEP 517 and 518 support.

Bug fixes:

- Part of PR \#1042, which added a new primary GEOS library name to be searched for, has been reverted by PR \#1201.


## 1.8rc1 (2021-10-04)

## Deprecations:

The almost_exact() method of BaseGeometry has been deprecated. It is confusing and will be removed in 2.0.0. The equals_exact() method is to be used instead.

Bug fixes:

- We ensure that the _speedups module is always imported before _vectorized to avoid an unexplained condition on Windows with Python 3.8 and 3.9 (\#1184).


## 1.8a3 (2021-08-24)

## Deprecations:

The STRtree class deprecation warnings have been removed. The class in 2.0 .0 will be backwards compatible with the class in 1.8.0.

Bug fixes:

- The __array_interface__raises only AttributeError, all other exceptions are deprecated starting with Numpy 1.21 (\#1173).
- The STRtree class now uses a pair of item, geom sequences internally instead of a dict (\#1177).


## 1.8a2 (2021-07-15)

Python version support:
Shapely 1.8 will support only Python versions $>=3.6$.
New features:

- The STRtree nearest*() methods now take an optional argument that specifies exclusion of the input geometry from results (\#1115).
- A GeometryTypeError has been added to shapely.errors and is consistently raised instead of TypeError or ValueError as in version 1.7. For backwards compatibility, the new exception will derive from TypeError and Value error until version 2.0 (\#1099).
- The STRtree class constructor now takes an optional second argument, a sequence of objects to be stored in the tree. If not provided, the sequence indices of the geometries will be stored, as before (\#1112).
- The STRtree class has new query_geoms(), query_items(), nearest_geom(), and nearest_item() methods (\#1112). The query() and nearest() methods remain as aliases for query_geoms() and nearest_geom().
Bug fixes:
- We no longer attempt to load libc to get the free function on Linux, but get it from the global symbol table.
- GEOS error messages printed when GEOS_getCoordSeq() is passed an empty geometry are avoided by never passing an empty geometry (\#1134).
- Python's builtin super() is now used only as described in PEP 3135 (\#1109).
- Only load conda GEOS dll if it exists (on Windows) (\#1108).
- Add /opt/homebrew/lib to the list of directories to be searched for the GEOS shared library.
- Added new library search path to assist app creation with cx_Freeze.


## 1.8a1 (2021-03-03)

Shapely 1.8 .0 will be a transitional version. There are a few bug fixes and new features, but it is mainly about warning of the upcoming changes in 2.0.0. Several more pre-releases before 1.8 .0 are expected. See the migration guide to Shapely 1.8 / 2.0 for more details on how to update your code (https://shapely.readthedocs.io/en/latest/migration.html).

Python version support:
Shapely 1.8 will support only Python versions $>=3.5$ (\#884).

## Deprecations:

The following functions and geometry attributes and methods will be removed in version 2.0.0.

- ops.cascaded_union
- geometry .empty()
- geometry .ctypes and .__array_interface
- multi-part geometry .__len__
- setting custom attributes on geometry objects

Geometry objects will become immutable in version 2.0.0.
The STRtree class will be entirely changed in 2.0.0. The exact future API is not yet decided, but will be decided before 1.8.0 is released.

Deprecation warnings will be emitted in 1.8 a 1 when any of these features are used.
The deprecated .to_wkb() and .to_wkt() methods on the geometry objects have been removed.
New features:

- Add a normalize() method to geometry classes, exposing the GEOSNormalize algorithm (\#1090).
- Initialize STRtree with a capacity of 10 items per node (\#1070).
- Load libraries relocated to shapely/.libs by auditwheel versions < 3.1 or relocated to Shapely.libs by auditwheel versions >=3.1.
- shapely.ops.voronoi_diagram() computes the Voronoi Diagram of a geometry or geometry collection (\#833, \#851).
- shapely.validation.make_valid() fixes invalid geometries (\#883)

Bug fixes:

- For pyinstaller we now handle the case of more than one GEOS library in the environment, such as when fiona and rasterio wheels are co-installed with shapely (\#1071).
- The ops.split function now splits on touch to eliminate confusing discrepancies between results using multi and single part splitters (\#1034).
- Several issues with duplication and order of vertices in ops.substring have been fixed (\#1008).

Packaging:

- The wheels uploaded to PyPI will include GEOS 3.9.1.


### 1.7.1 (2020-08-20)

- STRtree now safely implements the pickle protocol (\#915).
- Documentation has been added for minimum_clearance (\#875, \#874).
- In STRtree.__del__() we guard against calling GEOSSTRtree_destroy when the lgeos module has already been torn down on exit (\#897, \#830).
- Documentation for the overlaps () method has been corrected (\#920).
- Correct the test in shapely.geometry.base.BaseGeometry.empty() to eliminate memory leaks like the one reported in \#745.
- Get free() not from libc but from the processes global symbols (\#891), fixing a bug that manifests on OS X 10.15 and 10.16.
- Extracting substrings from complex lines has been made more correct (\#848, \#849).
- Splitting of complex geometries has been sped up by preparing the input geometry (\#871).
- Fix bug in concatenation of function argtypes (\#866).
- Improved documentation of STRtree usage (\#857).
- Improved handling for empty list or list of lists in GeoJSON coordinates (\#852).
- The polylabel algorithm now accounts for polygon holes (\#851, \#817).


## 1.7 .0 (2020-01-28)

This is the final 1.7.0 release. There have been no changes since 1.7 b 1 .

## 1.7b1 (2020-01-13)

First beta release.

## 1.7a3 (2019-12-31)

New features:

- The buffer operation can now be single-sides (\#806, \#727).

Bug fixes:

- Add /usr/local/lib to the list of directories to be searched for the GEOS shared library (\#795).
- ops.substring now returns a line with coords in end-to-front order when given a start position that is greater than the end position (\#628).
- Implement __bool__() for geometry base classes so that bool (geom) returns the logical complement of geom. is_empty (\#754).
- Remove assertion on the number of version-like strings found in the GEOS version string. It could be 2 or 3 .


## 1.7 a 2 (2019-06-21)

- Nearest neighbor search has been added to STRtree (\#668).
- Disallow sequences of MultiPolygons as arguments to the MultiPolygon constructor, resolving \#588.
- Removed vendorized functools functions previously used to support Python 2.5.

Bug fixes:

- Avoid reloading the GEOS shared library when using an installed binary wheel on OS X (\#735), resolving issue \#553.
- The shapely.ops.orient function can now orient multi polygons and geometry collections as well as polygons (\#733).
- Polygons can now be constructed from sequences of point objects as well as sequences of x , y sequences (\#732).
- The exterior of an empty polygon is now equal to an empty linear ring (\#731).
- The bounds property of an empty point object now returns an empty tuple, consistent with other geometry types (\#723).
- Segmentation faults when non-string values are passed to the WKT loader are avoided by \#700.
- Failure of ops.substring when the sub linestring coincides with the beginning of the linestring has been fixed (\#658).
- Segmentation faults from interpolating on an empty linestring are prevented by \#655.
- A missing special case for rectangular polygons has been added to the polylabel algorithm (\#644).
- LinearRing can be created from a LineString (\#638).
- The prepared geometry validation condition has been tightened in \#632 to fix the bug reported in \#631.
- Attempting to interpolate an empty geometry no longer results in a segmentation fault, raising ValueError instead (\#653).


## 1.7a1 (2018-07-29)

New features:

- A Python version check is made by the package setup script. Shapely 1.7 supports only Python versions 2.7 and 3.4+ (\#610).
- Added a new EmptyGeometry class to support GeoPandas (\#514).
- Added new shapely.ops.substring function (\#459).
- Added new shapely.ops.clip_by_rect function (\#583).
- Use DLLs indicated in sys._MEIPASS' to support PyInstaller frozen apps (\#523).
- shapely.wkb.dumps now accepts an srid integer keyword argument to write WKB data including a spatial reference ID in the output data (\#593).

Bug fixes:

- shapely.geometry.shape can now marshal empty GeoJSON representations (\#573).
- An exception is raised when an attempt is made to prepare a PreparedGeometry (\#577, \#595).
- Keyword arguments have been removed from a geometry object's wkt property getter (\#581, \#594).


### 1.6.4.post1 (2018-01-24)

- Fix broken markup in this change log, which restores our nicely formatted readme on PyPI.
1.6.4 (2018-01-24)
- Handle a TypeError that can occur when geometries are torn down (\#473, \#528).
1.6.3 (2017-12-09)
- AttributeError is no longer raised when accessing __geo_interface__ of an empty polygon (\#450).
- asShape now handles empty coordinates in mappings as shape does (\#542). Please note that asShape is likely to be deprecated in a future version of Shapely.
- Check for length of LineString coordinates in speed mode, preventing crashes when using LineStrings with only one coordinate (\#546).
1.6.2 (2017-10-30)
- A 1.6.2.post1 release has been made to fix a problem with macosx wheels uploaded to PyPI.


### 1.6.2 (2017-10-26)

- Splitting a linestring by one of its end points will now succeed instead of failing with a ValueError (\#524, \#533).
- Missing documentation of a geometry's overlaps predicate has been added (\#522).


### 1.6.1 (2017-09-01)

- Avoid STRTree crashes due to dangling references (\#505) by maintaining references to added geometries.
- Reduce log level to debug when reporting on calls to ctypes CDLL() that don't succeed and are retried (\#515).
- Clarification: applications like GeoPandas that need an empty geometry object should use BaseGeometry () instead of Point () or Polygon(). An EmptyGeometry class has been added in the master development branch and will be available in the next non-bugfix release.


### 1.6.0 (2017-08-21)

Shapely 1.6.0 adds new attributes to existing geometry classes and new functions (split() and polylabel()) to the shapely.ops module. Exceptions are consolidated in a shapely.errors module and logging practices have been improved. Shapely's optional features depending on Numpy are now gathered into a requirements set named "vectorized" and these may be installed like pip install shapely[vectorized].

Much of the work on 1.6 .0 was aimed to improve the project's build and packaging scripts and to minimize run-time dependencies. Shapely now vendorizes packaging to use during builds only and never again invokes the geos-config utility at run-time.
In addition to the changes listed under the alpha and beta pre-releases below, the following change has been made to the project:

- Project documentation is now hosted at https://shapely.readthedocs.io/en/latest/.

Thank you all for using, promoting, and contributing to the Shapely project.

## 1.6 b 5 (2017-08-18)

Bug fixes:

- Passing a single coordinate to LineString() with speedups disabled now raises a ValueError as happens with speedups enabled. This resolves \#509.


## 1.6b4 (2017-02-15)

Bug fixes:

- Isolate vendorized packaging in a _vendor directory, remove obsolete dist-info, and remove packaging from project requirements (resolves \#468).


## 1.6b3 (2016-12-31)

Bug fixes:

- Level for log messages originating from the GEOS notice handler reduced from WARNING to INFO (\#447).
- Permit speedups to be imported again without Numpy (\#444).


## 1.6b2 (2016-12-12)

New features:

- Add support for GeometryCollection to shape and asShape functions (\#422).


## 1.6b1 (2016-12-12)

Bug fixes:

- Implemented __array_interface__ for empty Points and LineStrings (\#403).


## 1.6a3 (2016-12-01)

Bug fixes:

- Remove accidental hard requirement of Numpy (\#431).

Packaging:

- Put Numpy in an optional requirement set named "vectorized" (\#431).


## 1.6a2 (2016-11-09)

Bug fixes:

- Shapely no longer configures logging in geos.py (\#415).

Refactoring:

- Consolidation of exceptions in shapely.errors.
- UnsupportedGEOSVersionError is raised when GEOS < 3.3.0 (\#407).

Packaging:

- Added new library search paths to assist Anaconda (\#413).
- geos-config will now be bypassed when NO_GEOS_CONFIG env var is set. This allows configuration of Shapely builds on Linux systems that for whatever reasons do not include the geos-config program (\#322).


## 1.6a1 (2016-09-14)

New features:

- A new error derived from NotImplementedError, with a more useful message, is raised when the GEOS backend doesn't support a called method (\#216).
- The project () method of LineString has been extended to LinearRing geometries (\#286).
- A new minimum_rotated_rectangle attribute has been added to the base geometry class (\#354).
- A new shapely.ops.polylabel() function has been added. It computes a point suited for labeling concave polygons (\#395).
- A new shapely.ops.split() function has been added. It splits a geometry by another geometry of lesser dimension: polygon by line, line by point (\#293, \#371).
- Polygon. from_bounds() constructs a Polygon from bounding coordinates (\#392).
- Support for testing with Numpy 1.4.1 has been added (\#301).
- Support creating all kinds of empty geometries from empty lists of Python objects (\#397, \#404).

Refactoring:

- Switch from SingleSidedBuffer() to OffsetCurve() for GEOS >= 3.3 (\#270).
- Cython speedups are now enabled by default (\#252).


## Packaging:

- Packaging 16.7, a setup dependency, is vendorized (\#314).
- Infrastructure for building manylinux 1 wheels has been added (\#391).
- The system's geos-config program is now only checked when setup.py is executed, never during normal use of the module (\#244).
- Added new library search paths to assist PyInstaller (\#382) and Windows (\#343).


### 1.5.17 (2016-08-31)

- Bug fix: eliminate memory leak in geom_factory() (\#408).
- Bug fix: remove mention of negative distances in parallel_offset and note that vertices of right hand offset lines are reversed (\#284).


### 1.5.16 (2016-05-26)

- Bug fix: eliminate memory leak when unpickling geometry objects (\#384, \#385).
- Bug fix: prevent crashes when attempting to pickle a prepared geometry, raising PicklingError instead (\#386).
- Packaging: extension modules in the OS X wheels uploaded to PyPI link only libgeos_c.dylib now (you can verify and compare to previous releases with otool -L shapely/vectorized/_vectorized.so).


### 1.5.15 (2016-03-29)

- Bug fix: use uintptr_t to store pointers instead of long in _geos.pxi, preventing an overflow error (\#372, \#373). Note that this bug fix was erroneously reported to have been made in 1.5 .14 , but was not.


### 1.5.14 (2016-03-27)

- Bug fix: use type() instead of isinstance() when evaluating geometry equality, preventing instances of base and derived classes from being mistaken for equals (\#317).
- Bug fix: ensure that empty geometries are created when constructors have no args (\#332, \#333).
- Bug fix: support app "freezing" better on Windows by not relying on the __file__ attribute (\#342, \#377).
- Bug fix: ensure that empty polygons evaluate to be $==(\# 355)$.
- Bug fix: filter out empty geometries that can cause segfaults when creating and loading STRtrees (\#345, \#348).
- Bug fix: no longer attempt to reuse GEOS DLLs already loaded by Rasterio or Fiona on OS X (\#374, \#375).


### 1.5.13 (2015-10-09)

- Restore setup and runtime discovery and loading of GEOS shared library to state at version 1.5 .9 (\#326).
- On OS X we try to reuse any GEOS shared library that may have been loaded via import of Fiona or Rasterio in order to avoid a bug involving the GEOS AbstractSTRtree (\#324, \#327).


### 1.5.12 (2015-08-27)

- Remove configuration of root logger from libgeos.py (\#312).
- Skip test_fallbacks on Windows (\#308).
- Call setlocale(locale.LC_ALL, "") instead of resetlocale() on Windows when tearing down the locale test (\#308).
- Fix for Sphinx warnings (\#309).
- Addition of .cache, .idea, .pyd, .pdb to .gitignore (\#310).


### 1.5.11 (2015-08-23)

- Remove packaging module requirement added in 1.5 .10 (\#305). Distutils can't parse versions using 'rc', but if we stick to ' a ' and ' $b$ ' we will be fine.


### 1.5.10 (2015-08-22)

- Monkey patch affinity module by absolute reference (\#299).
- Raise TopologicalError in relate() instead of crashing (\#294, \#295, \#303).


### 1.5.9 (2015-05-27)

- Fix for 64 bit speedups compatibility (\#274).


### 1.5.8 (2015-04-29)

- Setup file encoding bug fix (\#254).
- Support for pyinstaller (\#261).
- Major prepared geometry operation fix for Windows (\#268, \#269).
- Major fix for OS X binary wheel (\#262).


### 1.5.7 (2015-03-16)

- Test and fix buggy error and notice handlers (\#249).


### 1.5.6 (2015-02-02)

- Fix setup regression (\#232, \#234).
- SVG representation improvements (\#233, \#237).


### 1.5.5 (2015-01-20)

- MANIFEST changes to restore _geox.pxi (\#231).


### 1.5.4 (2015-01-19)

- Fixed OS X binary wheel library load path (\#224).


### 1.5.3 (2015-01-12)

- Fixed ownership and potential memory leak in polygonize (\#223).
- Wider release of binary wheels for OS X.


### 1.5.2 (2015-01-04)

- Fail installation if GEOS dependency is not met, preventing update breakage (\#218, \#219).
1.5.1 (2014-12-04)
- Restore geometry hashing (\#209).
1.5.0 (2014-12-02)
- Affine transformation speedups (\#197).
- New == rich comparison (\#195).
- Geometry collection constructor (\#200).
- ops.snap() backed by GEOSSnap (\#201).
- Clearer exceptions in cases of topological invalidity (\#203).


### 1.4.4 (2014-11-02)

- Proper conversion of numpy float32 vals to coords (\#186).


### 1.4.3 (2014-10-01)

- Fix for endianness bug in WKB writer (\#174).


### 1.4.2 (2014-09-29)

- Fix bungled 1.4.1 release (\#176).


### 1.4.1 (2014-09-23)

- Return of support for GEOS 3.2 (\#176, \#178).


## 1.4 .0 (2014-09-08)

- SVG representations for IPython's inline image protocol.
- Efficient and fast vectorized contains().
- Change mitre_limit default to 5.0; raise ValueError with 0.0 (\#139).
- Allow mix of tuples and Points in sped-up LineString ctor (\#152).
- New STRtree class (\#73).
- Add ops.nearest_points() (\#147).
- Faster creation of geometric objects from others (cloning) (\#165).
- Removal of tests from package.


### 1.3.3 (2014-07-23)

- Allow single-part geometries as argument to ops.cacaded_union() (\#135).
- Support affine transformations of LinearRings (\#112).


### 1.3.2 (2014-05-13)

- Let LineString() take a sequence of Points (\#130).


### 1.3.1 (2014-04-22)

- More reliable proxy cleanup on exit (\#106).
- More robust DLL loading on all platforms (\#114).


### 1.3.0 (2013-12-31)

- Include support for Python 3.2 and 3.3 (\#56), minimum version is now 2.6.
- Switch to GEOS WKT/WKB Reader/Writer API, with defaults changed to enable 3D output dimensions, and to 'trim' WKT output for GEOS >=3.3.0.
- Use GEOS version instead of GEOS C API version to determine library capabilities (\#65).


### 1.2.19 (2013-12-30)

- Add buffering style options (\#55).


### 1.2.18 (2013-07-23)

- Add shapely.ops.transform.
- Permit empty sequences in collection constructors (\#49, \#50).
- Individual polygons in MultiPolygon.__geo_interface__ are changed to tuples to match Polygon.__geo_interface__(\#51).
- Add shapely.ops.polygonize_full (\#57).


### 1.2.17 (2013-01-27)

- Avoid circular import between wkt/wkb and geometry.base by moving calls to GEOS serializers to the latter module.
- Set _ndim when unpickling (issue \#6).
- Don’t install DLLs to Python's DLL directory (\#37).
- Add affinity module of affine transformation (\#31).
- Fix NameError that blocked installation with PyPy (\#40, \#41).


### 1.2.16 (2012-09-18)

- Add ops.unary_union function.
- Alias ops.cascaded_union to ops.unary_union when GEOS CAPI >=(1,7,0).
- Add geos_version_string attribute to shapely.geos.
- Ensure parent is set when child geometry is accessed.
- Generate _speedups.c using Cython when building from repo when missing, stale, or the build target is "sdist".
- The is_simple predicate of invalid, self-intersecting linear rings now returns False.
- Remove VERSION.txt from repo, it's now written by the distutils setup script with value of shapely. $\qquad$ _version__ _.
1.2.15 (2012-06-27)
- Eliminate numerical sensitivity in a method chaining test (Debian bug \#663210).
- Account for cascaded union of random buffered test points being a polygon or multipolygon (Debian bug \#666655).
- Use Cython to build speedups if it is installed.
- Avoid stumbling over SVN revision numbers in GEOS C API version strings.


### 1.2.14 (2012-01-23)

- A geometry's coords property is now sliceable, yielding a list of coordinate values.
- Homogeneous collections are now sliceable, yielding a new collection of the same type.


### 1.2.13 (2011-09-16)

- Fixed errors in speedups on 32bit systems when GEOS references memory above 2GB.
- Add shapely.__version__ attribute.
- Update the manual.


### 1.2.12 (2011-08-15)

- Build Windows distributions with VC7 or VC9 as appropriate.
- More verbose report on failure to speed up.
- Fix for prepared geometries broken in 1.2.11.
- DO NOT INSTALL 1.2.11


### 1.2.11 (2011-08-04)

- Ignore AttributeError during exit.
- PyPy 1.5 support.
- Prevent operation on prepared geometry crasher (\#12).
- Optional Cython speedups for Windows.
- Linux 3 platform support.


### 1.2.10 (2011-05-09)

- Add optional Cython speedups.
- Add is_cww predicate to LinearRing.
- Add function that forces orientation of Polygons.
- Disable build of speedups on Windows pending packaging work.


### 1.2.9 (2011-03-31)

- Remove extra glob import.
- Move examples to shapely.examples.
- Add box() constructor for rectangular polygons.
- Fix extraneous imports.


### 1.2.8 (2011-12-03)

- New parallel_offset method (\#6).
- Support for Python 2.4.


### 1.2.7 (2010-11-05)

- Support for Windows eggs.


### 1.2.6 (2010-10-21)

- The geoms property of an empty collection yields [] instead of a ValueError (\#3).
- The coords and geometry type sproperties have the same behavior as above.
- Ensure that z values carry through into products of operations (\#4).


### 1.2.5 (2010-09-19)

- Stop distributing docs/_build.
- Include library fallbacks in test_dlls.py for linux platform.


### 1.2.4 (2010-09-09)

- Raise AttributeError when there's no backend support for a method.
- Raise OSError if libgeos_c.so (or variants) can't be found and loaded.
- Add geos_c DLL loading support for linux platforms where find_library doesn't work.


### 1.2.3 (2010-08-17)

- Add mapping function.
- Fix problem with GEOSisValidReason symbol for GEOS < 3.1.


### 1.2.2 (2010-07-23)

- Add representative_point method.


### 1.2.1 (2010-06-23)

- Fixed bounds of singular polygons.
- Added shapely.validation.explain_validity function (\#226).


## 1.2 (2010-05-27)

- Final release.


## 1.2rc2 (2010-05-26)

- Add examples and tests to MANIFEST.in.
- Release candidate 2.
1.2rc1 (2010-05-25)
- Release candidate.
1.2b7 (2010-04-22)
- Memory leak associated with new empty geometry state fixed.


## 1.2b6 (2010-04-13)

- Broken GeometryCollection fixed.


## 1.2b5 (2010-04-09)

- Objects can be constructed from others of the same type, thereby making copies. Collections can be constructed from sequences of objects, also making copies.
- Collections are now iterators over their component objects.
- New code for manual figures, using the descartes package.


## 1.2b4 (2010-03-19)

- Adds support for the "sunos5" platform.


## 1.2b3 (2010-02-28)

- Only provide simplification implementations for GEOS C API >=1.5.


## 1.2b2 (2010-02-19)

- Fix cascaded_union bug introduced in 1.2 b 1 (\#212).


## 1.2b1 (2010-02-18)

- Update the README. Remove cruft from setup.py. Add some version 1.2 metadata regarding required Python version ( $>=2.5,<3$ ) and external dependency (libgeos_c >=3.1).


## $1.2 a 6$ (2010-02-09)

- Add accessor for separate arrays of X and Y values (\#210).

TODO: fill gap here

## 1.2a1 (2010-01-20)

- Proper prototyping of WKB writer, and avoidance of errors on 64-bit systems (\#191).
- Prototype libgeos_c functions in a way that lets py2exe apps import shapely (\#189).
1.2 Branched (2009-09-19)
1.0.12 (2009-04-09)
- Fix for references held by topology and predicate descriptors.


### 1.0.11 (2008-11-20)

- Work around bug in GEOS 2.2.3, GEOSCoordSeq_getOrdinate not exported properly (\#178).
1.0 .10 (2008-11-17)
- Fixed compatibility with GEOS 2.2.3 that was broken in 1.0.8 release (\#176).
1.0.9 (2008-11-16)
- Find and load MacPorts libgeos.
1.0.8 (2008-11-01)
- Fill out GEOS function result and argument types to prevent faults on a 64-bit arch.
1.0.7 (2008-08-22)
- Polygon rings now have the same dimensions as parent (\#168).
- Eliminated reference cycles in polygons (\#169).
1.0.6 (2008-07-10)
- Fixed adaptation of multi polygon data.
- Raise exceptions earlier from binary predicates.
- Beginning distributing new windows DLLs (\#166).


### 1.0.5 (2008-05-20)

- Added access to GEOS polygonizer function.
- Raise exception when insufficient coordinate tuples are passed to LinearRing constructor (\#164).


### 1.0.4 (2008-05-01)

- Disentangle Python and topological equality (\#163).
- Add shape(), a factory that copies coordinates from a geo interface provider. To be used instead of asShape() unless you really need to store coordinates outside shapely for efficient use in other code.
- Cache GEOS geometries in adapters (\#163).
1.0.3 (2008-04-09)
- Do not release GIL when calling GEOS functions (\#158).
- Prevent faults when chaining multiple GEOS operators (\#159).


### 1.0.2 (2008-02-26)

- Fix loss of dimensionality in polygon rings (\#155).


### 1.0.1 (2008-02-08)

- Allow chaining expressions involving coordinate sequences and geometry parts (\#151).
- Protect against abnormal use of coordinate accessors (\#152).
- Coordinate sequences now implement the numpy array protocol (\#153).


## 1.0 (2008-01-18)

- Final release.
1.0 RC2 (2008-01-16)
- Added temporary solution for \#149.


### 1.0 RC1 (2008-01-14)

- First release candidate


### 5.6 Geometry

Shapely geometry classes, such as shapely.Point, are the central data types in Shapely. Each geometry class extends the shapely. Geometry base class, which is a container of the underlying GEOS geometry object, to provide geometry type-specific attributes and behavior. The Geometry object keeps track of the underlying GEOS geometry and lets the python garbage collector free its memory when it is not used anymore.
Geometry objects are immutable. This means that after constructed, they cannot be changed in place. Every Shapely operation will result in a new object being returned.

### 5.6.1 Geometry types

| Point(*args) | A geometry type that represents a single coordinate with <br> x,y and possibly z values. |
| :--- | :--- |
| LineString([coordinates]) | A geometry type composed of one or more line seg- <br> ments. |
| LinearRing([coordinates]) | A geometry type composed of one or more line segments <br> that forms a closed loop. |
| Polygon([shell, holes]) | A geometry type representing an area that is enclosed by <br> a linear ring. |
| MultiPoint([points]) | A collection of one or more Points. |
| MultiLineString([lines]) | A collection of one or more LineStrings. |
| MultiPolygon([polygons]) | A collection of one or more Polygons. |
| GeometryCollection([geoms]) | A collection of one or more geometries that may contain <br> more than one type of geometry. |

## shapely.Point

## class Point(*args)

A geometry type that represents a single coordinate with $\mathrm{x}, \mathrm{y}$ and possibly z values.
A point is a zero-dimensional feature and has zero length and zero area.

## Parameters

args [float, or sequence of floats] The coordinates can either be passed as a single parameter, or as individual float values using multiple parameters:

1) 1 parameter: a sequence or array-like of with 2 or 3 values.
2) 2 or 3 parameters (float): $x, y$, and possibly $z$.

## Examples

Constructing the Point using separate parameters for x and y :
>>> p = Point (1.0, -1.0)
Constructing the Point using a list of $\mathrm{x}, \mathrm{y}$ coordinates:

```
>>> p = Point([1.0, -1.0])
>>> print(p)
POINT (1 -1)
>>> p.y
-1.0
>>> p.x
1.0
```


## Attributes

$\mathbf{x}, \mathbf{y}, \mathbf{z}$ [float] Coordinate values

## almost_equals(other, decimal=6)

True if geometries are equal at all coordinates to a specified decimal place.
Deprecated since version 1.8.0: The 'almost_equals()' method is deprecated and will be removed in Shapely 2.1 because the name is confusing. The 'equals_exact()' method should be used instead.

Refers to approximate coordinate equality, which requires coordinates to be approximately equal and in the same order for all components of a geometry.

Because of this it is possible for "equals()" to be True for two geometries and "almost_equals()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
#.. [(0, 0), (2, 2)]
... ).equals_exact(
#.. LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
...)
False
```


## property area

Unitless area of the geometry (float)

## property boundary

Returns a lower dimension geometry that bounds the object
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty (null) collection.

## property bounds

Returns minimum bounding region (minx, miny, maxx, maxy)
buffer (distance, quad_segs=16, cap_style='round', join_style='round', mitre_limit=5.0, single_sided=False, **kwargs)
Get a geometry that represents all points within a distance of this geometry.
A positive distance produces a dilation, a negative distance an erosion. A very small or zero distance may sometimes be used to "tidy" a polygon.

## Parameters

distance [float] The distance to buffer around the object.
resolution [int, optional] The resolution of the buffer around each vertex of the object.
quad_segs [int, optional] Sets the number of line segments used to approximate an angle fillet.
cap_style [shapely.BufferCapStyle or \{'round', 'square', 'flat'\}, default 'round'] Specifies the shape of buffered line endings. BufferCapStyle.round ('round') results in circular line endings (see quad_segs). Both BufferCapStyle.square ('square') and BufferCapStyle.flat ('flat') result in rectangular line endings, only BufferCapStyle.flat ('flat') will end at the original vertex, while BufferCapStyle.square ('square') involves adding the buffer width.
join_style [shapely.BufferJoinStyle or \{'round', 'mitre', 'bevel'\}, default 'round'] Specifies the shape of buffered line midpoints. BufferJoinStyle.ROUND ('round') results in rounded shapes. BufferJoinStyle.bevel ('bevel') results in a beveled edge that touches the original vertex. BufferJoinStyle.mitre ('mitre') results in a single vertex that is beveled depending on the mitre_limit parameter.
mitre_limit [float, optional] The mitre limit ratio is used for very sharp corners. The mitre ratio is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
single_side [bool, optional] The side used is determined by the sign of the buffer distance:
a positive distance indicates the left-hand side a negative distance indicates the righthand side

The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of CAP_FLAT.
quadsegs [int, optional] Deprecated alias for quad_segs.

## Returns

## Geometry

## Notes

The return value is a strictly two-dimensional geometry. All Z coordinates of the original geometry will be ignored.

## Examples

```
>>> from shapely.wkt import loads
>>> g = loads('POINT (0.0 0.0)')
```

16-gon approx of a unit radius circle:

```
>>> g.buffer(1.0).area
3.1365484905459...
```

128-gon approximation:

```
>>> g.buffer(1.0, 128).area
3.141513801144...
```

triangle approximation:

```
>>> g.buffer(1.0, 3).area
3.0
>>> list(g.buffer(1.0, cap_style=BufferCapStyle.square).exterior.coords)
[(1.0, 1.0), (1.0, -1.0), (-1.0, -1.0), (-1.0, 1.0), (1.0, 1.0)]
>>> g.buffer(1.0, cap_style=BufferCapStyle.square).area
4.0
```


## property centroid

Returns the geometric center of the object

```
contains(other)
```

Returns True if the geometry contains the other, else False

## contains_properly (other)

Returns True if the geometry completely contains the other, with no common boundary points, else False
Refer to shapely.contains_properly for full documentation.

## property convex_hull

Imagine an elastic band stretched around the geometry: that's a convex hull, more or less
The convex hull of a three member multipoint, for example, is a triangular polygon.

## property coords

Access to geometry's coordinates (CoordinateSequence)
covered_by (other)
Returns True if the geometry is covered by the other, else False

## covers(other)

Returns True if the geometry covers the other, else False

## crosses (other)

Returns True if the geometries cross, else False

```
difference(other, grid_size=None)
```

Returns the difference of the geometries.
Refer to shapely.difference for full documentation.

## disjoint (other)

Returns True if geometries are disjoint, else False

## distance(other)

Unitless distance to other geometry (float)
dwithin(other, distance)
Returns True if geometry is within a given distance from the other, else False.
Refer to shapely.dwithin for full documentation.

## property envelope

A figure that envelopes the geometry

```
equals(other)
```

Returns True if geometries are equal, else False.
This method considers point-set equality (or topological equality), and is equivalent to (self.within(other) \& self.contains(other)).

## Returns

bool

## Examples

```
>>> LineString(
    #.. [(0, 0), (2, 2)]
... ).equals(
... LineString([(0, 0), (1, 1), (2, 2)])
... )
True
equals_exact(other, tolerance)
```

True if geometries are equal to within a specified tolerance.

## Parameters

other [BaseGeometry] The other geometry object in this comparison.
tolerance [float] Absolute tolerance in the same units as coordinates.
This method considers coordinate equality, which requires
coordinates to be equal and in the same order for all components
of a geometry.
Because of this it is possible for "equals()" to be True for two
geometries and "equals_exact()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
#. [(0, 0), (2, 2)]
... ).equals_exact(
#..LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
...)
False
```

property geom_type
Name of the geometry's type, such as 'Point'

## property has_z

True if the geometry's coordinate sequence(s) have $z$ values (are 3-dimensional)
hausdorff_distance(other)
Unitless hausdorff distance to other geometry (float)
interpolate (distance, normalized=False)
Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of line_interpolate_point.

```
intersection(other, grid_size=None)
```

Returns the intersection of the geometries.
Refer to shapely.intersection for full documentation.
intersects(other)
Returns True if geometries intersect, else False

## property is_closed

True if the geometry is closed, else False
Applicable only to 1-D geometries.

## property is_empty

True if the set of points in this geometry is empty, else False

## property is_ring

True if the geometry is a closed ring, else False
property is_simple
True if the geometry is simple, meaning that any self-intersections are only at boundary points, else False

## property is_valid

True if the geometry is valid (definition depends on sub-class), else False

## property length

Unitless length of the geometry (float)

## line_interpolate_point(distance, normalized=False)

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of interpolate.

## line_locate_point(other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of project.

## property minimum_clearance

Unitless distance by which a node could be moved to produce an invalid geometry (float)

## property minimum_rotated_rectangle

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of oriented_envelope.
normalize()
Converts geometry to normal form (or canonical form).
This method orders the coordinates, rings of a polygon and parts of multi geometries consistently. Typically useful for testing purposes (for example in combination with equals_exact).

## Examples

```
>>> from shapely import MultiLineString
>>> line = MultiLineString([[(0, 0), (1, 1)], [(3, 3), (2, 2)]])
>>> line.normalize()
<MULTILINESTRING ((2 2, 3 3), (0 0, 1 1))>
```


## property oriented_envelope

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of minimum_rotated_rectangle.
overlaps (other)
Returns True if geometries overlap, else False
point_on_surface()
Returns a point guaranteed to be within the object, cheaply.
Alias of representative_point.
project (other, normalized=False)
Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of line_locate_point.

## relate(other)

Returns the DE-9IM intersection matrix for the two geometries (string)
relate_pattern(other, pattern)
Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, else False
representative_point()
Returns a point guaranteed to be within the object, cheaply.
Alias of point_on_surface.
reverse()
Returns a copy of this geometry with the order of coordinates reversed.
If the geometry is a polygon with interior rings, the interior rings are also reversed.
Points are unchanged.
See also:
is_ccw Checks if a geometry is clockwise.

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (1, 2)]).reverse()
<LINESTRING (1 2, 0 0)>
>>> Polygon([(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)]).reverse()
<POLYGON ((Q Q, Q 1, 1 1, 1 0, Q 0))>
```

segmentize(max_segment_length)
Adds vertices to line segments based on maximum segment length.
Additional vertices will be added to every line segment in an input geometry so that segments are no longer than the provided maximum segment length. New vertices will evenly subdivide each segment.
Only linear components of input geometries are densified; other geometries are returned unmodified.

## Parameters

max_segment_length [float or array_like] Additional vertices will be added so that all line segments are no longer this value. Must be greater than 0 .

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (0, 10)]).segmentize(max_segment_length=5)
<LINESTRING (0 0, 0 5, 0 10)>
>>> Polygon([(0, 0), (10, 0), (10, 10), (0, 10), (0, 0)]).segmentize(max_
\rightarrow \text { segment_length=5)}
<POLYGON ((O 0, 5 0, 10 0, 10 5, 10 10, 5 10, 0 10, 0 5, 0 0))>
```

simplify(tolerance, preserve_topology=True)
Returns a simplified geometry produced by the Douglas-Peucker algorithm
Coordinates of the simplified geometry will be no more than the tolerance distance from the original. Unless the topology preserving option is used, the algorithm may produce self-intersecting or otherwise invalid geometries.
$\mathbf{s v g}$ (scale_factor=1.0, fill_color=None, opacity=None)
Returns SVG circle element for the Point geometry.

## Parameters

scale_factor [float] Multiplication factor for the SVG circle diameter. Default is 1.
fill_color [str, optional] Hex string for fill color. Default is to use "\#66cc99" if geometry is valid, and "\#ff3333" if invalid.
opacity [float] Float number between 0 and 1 for color opacity. Default value is 0.6

```
symmetric_difference(other,grid_size=None)
```

Returns the symmetric difference of the geometries.
Refer to shapely.symmetric_difference for full documentation.

## touches (other)

Returns True if geometries touch, else False

```
union(other, grid_size=None)
```

Returns the union of the geometries.
Refer to shapely.union for full documentation.
within(other)
Returns True if geometry is within the other, else False

## property wkb

WKB representation of the geometry
property wkb_hex
WKB hex representation of the geometry

## property wkt

WKT representation of the geometry
property x
Return x coordinate.
property xy
Separate arrays of $X$ and $Y$ coordinate values

## Example:

```
>>> x, y = Point(0, 0).xy
>>> list(x)
[0.0]
>>> list(y)
[0.0]
```


## property y

Return y coordinate.
property $z$
Return z coordinate.
shapely.LineString

## class LineString (coordinates=None)

A geometry type composed of one or more line segments.
A LineString is a one-dimensional feature and has a non-zero length but zero area. It may approximate a curve and need not be straight. Unlike a LinearRing, a LineString is not closed.

## Parameters

coordinates [sequence] A sequence of (x, y, [,z]) numeric coordinate pairs or triples, or an array-like with shape ( $\mathrm{N}, 2$ ) or ( $\mathrm{N}, 3$ ). Also can be a sequence of Point objects.

## Examples

Create a LineString with two segments

```
>>> a = LineString([[0, 0], [1, 0], [1, 1]])
>>> a.length
2.0
```

almost_equals(other, decimal=6)

True if geometries are equal at all coordinates to a specified decimal place.
Deprecated since version 1.8.0: The 'almost_equals()' method is deprecated and will be removed in Shapely 2.1 because the name is confusing. The 'equals_exact()' method should be used instead.

Refers to approximate coordinate equality, which requires coordinates to be approximately equal and in the same order for all components of a geometry.

Because of this it is possible for "equals()" to be True for two geometries and "almost_equals()" to be False.

## Returns

## bool

## Examples

```
>>> LineString(
... [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
...)
False
```


## property area

Unitless area of the geometry (float)

## property boundary

Returns a lower dimension geometry that bounds the object
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty (null) collection.

## property bounds

Returns minimum bounding region (minx, miny, maxx, maxy)
buffer (distance, quad_segs=16, cap_style='round', join_style='round', mitre_limit=5.0, single_sided=False, **kwargs)
Get a geometry that represents all points within a distance of this geometry.
A positive distance produces a dilation, a negative distance an erosion. A very small or zero distance may sometimes be used to "tidy" a polygon.

## Parameters

distance [float] The distance to buffer around the object.
resolution [int, optional] The resolution of the buffer around each vertex of the object.
quad_segs [int, optional] Sets the number of line segments used to approximate an angle fillet.
cap_style [shapely.BufferCapStyle or \{ 'round', 'square', 'flat'\}, default 'round'] Specifies the shape of buffered line endings. BufferCapStyle.round ('round') results in circular line endings (see quad_segs). Both BufferCapStyle.square ('square') and BufferCapStyle.flat ('flat') result in rectangular line endings, only BufferCapStyle.flat ('flat') will end at the original vertex, while BufferCapStyle.square ('square') involves adding the buffer width.
join_style [shapely.BufferJoinStyle or \{'round', 'mitre', 'bevel'\}, default 'round'] Specifies the shape of buffered line midpoints. BufferJoinStyle.ROUND ('round') results in rounded shapes. BufferJoinStyle.bevel ('bevel') results in a beveled edge that touches the original vertex. BufferJoinStyle.mitre ('mitre') results in a single vertex that is beveled depending on the mitre_limit parameter.
mitre_limit [float, optional] The mitre limit ratio is used for very sharp corners. The mitre ratio is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
single_side [bool, optional] The side used is determined by the sign of the buffer distance:
a positive distance indicates the left-hand side a negative distance indicates the righthand side

The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of CAP_FLAT.
quadsegs [int, optional] Deprecated alias for quad_segs.

## Returns

## Geometry

## Notes

The return value is a strictly two-dimensional geometry. All Z coordinates of the original geometry will be ignored.

## Examples

```
>>> from shapely.wkt import loads
>>> g = loads('POINT (0.0 0.0)')
```

16-gon approx of a unit radius circle:

```
>>> g.buffer(1.0).area
3.1365484905459...
```

128-gon approximation:

```
>>> g.buffer(1.0, 128).area
3.141513801144...
```

triangle approximation:

```
>>> g.buffer(1.0, 3).area
3.0
>>> list(g.buffer(1.0, cap_style=BufferCapStyle.square).exterior.coords)
[(1.0, 1.0), (1.0, -1.0), (-1.0, -1.0), (-1.0, 1.0), (1.0, 1.0)]
>>> g.buffer(1.0, cap_style=BufferCapStyle.square).area
4 . 0
```


## property centroid

Returns the geometric center of the object

## contains (other)

Returns True if the geometry contains the other, else False
contains_properly(other)
Returns True if the geometry completely contains the other, with no common boundary points, else False
Refer to shapely.contains_properly for full documentation.
property convex_hull
Imagine an elastic band stretched around the geometry: that's a convex hull, more or less
The convex hull of a three member multipoint, for example, is a triangular polygon.

## property coords

Access to geometry's coordinates (CoordinateSequence)
covered_by (other)
Returns True if the geometry is covered by the other, else False

## covers(other)

Returns True if the geometry covers the other, else False

```
crosses(other)
```

Returns True if the geometries cross, else False

## difference (other, grid_size=None)

Returns the difference of the geometries.
Refer to shapely.difference for full documentation.

## disjoint (other)

Returns True if geometries are disjoint, else False

## distance (other)

Unitless distance to other geometry (float)
dwithin(other, distance)
Returns True if geometry is within a given distance from the other, else False.
Refer to shapely.dwithin for full documentation.
property envelope
A figure that envelopes the geometry

## equals(other)

Returns True if geometries are equal, else False.
This method considers point-set equality (or topological equality), and is equivalent to (self.within(other) \& self.contains(other)).

## Returns

bool

## Examples

```
>>> LineString(
... [(0, 0), (2, 2)]
... ).equals(
... LineString([(0, 0), (1, 1), (2, 2)])
... )
True
```

equals_exact (other, tolerance)

True if geometries are equal to within a specified tolerance.

## Parameters

other [BaseGeometry] The other geometry object in this comparison.
tolerance [float] Absolute tolerance in the same units as coordinates.
This method considers coordinate equality, which requires coordinates to be equal and in the same order for all components of a geometry.

Because of this it is possible for "equals()" to be True for two geometries and "equals_exact()" to be False.

## Returns

bool

Examples

```
>>> LineString(
#.. [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
.".)
False
```


## property geom_type

Name of the geometry's type, such as 'Point'
property has_z
True if the geometry's coordinate sequence(s) have z values (are 3-dimensional)
hausdorff_distance (other)
Unitless hausdorff distance to other geometry (float)

## interpolate (distance, normalized=False)

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.

Alias of line_interpolate_point.
intersection(other, grid_size=None)
Returns the intersection of the geometries.
Refer to shapely.intersection for full documentation.

```
intersects(other)
```

Returns True if geometries intersect, else False

```
property is_closed
```

True if the geometry is closed, else False
Applicable only to 1-D geometries.

## property is_empty

True if the set of points in this geometry is empty, else False

## property is_ring

True if the geometry is a closed ring, else False

## property is_simple

True if the geometry is simple, meaning that any self-intersections are only at boundary points, else False

```
property is_valid
```

True if the geometry is valid (definition depends on sub-class), else False

## property length

Unitless length of the geometry (float)

## line_interpolate_point(distance, normalized=False)

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of interpolate.

## line_locate_point (other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of project.

## property minimum_clearance

Unitless distance by which a node could be moved to produce an invalid geometry (float)

## property minimum_rotated_rectangle

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of oriented_envelope.
normalize()
Converts geometry to normal form (or canonical form).
This method orders the coordinates, rings of a polygon and parts of multi geometries consistently. Typically useful for testing purposes (for example in combination with equals_exact).

## Examples

```
>>> from shapely import MultiLineString
>>> line = MultiLineString([[(0, 0), (1, 1)], [(3, 3), (2, 2)]])
>>> line.normalize()
<MULTILINESTRING ((2 2, 3 3), (0 0, 1 1))>
```

offset_curve(distance, quad_segs=16, join_style=BufferJoinStyle.round, mitre_limit=5.0)
Returns a LineString or MultiLineString geometry at a distance from the object on its right or its left side.
The side is determined by the sign of the distance parameter (negative for right side offset, positive for left side offset). The resolution of the buffer around each vertex of the object increases by increasing the quad_segs keyword parameter.

The join style is for outside corners between line segments. Accepted values are JOIN_STYLE.round (1), JOIN_STYLE.mitre (2), and JOIN_STYLE.bevel (3).

The mitre ratio limit is used for very sharp corners. It is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend far beyond the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
Note: the behaviour regarding orientation of the resulting line depends on the GEOS version. With GEOS <3.11, the line retains the same direction for a left offset (positive distance) or has reverse direction for a right offset (negative distance), and this behaviour was documented as such in previous Shapely versions. Starting with GEOS 3.11, the function tries to preserve the orientation of the original line.

## property oriented_envelope

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of minimum_rotated_rectangle.
overlaps (other)
Returns True if geometries overlap, else False
parallel_offset (distance, side='right', resolution=16, join_style=BufferJoinStyle.round, mitre_limit=5.0)
Alternative method to offset_curve() method.
Older alternative method to the offset_curve() method, but uses resolution instead of quad_segs and a side keyword ('left' or 'right') instead of sign of the distance. This method is kept for backwards compatibility for now, but is is recommended to use offset_curve() instead.

## point_on_surface()

Returns a point guaranteed to be within the object, cheaply.
Alias of representative_point.

## project (other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of line_locate_point.

```
relate(other)
```

Returns the DE-9IM intersection matrix for the two geometries (string)
relate_pattern(other, pattern)
Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, else False

## representative_point()

Returns a point guaranteed to be within the object, cheaply.
Alias of point_on_surface.
reverse()
Returns a copy of this geometry with the order of coordinates reversed.
If the geometry is a polygon with interior rings, the interior rings are also reversed.
Points are unchanged.

## See also:

is_ccw Checks if a geometry is clockwise.

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (1, 2)]).reverse()
<LINESTRING (1 2, 0 0)>
>> Polygon([(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)]).reverse()
<POLYGON ((Q 0, 0 1, 1 1, 1 0, 0 0))>
```

segmentize(max_segment_length)

Adds vertices to line segments based on maximum segment length.
Additional vertices will be added to every line segment in an input geometry so that segments are no longer than the provided maximum segment length. New vertices will evenly subdivide each segment.

Only linear components of input geometries are densified; other geometries are returned unmodified.

## Parameters

max_segment_length [float or array_like] Additional vertices will be added so that all line segments are no longer this value. Must be greater than 0 .

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (0, 10)]).segmentize(max_segment_length=5)
<LINESTRING (0 0, 0 5, 0 10)>
>>> Polygon([(0, 0), (10, 0), (10, 10), (0, 10), (0, 0)]).segmentize(max_
segment_length=5)
<POLYGON ((0 0, 5 0, 10 0, 10 5, 10 10, 5 10, 0 10, 0 5, 0 0))>
```

```
simplify(tolerance, preserve_topology=True)
```

Returns a simplified geometry produced by the Douglas-Peucker algorithm
Coordinates of the simplified geometry will be no more than the tolerance distance from the original. Unless the topology preserving option is used, the algorithm may produce self-intersecting or otherwise invalid geometries.
$\mathbf{s v g}($ scale_factor $=1.0$, stroke_color=None, opacity=None)
Returns SVG polyline element for the LineString geometry.

## Parameters

scale_factor [float] Multiplication factor for the SVG stroke-width. Default is 1.
stroke_color [str, optional] Hex string for stroke color. Default is to use "\#66cc99" if geometry is valid, and "\#ff 3333 " if invalid.
opacity [float] Float number between 0 and 1 for color opacity. Default value is 0.8

```
symmetric_difference(other, grid_size=None)
```

Returns the symmetric difference of the geometries.
Refer to shapely.symmetric_difference for full documentation.
touches (other)
Returns True if geometries touch, else False

```
union(other, grid_size=None)
```

Returns the union of the geometries.
Refer to shapely.union for full documentation.

```
within(other)
```

Returns True if geometry is within the other, else False

## property wkb

WKB representation of the geometry
property wkb_hex
WKB hex representation of the geometry
property wkt
WKT representation of the geometry
property xy
Separate arrays of X and Y coordinate values
Example:

```
>>> x, y = LineString([(0, 0), (1, 1)]).xy
>>> list(x)
[0.0, 1.0]
>>> list(y)
[0.0, 1.0]
```


## shapely.LinearRing

## class LinearRing(coordinates=None)

A geometry type composed of one or more line segments that forms a closed loop.
A LinearRing is a closed, one-dimensional feature. A LinearRing that crosses itself or touches itself at a single point is invalid and operations on it may fail.

## Parameters

coordinates [sequence] A sequence of ( $\mathrm{x}, \mathrm{y}[, \mathrm{z}]$ ) numeric coordinate pairs or triples, or an arraylike with shape ( $\mathrm{N}, 2$ ) or ( $\mathrm{N}, 3$ ). Also can be a sequence of Point objects.

## Notes

Rings are automatically closed. There is no need to specify a final coordinate pair identical to the first.

## Examples

Construct a square ring.

```
>> ring = LinearRing( ((0, 0), (0, 1), (1 , 1 ), (1 , 0)) )
>>> ring.is_closed
True
>>> list(ring.coords)
[(0.0, 0.0), (0.0, 1.0), (1.0, 1.0), (1.0, 0.0), (0.0, 0.0)]
>>> ring.length
4.0
```


## almost_equals(other, decimal=6)

True if geometries are equal at all coordinates to a specified decimal place.
Deprecated since version 1.8.0: The 'almost_equals()' method is deprecated and will be removed in Shapely 2.1 because the name is confusing. The 'equals_exact()' method should be used instead.

Refers to approximate coordinate equality, which requires coordinates to be approximately equal and in the same order for all components of a geometry.

Because of this it is possible for "equals()" to be True for two geometries and "almost_equals()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
                [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
...)
False
```

property area

Unitless area of the geometry (float)

## property boundary

Returns a lower dimension geometry that bounds the object
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty (null) collection.

## property bounds

Returns minimum bounding region (minx, miny, maxx, maxy)
buffer (distance, quad_segs=16, cap_style='round', join_style='round', mitre_limit=5.0, single_sided=False, **kwargs)
Get a geometry that represents all points within a distance of this geometry.
A positive distance produces a dilation, a negative distance an erosion. A very small or zero distance may sometimes be used to "tidy" a polygon.

## Parameters

distance [float] The distance to buffer around the object.
resolution [int, optional] The resolution of the buffer around each vertex of the object.
quad_segs [int, optional] Sets the number of line segments used to approximate an angle fillet.
cap_style [shapely.BufferCapStyle or \{ 'round', 'square', 'flat'\}, default 'round'] Specifies the shape of buffered line endings. BufferCapStyle.round ('round') results in circular line endings (see quad_segs). Both BufferCapStyle.square ('square') and BufferCapStyle.flat ('flat') result in rectangular line endings, only BufferCapStyle.flat ('flat') will end at the original vertex, while BufferCapStyle.square ('square') involves adding the buffer width.
join_style [shapely.BufferJoinStyle or \{'round', 'mitre', 'bevel'\}, default 'round'] Specifies the shape of buffered line midpoints. BufferJoinStyle.ROUND ('round') results in rounded shapes. BufferJoinStyle.bevel ('bevel') results in a beveled edge that touches the original vertex. BufferJoinStyle.mitre ('mitre') results in a single vertex that is beveled depending on the mitre_limit parameter.
mitre_limit [float, optional] The mitre limit ratio is used for very sharp corners. The mitre ratio is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
single_side [bool, optional] The side used is determined by the sign of the buffer distance:
a positive distance indicates the left-hand side a negative distance indicates the righthand side

The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of CAP_FLAT.
quadsegs [int, optional] Deprecated alias for quad_segs.

## Returns

## Geometry

## Notes

The return value is a strictly two-dimensional geometry. All Z coordinates of the original geometry will be ignored.

## Examples

```
>>> from shapely.wkt import loads
>>> g = loads('POINT (0.0 0.0)')
```

16-gon approx of a unit radius circle:

```
>>> g.buffer(1.0).area
3.1365484905459...
```

128-gon approximation:

```
>>> g.buffer(1.0, 128).area
3.141513801144...
```

triangle approximation:

```
>>> g.buffer(1.0, 3).area
3.0
>>> list(g.buffer(1.0, cap_style=BufferCapStyle.square).exterior.coords)
[(1.0, 1.0), (1.0, -1.0), (-1.0, -1.0), (-1.0, 1.0), (1.0, 1.0)]
>>> g.buffer(1.0, cap_style=BufferCapStyle.square).area
4.0
```


## property centroid

Returns the geometric center of the object

## contains(other)

Returns True if the geometry contains the other, else False

## contains_properly(other)

Returns True if the geometry completely contains the other, with no common boundary points, else False
Refer to shapely.contains_properly for full documentation.

## property convex_hull

Imagine an elastic band stretched around the geometry: that's a convex hull, more or less
The convex hull of a three member multipoint, for example, is a triangular polygon.
property coords
Access to geometry's coordinates (CoordinateSequence)

```
covered_by(other)
```

Returns True if the geometry is covered by the other, else False

## covers(other)

Returns True if the geometry covers the other, else False

## crosses (other)

Returns True if the geometries cross, else False

```
difference(other, grid_size=None)
```

Returns the difference of the geometries.
Refer to shapely.difference for full documentation.

## disjoint(other)

Returns True if geometries are disjoint, else False

## distance(other)

Unitless distance to other geometry (float)
dwithin(other, distance)
Returns True if geometry is within a given distance from the other, else False.
Refer to shapely.dwithin for full documentation.

## property envelope

A figure that envelopes the geometry

## equals(other)

Returns True if geometries are equal, else False.
This method considers point-set equality (or topological equality), and is equivalent to (self.within(other) \& self.contains(other)).

## Returns

bool

## Examples

```
>>> LineString(
#. [(0, 0), (2, 2)]
... ).equals(
... LineString([(0, 0), (1, 1), (2, 2)])
... )
True
```

equals_exact (other, tolerance)

True if geometries are equal to within a specified tolerance.

## Parameters

other [BaseGeometry] The other geometry object in this comparison.
tolerance [float] Absolute tolerance in the same units as coordinates.
This method considers coordinate equality, which requires coordinates to be equal and in the same order for all components
of a geometry.
Because of this it is possible for "equals()" to be True for two
geometries and "equals_exact()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
... [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
#..)
False
```

property geom_type

Name of the geometry's type, such as 'Point'
property has_z

True if the geometry's coordinate sequence(s) have $z$ values (are 3-dimensional)
hausdorff_distance(other)
Unitless hausdorff distance to other geometry (float)

```
interpolate(distance, normalized=False)
```

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of line_interpolate_point.
intersection(other, grid_size=None)
Returns the intersection of the geometries.
Refer to shapely.intersection for full documentation.
intersects (other)
Returns True if geometries intersect, else False
property is_ccw
True is the ring is oriented counter clock-wise
property is_closed
True if the geometry is closed, else False
Applicable only to 1-D geometries.
property is_empty
True if the set of points in this geometry is empty, else False
property is_ring
True if the geometry is a closed ring, else False

## property is_simple

True if the geometry is simple, meaning that any self-intersections are only at boundary points, else False property is_valid

True if the geometry is valid (definition depends on sub-class), else False

## property length

Unitless length of the geometry (float)

## line_interpolate_point (distance, normalized=False)

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of interpolate.

## line_locate_point (other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of project.
property minimum_clearance
Unitless distance by which a node could be moved to produce an invalid geometry (float)

## property minimum_rotated_rectangle

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of oriented_envelope.
normalize()
Converts geometry to normal form (or canonical form).
This method orders the coordinates, rings of a polygon and parts of multi geometries consistently. Typically useful for testing purposes (for example in combination with equals_exact).

## Examples

```
>>> from shapely import MultiLineString
>>> line = MultiLineString([[(0, 0), (1, 1)], [(3, 3), (2, 2)]])
>>> line.normalize()
<MULTILINESTRING ((2 2, 3 3), (0 0, 1 1))>
```

offset_curve(distance, quad_segs=16, join_style=BufferJoinStyle.round, mitre_limit=5.0)
Returns a LineString or MultiLineString geometry at a distance from the object on its right or its left side.
The side is determined by the sign of the distance parameter (negative for right side offset, positive for left side offset). The resolution of the buffer around each vertex of the object increases by increasing the quad_segs keyword parameter.

The join style is for outside corners between line segments. Accepted values are JOIN_STYLE.round (1), JOIN_STYLE.mitre (2), and JOIN_STYLE.bevel (3).

The mitre ratio limit is used for very sharp corners. It is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend far beyond the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
Note: the behaviour regarding orientation of the resulting line depends on the GEOS version. With GEOS <3.11, the line retains the same direction for a left offset (positive distance) or has reverse direction for a right offset (negative distance), and this behaviour was documented as such in previous Shapely versions. Starting with GEOS 3.11, the function tries to preserve the orientation of the original line.

## property oriented_envelope

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of minimum_rotated_rectangle.

## overlaps(other)

Returns True if geometries overlap, else False
parallel_offset (distance, side='right', resolution=16, join_style=BufferJoinStyle.round, mitre_limit=5.0)
Alternative method to offset_curve() method.
Older alternative method to the offset_curve() method, but uses resolution instead of quad_segs and a side keyword ('left' or 'right') instead of sign of the distance. This method is kept for backwards compatibility for now, but is is recommended to use offset_curve() instead.

## point_on_surface()

Returns a point guaranteed to be within the object, cheaply.
Alias of representative_point.
project (other, normalized=False)
Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of line_locate_point.
relate(other)
Returns the DE-9IM intersection matrix for the two geometries (string)
relate_pattern (other, pattern)
Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, else False
representative_point()
Returns a point guaranteed to be within the object, cheaply.
Alias of point_on_surface.
reverse()
Returns a copy of this geometry with the order of coordinates reversed.
If the geometry is a polygon with interior rings, the interior rings are also reversed.
Points are unchanged.
See also:
is_ccw Checks if a geometry is clockwise.

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (1, 2)]).reverse()
<LINESTRING (1 2, 0 0)>
>>> Polygon([(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)]).reverse()
<POLYGON ((0 0, 0 1, 1 1, 1 0, 0 0))>
```

segmentize (max_segment_length)
Adds vertices to line segments based on maximum segment length.
Additional vertices will be added to every line segment in an input geometry so that segments are no longer than the provided maximum segment length. New vertices will evenly subdivide each segment.

Only linear components of input geometries are densified; other geometries are returned unmodified.

## Parameters

max_segment_length [float or array_like] Additional vertices will be added so that all line segments are no longer this value. Must be greater than 0 .

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (0, 10)]).segmentize(max_segment_length=5)
<LINESTRING (0 0, 0 5, 0 10)>
>>> Polygon([(0, 0), (10, 0), (10, 10), (0, 10), (0, 0)]).segmentize(max_
segment_length=5)
<POLYGON ((0 0, 5 0, 10 0, 10 5, 10 10, 5 10, 0 10, 0 5, 0 0))>
```

simplify(tolerance, preserve_topology=True)
Returns a simplified geometry produced by the Douglas-Peucker algorithm
Coordinates of the simplified geometry will be no more than the tolerance distance from the original. Unless the topology preserving option is used, the algorithm may produce self-intersecting or otherwise invalid geometries.
$\mathbf{s v g}($ scale_factor $=1.0$, stroke_color=None, opacity=None)
Returns SVG polyline element for the LineString geometry.

## Parameters

scale_factor [float] Multiplication factor for the SVG stroke-width. Default is 1.
stroke_color [str, optional] Hex string for stroke color. Default is to use "\#66cc99" if geometry is valid, and "\#ff 3333 " if invalid.
opacity [float] Float number between 0 and 1 for color opacity. Default value is 0.8

```
symmetric_difference(other, grid_size=None)
```

Returns the symmetric difference of the geometries.
Refer to shapely.symmetric_difference for full documentation.

## touches (other)

Returns True if geometries touch, else False
union(other, grid_size=None)
Returns the union of the geometries.
Refer to shapely.union for full documentation.
within(other)
Returns True if geometry is within the other, else False

## property wkb

WKB representation of the geometry
property wkb_hex
WKB hex representation of the geometry

## property wkt

WKT representation of the geometry
property xy
Separate arrays of X and Y coordinate values
Example:

```
>>> x, y = LineString([(0, 0), (1, 1)]).xy
>>> list(x)
[0.0, 1.0]
>>> list(y)
[0.0, 1.0]
```


## shapely.Polygon

class Polygon (shell=None, holes=None)
A geometry type representing an area that is enclosed by a linear ring.
A polygon is a two-dimensional feature and has a non-zero area. It may have one or more negative-space "holes" which are also bounded by linear rings. If any rings cross each other, the feature is invalid and operations on it may fail.

## Parameters

shell [sequence] A sequence of (x, y [,z]) numeric coordinate pairs or triples, or an array-like with shape ( $\mathrm{N}, 2$ ) or ( $\mathrm{N}, 3$ ). Also can be a sequence of Point objects.
holes [sequence] A sequence of objects which satisfy the same requirements as the shell parameters above

## Examples

Create a square polygon with no holes

```
>>> coords = ((0., 0.), (0., 1.), (1., 1.), (1., 0.), (0., 0.))
>>> polygon = Polygon(coords)
>>> polygon.area
1.0
```


## Attributes

exterior [LinearRing] The ring which bounds the positive space of the polygon.
interiors [sequence] A sequence of rings which bound all existing holes.

## almost_equals(other, decimal=6)

True if geometries are equal at all coordinates to a specified decimal place.
Deprecated since version 1.8.0: The 'almost_equals()' method is deprecated and will be removed in Shapely 2.1 because the name is confusing. The 'equals_exact()' method should be used instead.

Refers to approximate coordinate equality, which requires coordinates to be approximately equal and in the same order for all components of a geometry.
Because of this it is possible for "equals()" to be True for two geometries and "almost_equals()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
#.. [(0, 0), (2, 2)]
... ).equals_exact(
#.. LineString([(0, 0), (1, 1), (2, 2)]),
#. 1e-6
...)
False
```


## property area

Unitless area of the geometry (float)

## property boundary

Returns a lower dimension geometry that bounds the object
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty (null) collection.

## property bounds

Returns minimum bounding region (minx, miny, maxx, maxy)
buffer (distance, quad_segs=16, cap_style='round', join_style='round', mitre_limit=5.0, single_sided=False, **kwargs)
Get a geometry that represents all points within a distance of this geometry.
A positive distance produces a dilation, a negative distance an erosion. A very small or zero distance may sometimes be used to "tidy" a polygon.

## Parameters

distance [float] The distance to buffer around the object.
resolution [int, optional] The resolution of the buffer around each vertex of the object.
quad_segs [int, optional] Sets the number of line segments used to approximate an angle fillet.
cap_style [shapely.BufferCapStyle or \{ 'round', 'square', 'flat'\}, default 'round'] Specifies the shape of buffered line endings. BufferCapStyle.round ('round') results in circular line endings (see quad_segs). Both BufferCapStyle.square ('square') and BufferCapStyle.flat
('flat') result in rectangular line endings, only BufferCapStyle.flat ('flat') will end at the original vertex, while BufferCapStyle.square ('square') involves adding the buffer width.
join_style [shapely.BufferJoinStyle or \{ 'round', 'mitre', 'bevel'\}, default 'round'] Specifies the shape of buffered line midpoints. BufferJoinStyle.ROUND ('round') results in rounded shapes. BufferJoinStyle.bevel ('bevel') results in a beveled edge that touches the original vertex. BufferJoinStyle.mitre ('mitre') results in a single vertex that is beveled depending on the mitre_limit parameter.
mitre_limit [float, optional] The mitre limit ratio is used for very sharp corners. The mitre ratio is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
single_side [bool, optional] The side used is determined by the sign of the buffer distance:
a positive distance indicates the left-hand side a negative distance indicates the righthand side

The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of CAP_FLAT.
quadsegs [int, optional] Deprecated alias for quad_segs.

## Returns

## Geometry

## Notes

The return value is a strictly two-dimensional geometry. All Z coordinates of the original geometry will be ignored.

## Examples

```
>>> from shapely.wkt import loads
>>> g = loads('POINT (0.0 0.0)')
```

16-gon approx of a unit radius circle:

```
>>> g.buffer(1.0).area
3.1365484905459...
```

128-gon approximation:

```
>>> g.buffer(1.0, 128).area
3.141513801144...
```

triangle approximation:

```
>>> g.buffer(1.0, 3).area
3.0
>>> list(g.buffer(1.0, cap_style=BufferCapStyle.square).exterior.coords)
[(1.0, 1.0), (1.0, -1.0), (-1.0, -1.0), (-1.0, 1.0), (1.0, 1.0)]
>>> g.buffer(1.0, cap_style=BufferCapStyle.square).area
4.0
```


## property centroid

Returns the geometric center of the object

## contains(other)

Returns True if the geometry contains the other, else False

## contains_properly (other)

Returns True if the geometry completely contains the other, with no common boundary points, else False
Refer to shapely.contains_properly for full documentation.

## property convex_hull

Imagine an elastic band stretched around the geometry: that's a convex hull, more or less
The convex hull of a three member multipoint, for example, is a triangular polygon.

## property coords

Access to geometry's coordinates (CoordinateSequence)

## covered_by(other)

Returns True if the geometry is covered by the other, else False
covers(other)
Returns True if the geometry covers the other, else False

## crosses (other)

Returns True if the geometries cross, else False

## difference(other, grid_size=None)

Returns the difference of the geometries.
Refer to shapely.difference for full documentation.

```
disjoint(other)
```

Returns True if geometries are disjoint, else False

## distance(other)

Unitless distance to other geometry (float)
dwithin(other, distance)
Returns True if geometry is within a given distance from the other, else False.
Refer to shapely.dwithin for full documentation.

## property envelope

A figure that envelopes the geometry

```
equals(other)
```

Returns True if geometries are equal, else False.
This method considers point-set equality (or topological equality), and is equivalent to (self.within(other) \& self.contains(other)).

## Returns

bool

## Examples

```
>>> LineString(
... [(0, 0), (2, 2)]
... ).equals(
... LineString([(0, 0), (1, 1), (2, 2)])
..")
True
```


## equals_exact (other, tolerance)

True if geometries are equal to within a specified tolerance.

## Parameters

other [BaseGeometry] The other geometry object in this comparison. tolerance [float] Absolute tolerance in the same units as coordinates.
This method considers coordinate equality, which requires coordinates to be equal and in the same order for all components of a geometry.

Because of this it is possible for "equals()" to be True for two geometries and "equals_exact()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
#. [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
...")
False
```

classmethod from_bounds (xmin, ymin, xmax, ymax)

Construct a Polygon() from spatial bounds.

```
property geom_type
```

Name of the geometry's type, such as 'Point'
property has_z

True if the geometry's coordinate sequence(s) have $z$ values (are 3-dimensional)
hausdorff_distance(other)
Unitless hausdorff distance to other geometry (float)
interpolate (distance, normalized=False)
Return a point at the specified distance along a linear geometry

Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of line_interpolate_point.

```
intersection(other, grid_size=None)
```

Returns the intersection of the geometries.
Refer to shapely.intersection for full documentation.

## intersects(other)

Returns True if geometries intersect, else False

## property is_closed

True if the geometry is closed, else False
Applicable only to 1-D geometries.

```
property is_empty
```

True if the set of points in this geometry is empty, else False

```
property is_ring
```

True if the geometry is a closed ring, else False

## property is_simple

True if the geometry is simple, meaning that any self-intersections are only at boundary points, else False

## property is_valid

True if the geometry is valid (definition depends on sub-class), else False

## property length

Unitless length of the geometry (float)

```
line_interpolate_point(distance, normalized=False)
```

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.

Alias of interpolate.

## line_locate_point(other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of project.

## property minimum_clearance

Unitless distance by which a node could be moved to produce an invalid geometry (float)
property minimum_rotated_rectangle
Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.
Alias of oriented_envelope.

## normalize()

Converts geometry to normal form (or canonical form).
This method orders the coordinates, rings of a polygon and parts of multi geometries consistently. Typically useful for testing purposes (for example in combination with equals_exact).

## Examples

```
>>> from shapely import MultiLineString
>>> line = MultiLineString([[(0, 0), (1, 1)], [(3, 3), (2, 2)]])
>>> line.normalize()
<MULTILINESTRING ((2 2, 3 3), (0 0, 1 1))>
```


## property oriented_envelope

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of minimum_rotated_rectangle.

## overlaps(other)

Returns True if geometries overlap, else False

```
point_on_surface()
```

Returns a point guaranteed to be within the object, cheaply.
Alias of representative_point.
project (other, normalized=False)
Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of line_locate_point.
relate(other)
Returns the DE-9IM intersection matrix for the two geometries (string)
relate_pattern(other, pattern)
Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, else False
representative_point()
Returns a point guaranteed to be within the object, cheaply.
Alias of point_on_surface.
reverse()
Returns a copy of this geometry with the order of coordinates reversed.
If the geometry is a polygon with interior rings, the interior rings are also reversed.
Points are unchanged.
See also:
is_ccw Checks if a geometry is clockwise.

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (1, 2)]).reverse()
<LINESTRING (1 2, 0 0)>
>>> Polygon([(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)]).reverse()
<POLYGON ((0 0, 0 1, 1 1, 1 0, 0 0))>
```

segmentize (max_segment_length)
Adds vertices to line segments based on maximum segment length.
Additional vertices will be added to every line segment in an input geometry so that segments are no longer than the provided maximum segment length. New vertices will evenly subdivide each segment.
Only linear components of input geometries are densified; other geometries are returned unmodified.

## Parameters

max_segment_length [float or array_like] Additional vertices will be added so that all line segments are no longer this value. Must be greater than 0 .

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (0, 10)]).segmentize(max_segment_length=5)
<LINESTRING (0 0, 0 5, 0 10)>
>>> Polygon([(0, 0), (10, 0), (10, 10), (0, 10), (0, 0)]).segmentize(max_
segment_length=5)
<POLYGON ((0 0, 5 0, 10 0, 10 5, 10 10, 5 10, 0 10, 0 5, 0 0))>
```

simplify (tolerance, preserve_topology=True)
Returns a simplified geometry produced by the Douglas-Peucker algorithm
Coordinates of the simplified geometry will be no more than the tolerance distance from the original. Unless the topology preserving option is used, the algorithm may produce self-intersecting or otherwise invalid geometries.
$\mathbf{s v g}$ (scale_factor=1.0, fill_color=None, opacity=None)
Returns SVG path element for the Polygon geometry.

## Parameters

scale_factor [float] Multiplication factor for the SVG stroke-width. Default is 1.
fill_color [str, optional] Hex string for fill color. Default is to use "\#66cc99" if geometry is valid, and "\#ff3333" if invalid.
opacity [float] Float number between 0 and 1 for color opacity. Default value is 0.6

```
symmetric_difference(other, grid_size=None)
```

Returns the symmetric difference of the geometries.
Refer to shapely.symmetric_difference for full documentation.

## touches (other)

Returns True if geometries touch, else False
union(other, grid_size=None)
Returns the union of the geometries.
Refer to shapely.union for full documentation.
within(other)
Returns True if geometry is within the other, else False

## property wkb

WKB representation of the geometry
property wkb_hex
WKB hex representation of the geometry

## property wkt

WKT representation of the geometry
property xy
Separate arrays of X and Y coordinate values

## shapely.MultiPoint

```
class MultiPoint(points=None)
```

A collection of one or more Points.
A MultiPoint has zero area and zero length.

## Parameters

points [sequence] A sequence of Points, or a sequence of ( $\mathrm{x}, \mathrm{y}[\mathrm{z}]$ ) numeric coordinate pairs or triples, or an array-like of shape $(\mathrm{N}, 2)$ or $(\mathrm{N}, 3)$.

## Examples

Construct a MultiPoint containing two Points

```
>>> from shapely import Point
>>> ob = MultiPoint([[0.0, 0.0], [1.0, 2.0]])
>>> len(ob.geoms)
2
>>> type(ob.geoms[0]) == Point
True
```

```
    Attributes
        geoms [sequence] A sequence of Points
almost_equals(other, decimal=6)
```

True if geometries are equal at all coordinates to a specified decimal place.
Deprecated since version 1.8.0: The 'almost_equals()' method is deprecated and will be removed in Shapely 2.1 because the name is confusing. The 'equals_exact()' method should be used instead.

Refers to approximate coordinate equality, which requires coordinates to be approximately equal and in the same order for all components of a geometry.
Because of this it is possible for "equals()" to be True for two geometries and "almost_equals()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
#.. [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
... )
False
```


## property area

Unitless area of the geometry (float)

## property boundary

Returns a lower dimension geometry that bounds the object
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty (null) collection.

## property bounds

Returns minimum bounding region (minx, miny, maxx, maxy)
buffer (distance, quad_segs=16, cap_style='round', join_style='round', mitre_limit=5.0, single_sided=False,
**kwargs)
Get a geometry that represents all points within a distance of this geometry.
A positive distance produces a dilation, a negative distance an erosion. A very small or zero distance may sometimes be used to "tidy" a polygon.

## Parameters

distance [float] The distance to buffer around the object.
resolution [int, optional] The resolution of the buffer around each vertex of the object.
quad_segs [int, optional] Sets the number of line segments used to approximate an angle fillet.
cap_style [shapely.BufferCapStyle or \{ 'round', 'square', 'flat'\}, default 'round'] Specifies the shape of buffered line endings. BufferCapStyle.round ('round') results in circular line endings (see quad_segs). Both BufferCapStyle.square ('square') and BufferCapStyle.flat ('flat') result in rectangular line endings, only BufferCapStyle.flat ('flat') will end at the original vertex, while BufferCapStyle.square ('square') involves adding the buffer width.
join_style [shapely.BufferJoinStyle or \{'round', 'mitre', 'bevel'\}, default 'round'] Specifies the shape of buffered line midpoints. BufferJoinStyle.ROUND ('round') results in rounded shapes. BufferJoinStyle.bevel ('bevel') results in a beveled edge that touches the original vertex. BufferJoinStyle.mitre ('mitre') results in a single vertex that is beveled depending on the mitre_limit parameter.
mitre_limit [float, optional] The mitre limit ratio is used for very sharp corners. The mitre ratio is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
single_side [bool, optional] The side used is determined by the sign of the buffer distance:
a positive distance indicates the left-hand side a negative distance indicates the righthand side

The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of CAP_FLAT. quadsegs [int, optional] Deprecated alias for quad_segs.

## Returns

## Geometry

## Notes

The return value is a strictly two-dimensional geometry. All Z coordinates of the original geometry will be ignored.

## Examples

```
>>> from shapely.wkt import loads
>>> g = loads('POINT (0.0 0.0)')
```

16-gon approx of a unit radius circle:

```
>>> g.buffer(1.0).area
3.1365484905459...
```

128-gon approximation:

```
>>> g.buffer(1.0, 128).area
3.141513801144...
```

triangle approximation:

```
>>> g.buffer(1.0, 3).area
3.0
>>> list(g.buffer(1.0, cap_style=BufferCapStyle.square).exterior.coords)
[(1.0, 1.0), (1.0, -1.0), (-1.0, -1.0), (-1.0, 1.0), (1.0, 1.0)]
>>> g.buffer(1.0, cap_style=BufferCapStyle.square).area
4.0
```


## property centroid

Returns the geometric center of the object

```
contains(other)
```

Returns True if the geometry contains the other, else False

## contains_properly(other)

Returns True if the geometry completely contains the other, with no common boundary points, else False
Refer to shapely.contains_properly for full documentation.

## property convex_hull

Imagine an elastic band stretched around the geometry: that's a convex hull, more or less
The convex hull of a three member multipoint, for example, is a triangular polygon.
property coords
Access to geometry's coordinates (CoordinateSequence)

## covered_by (other)

Returns True if the geometry is covered by the other, else False
covers(other)
Returns True if the geometry covers the other, else False

## crosses (other)

Returns True if the geometries cross, else False
difference(other, grid_size=None)
Returns the difference of the geometries.
Refer to shapely.difference for full documentation.

## disjoint(other)

Returns True if geometries are disjoint, else False

## distance(other)

Unitless distance to other geometry (float)
dwithin(other, distance)
Returns True if geometry is within a given distance from the other, else False.
Refer to shapely.dwithin for full documentation.

## property envelope

A figure that envelopes the geometry
equals(other)
Returns True if geometries are equal, else False.
This method considers point-set equality (or topological equality), and is equivalent to (self.within(other) \& self.contains(other)).

## Returns

bool

## Examples

```
>>> LineString(
... [(0, 0), (2, 2)]
... ).equals(
... LineString([(0, 0), (1, 1), (2, 2)])
...)
True
```

equals_exact (other, tolerance)

True if geometries are equal to within a specified tolerance.

## Parameters

other [BaseGeometry] The other geometry object in this comparison.
tolerance [float] Absolute tolerance in the same units as coordinates.
This method considers coordinate equality, which requires coordinates to be equal and in the same order for all components
of a geometry.

## Because of this it is possible for "equals()" to be True for two

 geometries and "equals_exact()" to be False.
## Returns

bool

## Examples

```
>>> LineString(
#.. [(0, 0), (2, 2)]
.". ).equals_exact(
#.. LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
... )
False
```


## property geom_type

Name of the geometry's type, such as 'Point'
property has_z
True if the geometry's coordinate sequence(s) have z values (are 3-dimensional)
hausdorff_distance(other)
Unitless hausdorff distance to other geometry (float)
interpolate (distance, normalized=False)
Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of line_interpolate_point.
intersection (other, grid_size=None)
Returns the intersection of the geometries.
Refer to shapely.intersection for full documentation.
intersects (other)
Returns True if geometries intersect, else False
property is_closed
True if the geometry is closed, else False
Applicable only to 1-D geometries.

## property is_empty

True if the set of points in this geometry is empty, else False

## property is_ring

True if the geometry is a closed ring, else False

## property is_simple

True if the geometry is simple, meaning that any self-intersections are only at boundary points, else False

## property is_valid

True if the geometry is valid (definition depends on sub-class), else False

## property length

Unitless length of the geometry (float)

## line_interpolate_point(distance, normalized=False)

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.

Alias of interpolate.

## line_locate_point(other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of project.

## property minimum_clearance

Unitless distance by which a node could be moved to produce an invalid geometry (float)

## property minimum_rotated_rectangle

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of oriented_envelope.

## normalize()

Converts geometry to normal form (or canonical form).
This method orders the coordinates, rings of a polygon and parts of multi geometries consistently. Typically useful for testing purposes (for example in combination with equals_exact).

## Examples

```
>>> from shapely import MultiLineString
>>> line = MultiLineString([[(0, 0), (1, 1)], [(3, 3), (2, 2)]])
>>> line.normalize()
<MULTILINESTRING ((2 2, 3 3), (0 0, 1 1))>
```


## property oriented_envelope

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of minimum_rotated_rectangle.
overlaps (other)
Returns True if geometries overlap, else False
point_on_surface()
Returns a point guaranteed to be within the object, cheaply.
Alias of representative_point.
project (other, normalized=False)
Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of line_locate_point.

## relate(other)

Returns the DE-9IM intersection matrix for the two geometries (string)
relate_pattern(other, pattern)
Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, else False
representative_point()
Returns a point guaranteed to be within the object, cheaply.
Alias of point_on_surface.
reverse()
Returns a copy of this geometry with the order of coordinates reversed.
If the geometry is a polygon with interior rings, the interior rings are also reversed.
Points are unchanged.
See also:
is_ccw Checks if a geometry is clockwise.

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (1, 2)]).reverse()
<LINESTRING (1 2, 0 0)>
>> Polygon([(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)]).reverse()
<POLYGON ((O Q, Q 1, 1 1, 1 0, Q 0))>
```

segmentize(max_segment_length)

Adds vertices to line segments based on maximum segment length.
Additional vertices will be added to every line segment in an input geometry so that segments are no longer than the provided maximum segment length. New vertices will evenly subdivide each segment.

Only linear components of input geometries are densified; other geometries are returned unmodified.

## Parameters

max_segment_length [float or array_like] Additional vertices will be added so that all line segments are no longer this value. Must be greater than 0 .

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (0, 10)]).segmentize(max_segment_length=5)
<LINESTRING (0 0, 0 5, 0 10)>
>>> Polygon([(0, 0), (10, 0), (10, 10), (0, 10), (0, 0)]).segmentize(max_
\rightarrow \text { segment_length=5)}
<POLYGON ((0 0, 5 0, 10 0, 10 5, 10 10, 5 10, 0 10, 0 5, 0 0))>
```

simplify(tolerance, preserve_topology=True)
Returns a simplified geometry produced by the Douglas-Peucker algorithm
Coordinates of the simplified geometry will be no more than the tolerance distance from the original. Unless the topology preserving option is used, the algorithm may produce self-intersecting or otherwise invalid geometries.
$\mathbf{s v g}$ (scale_factor $=1.0$, fill_color=None, opacity=None)
Returns a group of SVG circle elements for the MultiPoint geometry.

## Parameters

scale_factor [float] Multiplication factor for the SVG circle diameters. Default is 1.
fill_color [str, optional] Hex string for fill color. Default is to use "\#66cc99" if geometry is valid, and "\#ff3333" if invalid.
opacity [float] Float number between 0 and 1 for color opacity. Default value is 0.6

```
symmetric_difference(other,grid_size=None)
```

Returns the symmetric difference of the geometries.
Refer to shapely.symmetric_difference for full documentation.

## touches (other)

Returns True if geometries touch, else False
union(other, grid_size=None)
Returns the union of the geometries.
Refer to shapely.union for full documentation.
within(other)
Returns True if geometry is within the other, else False
property wkb
WKB representation of the geometry
property wkb_hex
WKB hex representation of the geometry
property wkt
WKT representation of the geometry

## property xy

Separate arrays of X and Y coordinate values

## shapely.MultiLineString

## class MultiLineString (lines=None)

A collection of one or more LineStrings.
A MultiLineString has non-zero length and zero area.

## Parameters

lines [sequence] A sequence LineStrings, or a sequence of line-like coordinate sequences or array-likes (see accepted input for LineString).

## Examples

Construct a MultiLineString containing two LineStrings.

```
>>> lines = MultiLineString([[[0, 0], [1, 2]], [[4, 4], [5, 6]]])
```


## Attributes

geoms [sequence] A sequence of LineStrings
almost_equals(other, decimal=6)
True if geometries are equal at all coordinates to a specified decimal place.
Deprecated since version 1.8.0: The 'almost_equals()' method is deprecated and will be removed in Shapely 2.1 because the name is confusing. The 'equals_exact()' method should be used instead.

Refers to approximate coordinate equality, which requires coordinates to be approximately equal and in the same order for all components of a geometry.

Because of this it is possible for "equals()" to be True for two geometries and "almost_equals()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
#. [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
... )
False
```

property area

Unitless area of the geometry (float)

## property boundary

Returns a lower dimension geometry that bounds the object
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty (null) collection.

## property bounds

Returns minimum bounding region (minx, miny, maxx, maxy)
buffer (distance, quad_segs=16, cap_style='round', join_style='round', mitre_limit=5.0, single_sided=False, **kwargs)
Get a geometry that represents all points within a distance of this geometry.
A positive distance produces a dilation, a negative distance an erosion. A very small or zero distance may sometimes be used to "tidy" a polygon.

## Parameters

distance [float] The distance to buffer around the object.
resolution [int, optional] The resolution of the buffer around each vertex of the object.
quad_segs [int, optional] Sets the number of line segments used to approximate an angle fillet.
cap_style [shapely.BufferCapStyle or \{ 'round', 'square', 'flat'\}, default 'round'] Specifies the shape of buffered line endings. BufferCapStyle.round ('round') results in circular line endings (see quad_segs). Both BufferCapStyle.square ('square') and BufferCapStyle.flat ('flat') result in rectangular line endings, only BufferCapStyle.flat ('flat') will end at the original vertex, while BufferCapStyle.square ('square') involves adding the buffer width.
join_style [shapely.BufferJoinStyle or \{ 'round', 'mitre', 'bevel'\}, default 'round'] Specifies the shape of buffered line midpoints. BufferJoinStyle.ROUND ('round') results in rounded shapes. BufferJoinStyle.bevel ('bevel') results in a beveled edge that touches the original vertex. BufferJoinStyle.mitre ('mitre') results in a single vertex that is beveled depending on the mitre_limit parameter.
mitre_limit [float, optional] The mitre limit ratio is used for very sharp corners. The mitre ratio is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
single_side [bool, optional] The side used is determined by the sign of the buffer distance:
a positive distance indicates the left-hand side a negative distance indicates the righthand side

The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of CAP_FLAT.
quadsegs [int, optional] Deprecated alias for quad_segs.

## Returns

## Geometry

## Notes

The return value is a strictly two-dimensional geometry. All Z coordinates of the original geometry will be ignored.

## Examples

```
>>> from shapely.wkt import loads
>>> g = loads('POINT (0.0 0.0)')
```

16-gon approx of a unit radius circle:

```
>>> g.buffer(1.0).area
3.1365484905459...
```

128-gon approximation:

```
>>> g.buffer(1.0, 128).area
3.141513801144...
```

triangle approximation:

```
>>> g.buffer(1.0, 3).area
3.0
>>> list(g.buffer(1.0, cap_style=BufferCapStyle.square).exterior.coords)
[(1.0, 1.0), (1.0, -1.0), (-1.0, -1.0), (-1.0, 1.0), (1.0, 1.0)]
>>> g.buffer(1.0, cap_style=BufferCapStyle.square).area
4.0
```


## property centroid

Returns the geometric center of the object
contains (other)
Returns True if the geometry contains the other, else False
contains_properly (other)
Returns True if the geometry completely contains the other, with no common boundary points, else False
Refer to shapely.contains_properly for full documentation.
property convex_hull
Imagine an elastic band stretched around the geometry: that's a convex hull, more or less
The convex hull of a three member multipoint, for example, is a triangular polygon.

## property coords

Access to geometry's coordinates (CoordinateSequence)
covered_by (other)
Returns True if the geometry is covered by the other, else False
covers(other)
Returns True if the geometry covers the other, else False
crosses (other)
Returns True if the geometries cross, else False
difference (other, grid_size=None)
Returns the difference of the geometries.
Refer to shapely.difference for full documentation.

```
disjoint(other)
```

Returns True if geometries are disjoint, else False

## distance (other)

Unitless distance to other geometry (float)
dwithin(other, distance)
Returns True if geometry is within a given distance from the other, else False.
Refer to shapely.dwithin for full documentation.

## property envelope

A figure that envelopes the geometry
equals(other)
Returns True if geometries are equal, else False.
This method considers point-set equality (or topological equality), and is equivalent to (self.within(other) \& self.contains(other)).

## Returns

bool

## Examples

```
>>> LineString(
#.. [(0, 0), (2, 2)]
....).equals(
... LineString([(0, 0), (1, 1), (2, 2)])
...)
True
```

equals_exact (other, tolerance)
True if geometries are equal to within a specified tolerance.

## Parameters

other [BaseGeometry] The other geometry object in this comparison.
tolerance [float] Absolute tolerance in the same units as coordinates.
This method considers coordinate equality, which requires
coordinates to be equal and in the same order for all components
of a geometry.
Because of this it is possible for "equals()" to be True for two geometries and "equals_exact()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
... [(0, 0), (2, 2)]
... ).equals_exact(
#.. LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
...)
False
```

property geom_type
Name of the geometry's type, such as 'Point'
property has_z
True if the geometry's coordinate sequence(s) have z values (are 3-dimensional)
hausdorff_distance(other)
Unitless hausdorff distance to other geometry (float)
interpolate (distance, normalized=False)
Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of line_interpolate_point.
intersection(other, grid_size=None)
Returns the intersection of the geometries.
Refer to shapely.intersection for full documentation.
intersects (other)
Returns True if geometries intersect, else False
property is_closed
True if the geometry is closed, else False
Applicable only to 1-D geometries.
property is_empty
True if the set of points in this geometry is empty, else False

## property is_ring

True if the geometry is a closed ring, else False
property is_simple
True if the geometry is simple, meaning that any self-intersections are only at boundary points, else False

## property is_valid

True if the geometry is valid (definition depends on sub-class), else False
property length
Unitless length of the geometry (float)

## line_interpolate_point(distance, normalized=False)

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.

Alias of interpolate.
line_locate_point (other, normalized=False)
Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of project.
property minimum_clearance
Unitless distance by which a node could be moved to produce an invalid geometry (float)
property minimum_rotated_rectangle
Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of oriented_envelope.
normalize()
Converts geometry to normal form (or canonical form).
This method orders the coordinates, rings of a polygon and parts of multi geometries consistently. Typically useful for testing purposes (for example in combination with equals_exact).

## Examples

```
>>> from shapely import MultiLineString
>>> line = MultiLineString([[(0, 0), (1, 1)], [(3, 3), (2, 2)]])
>>> line.normalize()
<MULTILINESTRING ((2 2, 3 3), (0 0, 1 1))>
```

property oriented_envelope

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.
Alias of minimum_rotated_rectangle.

## overlaps (other)

Returns True if geometries overlap, else False

```
point_on_surface()
```

Returns a point guaranteed to be within the object, cheaply.
Alias of representative_point.

## project (other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of line_locate_point.

```
relate(other)
```

Returns the DE-9IM intersection matrix for the two geometries (string)
relate_pattern(other, pattern)
Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, else False

## representative_point()

Returns a point guaranteed to be within the object, cheaply.
Alias of point_on_surface.
reverse()
Returns a copy of this geometry with the order of coordinates reversed.
If the geometry is a polygon with interior rings, the interior rings are also reversed.
Points are unchanged.

## See also:

is_ccw Checks if a geometry is clockwise.

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (1, 2)]).reverse()
<LINESTRING (1 2, 0 0)>
>> Polygon([(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)]).reverse()
<POLYGON ((Q 0, 0 1, 1 1, 1 0, 0 0))>
```

segmentize(max_segment_length)

Adds vertices to line segments based on maximum segment length.
Additional vertices will be added to every line segment in an input geometry so that segments are no longer than the provided maximum segment length. New vertices will evenly subdivide each segment.

Only linear components of input geometries are densified; other geometries are returned unmodified.

## Parameters

max_segment_length [float or array_like] Additional vertices will be added so that all line segments are no longer this value. Must be greater than 0 .

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (0, 10)]).segmentize(max_segment_length=5)
<LINESTRING (0 0, 0 5, 0 10)>
>>> Polygon([(0, 0), (10, 0), (10, 10), (0, 10), (0, 0)]).segmentize(max_
segment_length=5)
<POLYGON ((0 0, 5 0, 10 0, 10 5, 10 10, 5 10, 0 10, 0 5, 0 0))>
```

```
simplify(tolerance, preserve_topology=True)
```

Returns a simplified geometry produced by the Douglas-Peucker algorithm
Coordinates of the simplified geometry will be no more than the tolerance distance from the original. Unless the topology preserving option is used, the algorithm may produce self-intersecting or otherwise invalid geometries.
$\mathbf{s v g}($ scale_factor $=1.0$, stroke_color=None, opacity=None)
Returns a group of SVG polyline elements for the LineString geometry.

## Parameters

scale_factor [float] Multiplication factor for the SVG stroke-width. Default is 1.
stroke_color [str, optional] Hex string for stroke color. Default is to use "\#66cc99" if geometry is valid, and "\#ff 3333 " if invalid.
opacity [float] Float number between 0 and 1 for color opacity. Default value is 0.8
symmetric_difference (other, grid_size=None)
Returns the symmetric difference of the geometries.
Refer to shapely.symmetric_difference for full documentation.
touches (other)
Returns True if geometries touch, else False

```
union(other, grid_size=None)
```

Returns the union of the geometries.
Refer to shapely.union for full documentation.

```
within(other)
```

Returns True if geometry is within the other, else False

## property wkb

WKB representation of the geometry
property wkb_hex
WKB hex representation of the geometry
property wkt
WKT representation of the geometry
property xy
Separate arrays of X and Y coordinate values

## shapely.MultiPolygon

```
class MultiPolygon(polygons=None)
```

A collection of one or more Polygons.
If component polygons overlap the collection is invalid and some operations on it may fail.

## Parameters

polygons [sequence] A sequence of Polygons, or a sequence of (shell, holes) tuples where shell is the sequence representation of a linear ring (see LinearRing) and holes is a sequence of such linear rings.

## Examples

Construct a MultiPolygon from a sequence of coordinate tuples

```
>>> from shapely import Polygon
>>> ob = MultiPolygon([
... (
#. ((0.0, 0.0), (0.0, 1.0), (1.0, 1.0), (1.0, 0.0)),
# [((0.1,0.1), (0.1,0.2), (0.2,0.2), (0.2,0.1))]
# )
... ])
>>> len(ob.geoms)
1
>>> type(ob.geoms[0]) == Polygon
True
```


## Attributes

geoms [sequence] A sequence of Polygon instances
almost_equals(other, decimal=6)
True if geometries are equal at all coordinates to a specified decimal place.
Deprecated since version 1.8.0: The 'almost_equals()' method is deprecated and will be removed in Shapely 2.1 because the name is confusing. The 'equals_exact()' method should be used instead.

Refers to approximate coordinate equality, which requires coordinates to be approximately equal and in the same order for all components of a geometry.
Because of this it is possible for "equals()" to be True for two geometries and "almost_equals()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
                [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
...)
False
```

property area

Unitless area of the geometry (float)

## property boundary

Returns a lower dimension geometry that bounds the object
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty (null) collection.

## property bounds

Returns minimum bounding region (minx, miny, maxx, maxy)
buffer (distance, quad_segs=16, cap_style='round', join_style='round', mitre_limit=5.0, single_sided=False, **kwargs)
Get a geometry that represents all points within a distance of this geometry.
A positive distance produces a dilation, a negative distance an erosion. A very small or zero distance may sometimes be used to "tidy" a polygon.

## Parameters

distance [float] The distance to buffer around the object.
resolution [int, optional] The resolution of the buffer around each vertex of the object.
quad_segs [int, optional] Sets the number of line segments used to approximate an angle fillet.
cap_style [shapely.BufferCapStyle or \{ 'round', 'square', 'flat'\}, default 'round'] Specifies the shape of buffered line endings. BufferCapStyle.round ('round') results in circular line endings (see quad_segs). Both BufferCapStyle.square ('square') and BufferCapStyle.flat ('flat') result in rectangular line endings, only BufferCapStyle.flat ('flat') will end at the original vertex, while BufferCapStyle.square ('square') involves adding the buffer width.
join_style [shapely.BufferJoinStyle or \{'round', 'mitre', 'bevel'\}, default 'round'] Specifies the shape of buffered line midpoints. BufferJoinStyle.ROUND ('round') results in rounded shapes. BufferJoinStyle.bevel ('bevel') results in a beveled edge that touches the original vertex. BufferJoinStyle.mitre ('mitre') results in a single vertex that is beveled depending on the mitre_limit parameter.
mitre_limit [float, optional] The mitre limit ratio is used for very sharp corners. The mitre ratio is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
single_side [bool, optional] The side used is determined by the sign of the buffer distance:
a positive distance indicates the left-hand side a negative distance indicates the righthand side

The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of CAP_FLAT.
quadsegs [int, optional] Deprecated alias for quad_segs.

## Returns

## Geometry

## Notes

The return value is a strictly two-dimensional geometry. All Z coordinates of the original geometry will be ignored.

## Examples

```
>>> from shapely.wkt import loads
>>> g = loads('POINT (0.0 0.0)')
```

16-gon approx of a unit radius circle:

```
>>> g.buffer(1.0).area
3.1365484905459...
```

128-gon approximation:

```
>>> g.buffer(1.0, 128).area
3.141513801144...
```

triangle approximation:

```
>>> g.buffer(1.0, 3).area
3.0
>>> list(g.buffer(1.0, cap_style=BufferCapStyle.square).exterior.coords)
[(1.0, 1.0), (1.0, -1.0), (-1.0, -1.0), (-1.0, 1.0), (1.0, 1.0)]
>>> g.buffer(1.0, cap_style=BufferCapStyle.square).area
4.0
```


## property centroid

Returns the geometric center of the object

## contains(other)

Returns True if the geometry contains the other, else False

## contains_properly(other)

Returns True if the geometry completely contains the other, with no common boundary points, else False
Refer to shapely.contains_properly for full documentation.

## property convex_hull

Imagine an elastic band stretched around the geometry: that's a convex hull, more or less
The convex hull of a three member multipoint, for example, is a triangular polygon.

## property coords

Access to geometry's coordinates (CoordinateSequence)

```
covered_by(other)
```

Returns True if the geometry is covered by the other, else False

## covers(other)

Returns True if the geometry covers the other, else False

## crosses (other)

Returns True if the geometries cross, else False

```
difference(other, grid_size=None)
```

Returns the difference of the geometries.
Refer to shapely.difference for full documentation.

## disjoint(other)

Returns True if geometries are disjoint, else False

## distance(other)

Unitless distance to other geometry (float)
dwithin(other, distance)
Returns True if geometry is within a given distance from the other, else False.
Refer to shapely.dwithin for full documentation.

## property envelope

A figure that envelopes the geometry

## equals(other)

Returns True if geometries are equal, else False.
This method considers point-set equality (or topological equality), and is equivalent to (self.within(other) \& self.contains(other)).

## Returns

bool

## Examples

```
>>> LineString(
#. [(0, 0), (2, 2)]
... ).equals(
... LineString([(0, 0), (1, 1), (2, 2)])
... )
True
```

equals_exact (other, tolerance)

True if geometries are equal to within a specified tolerance.

## Parameters

other [BaseGeometry] The other geometry object in this comparison.
tolerance [float] Absolute tolerance in the same units as coordinates.
This method considers coordinate equality, which requires coordinates to be equal and in the same order for all components
of a geometry.
Because of this it is possible for "equals()" to be True for two
geometries and "equals_exact()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
#. [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
#..)
False
```

property geom_type

Name of the geometry's type, such as 'Point'
property has_z

True if the geometry's coordinate sequence(s) have $z$ values (are 3-dimensional)
hausdorff_distance(other)
Unitless hausdorff distance to other geometry (float)

```
interpolate(distance, normalized=False)
```

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of line_interpolate_point.
intersection(other, grid_size=None)
Returns the intersection of the geometries.
Refer to shapely.intersection for full documentation.

## intersects(other)

Returns True if geometries intersect, else False
property is_closed
True if the geometry is closed, else False
Applicable only to 1-D geometries.
property is_empty
True if the set of points in this geometry is empty, else False

## property is_ring

True if the geometry is a closed ring, else False
property is_simple
True if the geometry is simple, meaning that any self-intersections are only at boundary points, else False

## property is_valid

True if the geometry is valid (definition depends on sub-class), else False

## property length

Unitless length of the geometry (float)
line_interpolate_point (distance, normalized=False)
Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.

Alias of interpolate.

## line_locate_point (other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of project.

## property minimum_clearance

Unitless distance by which a node could be moved to produce an invalid geometry (float)

## property minimum_rotated_rectangle

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.
Alias of oriented_envelope.
normalize()
Converts geometry to normal form (or canonical form).
This method orders the coordinates, rings of a polygon and parts of multi geometries consistently. Typically useful for testing purposes (for example in combination with equals_exact).

## Examples

```
>>> from shapely import MultiLineString
>>> line = MultiLineString([[(0, 0), (1, 1)], [(3, 3), (2, 2)]])
>>> line.normalize()
<MULTILINESTRING ((2 2, 3 3), (0 0, 1 1))>
```


## property oriented_envelope

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of minimum_rotated_rectangle.
overlaps (other)
Returns True if geometries overlap, else False

## point_on_surface()

Returns a point guaranteed to be within the object, cheaply.
Alias of representative_point.
project (other, normalized=False)
Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of line_locate_point.
relate(other)
Returns the DE-9IM intersection matrix for the two geometries (string)
relate_pattern(other, pattern)
Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, else False
representative_point()
Returns a point guaranteed to be within the object, cheaply.
Alias of point_on_surface.
reverse()
Returns a copy of this geometry with the order of coordinates reversed.
If the geometry is a polygon with interior rings, the interior rings are also reversed.
Points are unchanged.
See also:
is_ccw Checks if a geometry is clockwise.

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (1, 2)]).reverse()
<LINESTRING (1 2, 0 0)>
>>> Polygon([(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)]).reverse()
<POLYGON ((Q 0, 0 1, 1 1, 1 0, 0 0))>
```


## segmentize(max_segment_length)

Adds vertices to line segments based on maximum segment length.
Additional vertices will be added to every line segment in an input geometry so that segments are no longer than the provided maximum segment length. New vertices will evenly subdivide each segment.
Only linear components of input geometries are densified; other geometries are returned unmodified.

## Parameters

max_segment_length [float or array_like] Additional vertices will be added so that all line segments are no longer this value. Must be greater than 0 .

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (0, 10)]).segmentize(max_segment_length=5)
<LINESTRING (0 0, 0 5, © 10)>
>> Polygon([(0, 0), (10, 0), (10, 10), (0, 10), (0, 0)]).segmentize(max_
<segment_length=5)
<POLYGON ((0 0, 5 0, 10 0, 10 5, 10 10, 5 10, 0 10, 0 5, 0 0))>
```

```
simplify(tolerance, preserve_topology=True)
```

Returns a simplified geometry produced by the Douglas-Peucker algorithm
Coordinates of the simplified geometry will be no more than the tolerance distance from the original. Unless the topology preserving option is used, the algorithm may produce self-intersecting or otherwise invalid geometries.
$\mathbf{s v g}$ (scale_factor=1.0, fill_color=None, opacity=None)
Returns group of SVG path elements for the MultiPolygon geometry.

## Parameters

scale_factor [float] Multiplication factor for the SVG stroke-width. Default is 1.
fill_color [str, optional] Hex string for fill color. Default is to use "\#66cc99" if geometry is valid, and "\#ff3333" if invalid.
opacity [float] Float number between 0 and 1 for color opacity. Default value is 0.6

## symmetric_difference (other, grid_size=None)

Returns the symmetric difference of the geometries.
Refer to shapely.symmetric_difference for full documentation.
touches (other)
Returns True if geometries touch, else False

```
union(other, grid_size=None)
```

Returns the union of the geometries.
Refer to shapely.union for full documentation.

```
within(other)
```

Returns True if geometry is within the other, else False

## property wkb

WKB representation of the geometry
property wkb_hex
WKB hex representation of the geometry
property wkt
WKT representation of the geometry
property xy
Separate arrays of X and Y coordinate values

## shapely.GeometryCollection

class GeometryCollection(geoms=None)
A collection of one or more geometries that may contain more than one type of geometry.

## Parameters

geoms [list] A list of shapely geometry instances, which may be of varying geometry types.

## Examples

Create a GeometryCollection with a Point and a LineString
>>> from shapely import LineString, Point
>>> p = Point (51, -1)
>>> 1 = LineString([(52, -1), (49, 2)])
>>> gc = GeometryCollection([p, l])

## Attributes

geoms [sequence] A sequence of Shapely geometry instances
almost_equals(other, decimal=6)
True if geometries are equal at all coordinates to a specified decimal place.
Deprecated since version 1.8.0: The 'almost_equals()' method is deprecated and will be removed in Shapely 2.1 because the name is confusing. The 'equals_exact()' method should be used instead.

Refers to approximate coordinate equality, which requires coordinates to be approximately equal and in the same order for all components of a geometry.
Because of this it is possible for "equals()" to be True for two geometries and "almost_equals()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
#.. [(0, 0), (2, 2)]
... ).equals_exact(
... LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
... )
False
```


## property area

Unitless area of the geometry (float)

## property boundary

Returns a lower dimension geometry that bounds the object
The boundary of a polygon is a line, the boundary of a line is a collection of points. The boundary of a point is an empty (null) collection.

## property bounds

Returns minimum bounding region (minx, miny, maxx, maxy)
buffer(distance, quad_segs=16, cap_style='round', join_style='round', mitre_limit=5.0, single_sided=False,
**kwargs)
Get a geometry that represents all points within a distance of this geometry.
A positive distance produces a dilation, a negative distance an erosion. A very small or zero distance may sometimes be used to "tidy" a polygon.

## Parameters

distance [float] The distance to buffer around the object.
resolution [int, optional] The resolution of the buffer around each vertex of the object.
quad_segs [int, optional] Sets the number of line segments used to approximate an angle fillet.
cap_style [shapely.BufferCapStyle or \{ 'round', 'square', 'flat'\}, default 'round'] Specifies the shape of buffered line endings. BufferCapStyle.round ('round') results in circular line endings (see quad_segs). Both BufferCapStyle.square ('square') and BufferCapStyle.flat ('flat') result in rectangular line endings, only BufferCapStyle.flat ('flat') will end at the original vertex, while BufferCapStyle.square ('square') involves adding the buffer width.
join_style [shapely.BufferJoinStyle or \{'round', 'mitre', 'bevel'\}, default 'round'] Specifies the shape of buffered line midpoints. BufferJoinStyle.ROUND ('round') results in rounded shapes. BufferJoinStyle.bevel ('bevel') results in a beveled edge that touches the original vertex. BufferJoinStyle.mitre ('mitre') results in a single vertex that is beveled depending on the mitre_limit parameter.
mitre_limit [float, optional] The mitre limit ratio is used for very sharp corners. The mitre ratio is the ratio of the distance from the corner to the end of the mitred offset corner. When two line segments meet at a sharp angle, a miter join will extend the original geometry. To prevent unreasonable geometry, the mitre limit allows controlling the maximum length of the join corner. Corners with a ratio which exceed the limit will be beveled.
single_side [bool, optional] The side used is determined by the sign of the buffer distance:
a positive distance indicates the left-hand side a negative distance indicates the righthand side

The single-sided buffer of point geometries is the same as the regular buffer. The End Cap Style for single-sided buffers is always ignored, and forced to the equivalent of CAP_FLAT.
quadsegs [int, optional] Deprecated alias for quad_segs.

## Returns

## Geometry

## Notes

The return value is a strictly two-dimensional geometry. All Z coordinates of the original geometry will be ignored.

## Examples

```
>>> from shapely.wkt import loads
>>> g = loads('POINT (0.0 0.0)')
```

16-gon approx of a unit radius circle:

```
>>> g.buffer(1.0).area
3.1365484905459...
```

128-gon approximation:

```
>>> g.buffer(1.0, 128).area
3.141513801144...
```

triangle approximation:

```
>>> g.buffer(1.0, 3).area
3.0
>>> list(g.buffer(1.0, cap_style=BufferCapStyle.square).exterior.coords)
[(1.0, 1.0), (1.0, -1.0), (-1.0, -1.0), (-1.0, 1.0), (1.0, 1.0)]
>>> g.buffer(1.0, cap_style=BufferCapStyle.square).area
4.0
```


## property centroid

Returns the geometric center of the object
contains (other)
Returns True if the geometry contains the other, else False
contains_properly (other)
Returns True if the geometry completely contains the other, with no common boundary points, else False
Refer to shapely.contains_properly for full documentation.
property convex_hull
Imagine an elastic band stretched around the geometry: that's a convex hull, more or less
The convex hull of a three member multipoint, for example, is a triangular polygon.

## property coords

Access to geometry's coordinates (CoordinateSequence)
covered_by (other)
Returns True if the geometry is covered by the other, else False

## covers(other)

Returns True if the geometry covers the other, else False
crosses (other)
Returns True if the geometries cross, else False
difference (other, grid_size=None)
Returns the difference of the geometries.
Refer to shapely.difference for full documentation.

```
disjoint(other)
```

Returns True if geometries are disjoint, else False

## distance (other)

Unitless distance to other geometry (float)
dwithin(other, distance)
Returns True if geometry is within a given distance from the other, else False.
Refer to shapely.dwithin for full documentation.

## property envelope

A figure that envelopes the geometry
equals(other)
Returns True if geometries are equal, else False.
This method considers point-set equality (or topological equality), and is equivalent to (self.within(other) \& self.contains(other)).

## Returns

bool

## Examples

```
>>> LineString(
#.. [(0, 0), (2, 2)]
....).equals(
... LineString([(0, 0), (1, 1), (2, 2)])
...)
True
```

equals_exact (other, tolerance)
True if geometries are equal to within a specified tolerance.

## Parameters

other [BaseGeometry] The other geometry object in this comparison.
tolerance [float] Absolute tolerance in the same units as coordinates.
This method considers coordinate equality, which requires
coordinates to be equal and in the same order for all components
of a geometry.
Because of this it is possible for "equals()" to be True for two geometries and "equals_exact()" to be False.

## Returns

bool

## Examples

```
>>> LineString(
... [(0, 0), (2, 2)]
... ).equals_exact(
#.. LineString([(0, 0), (1, 1), (2, 2)]),
... 1e-6
...)
False
```

property geom_type
Name of the geometry's type, such as 'Point'
property has_z
True if the geometry's coordinate sequence(s) have z values (are 3-dimensional)
hausdorff_distance(other)
Unitless hausdorff distance to other geometry (float)
interpolate (distance, normalized=False)
Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.
Alias of line_interpolate_point.
intersection(other, grid_size=None)
Returns the intersection of the geometries.
Refer to shapely.intersection for full documentation.
intersects (other)
Returns True if geometries intersect, else False
property is_closed
True if the geometry is closed, else False
Applicable only to 1-D geometries.
property is_empty
True if the set of points in this geometry is empty, else False

## property is_ring

True if the geometry is a closed ring, else False
property is_simple
True if the geometry is simple, meaning that any self-intersections are only at boundary points, else False

## property is_valid

True if the geometry is valid (definition depends on sub-class), else False
property length
Unitless length of the geometry (float)

## line_interpolate_point(distance, normalized=False)

Return a point at the specified distance along a linear geometry
Negative length values are taken as measured in the reverse direction from the end of the geometry. Out-of-range index values are handled by clamping them to the valid range of values. If the normalized arg is True, the distance will be interpreted as a fraction of the geometry's length.

Alias of interpolate.
line_locate_point (other, normalized=False)
Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of project.
property minimum_clearance
Unitless distance by which a node could be moved to produce an invalid geometry (float)
property minimum_rotated_rectangle
Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.

Alias of oriented_envelope.
normalize()
Converts geometry to normal form (or canonical form).
This method orders the coordinates, rings of a polygon and parts of multi geometries consistently. Typically useful for testing purposes (for example in combination with equals_exact).

## Examples

```
>>> from shapely import MultiLineString
>>> line = MultiLineString([[(0, 0), (1, 1)], [(3, 3), (2, 2)]])
>>> line.normalize()
<MULTILINESTRING ((2 2, 3 3), (0 0, 1 1))>
```

property oriented_envelope

Returns the oriented envelope (minimum rotated rectangle) that encloses the geometry.
Unlike envelope this rectangle is not constrained to be parallel to the coordinate axes. If the convex hull of the object is a degenerate (line or point) this degenerate is returned.
Alias of minimum_rotated_rectangle.

## overlaps (other)

Returns True if geometries overlap, else False

```
point_on_surface()
```

Returns a point guaranteed to be within the object, cheaply.
Alias of representative_point.

## project (other, normalized=False)

Returns the distance along this geometry to a point nearest the specified point
If the normalized arg is True, return the distance normalized to the length of the linear geometry.
Alias of line_locate_point.

```
relate(other)
```

Returns the DE-9IM intersection matrix for the two geometries (string)
relate_pattern(other, pattern)
Returns True if the DE-9IM string code for the relationship between the geometries satisfies the pattern, else False

## representative_point()

Returns a point guaranteed to be within the object, cheaply.
Alias of point_on_surface.
reverse()
Returns a copy of this geometry with the order of coordinates reversed.
If the geometry is a polygon with interior rings, the interior rings are also reversed.
Points are unchanged.

## See also:

is_ccw Checks if a geometry is clockwise.

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (1, 2)]).reverse()
<LINESTRING (1 2, 0 0)>
>> Polygon([(0, 0), (1, 0), (1, 1), (0, 1), (0, 0)]).reverse()
<POLYGON ((Q 0, 0 1, 1 1, 1 0, 0 0))>
```

segmentize(max_segment_length)

Adds vertices to line segments based on maximum segment length.
Additional vertices will be added to every line segment in an input geometry so that segments are no longer than the provided maximum segment length. New vertices will evenly subdivide each segment.

Only linear components of input geometries are densified; other geometries are returned unmodified.

## Parameters

max_segment_length [float or array_like] Additional vertices will be added so that all line segments are no longer this value. Must be greater than 0 .

## Examples

```
>>> from shapely import LineString, Polygon
>>> LineString([(0, 0), (0, 10)]).segmentize(max_segment_length=5)
<LINESTRING (0 0, 0 5, 0 10)>
>>> Polygon([(0, 0), (10, 0), (10, 10), (0, 10), (0, 0)]).segmentize(max_
segment_length=5)
<POLYGON ((0 0, 5 0, 10 0, 10 5, 10 10, 5 10, 0 10, 0 5, 0 0))>
```

```
simplify(tolerance, preserve_topology=True)
```

Returns a simplified geometry produced by the Douglas-Peucker algorithm
Coordinates of the simplified geometry will be no more than the tolerance distance from the original. Unless the topology preserving option is used, the algorithm may produce self-intersecting or otherwise invalid geometries.
$\mathbf{s v g}$ (scale_factor $=1.0$, color $=$ None)
Returns a group of SVG elements for the multipart geometry.

## Parameters

scale_factor [float] Multiplication factor for the SVG stroke-width. Default is 1.
color [str, optional] Hex string for stroke or fill color. Default is to use "\#66cc99" if geometry is valid, and "\#ff 3333 " if invalid.
symmetric_difference(other, grid_size=None)
Returns the symmetric difference of the geometries.
Refer to shapely.symmetric_difference for full documentation.

## touches (other)

Returns True if geometries touch, else False
union(other, grid_size=None)
Returns the union of the geometries.
Refer to shapely.union for full documentation.
within(other)
Returns True if geometry is within the other, else False

## property wkb

WKB representation of the geometry
property wkb_hex
WKB hex representation of the geometry
property wkt
WKT representation of the geometry
property xy
Separate arrays of X and Y coordinate values

### 5.6.2 Construction

Geometries can be constructed directly using Shapely geometry classes:

```
>>> from shapely import Point, LineString
>>> Point(5.2, 52.1)
<POINT (5.2 52.1)>
>>> LineString([(0, 0), (1, 2)])
<LINESTRING (0 0, 1 2)>
```

Geometries can also be constructed from a WKT (Well-Known Text) or WKB (Well-Known Binary) representation:

```
>>> from shapely import from_wkb, from_wkt
>>> from_wkt("POINT (5.2 52.1)")
<POINT (5.2 52.1)>
>>> from_wkb(b"\x01\x01\x00\x00\x00\x00\x00\x00\x00\x00\x00\xf0?\x00\x00\x00\x00\x00\x00\
<xf0?")
<POINT (1 1)>
```

A more efficient way of constructing geometries is by making use of the (vectorized) functions described in Geometry creation.

### 5.6.3 Pickling

Geometries can be serialized using pickle:

```
>>> import pickle
>>> from shapely import Point
>>> pickled = pickle.dumps(Point(1, 1))
>>> pickle.loads(pickled)
<POINT (1 1)>
```

Warning: Pickling will convert linearrings to linestrings. See shapely.to_wkb() for a complete list of limitations.

### 5.6.4 Hashing

Geometries can be used as elements in sets or as keys in dictionaries. Python uses a technique called hashing for lookups in these datastructures. Shapely generates this hash from the WKB representation. Therefore, geometries are equal if and only if their WKB representations are equal.

```
>>> from shapely import Point
>>> point_1 = Point(5.2, 52.1)
>>> point_2 = Point(1, 1)
>>> point_3 = Point(5.2, 52.1)
>>> {point_1, point_2, point_3}
{<POINT (1 1)>, <POINT (5.2 52.1) >}
```

Warning: Due to limitations of WKB, linearrings will equal linestrings if they contain the exact same points. See shapely.to_wkb().

Comparing two geometries directly is also supported. This is the same as using shapely.equals_exact() with a tolerance value of zero.

```
>>> point_1 == point_2
False
>>> point_1 == point_3
True
>>> point_1 != point_2
True
```


### 5.6.5 Formatting

Geometries can be formatted to strings using properties, functions, or a Python format specification.
The most convenient is to use .wkb_hex and .wkt properties.

```
>>> from shapely import Point, to_wkb, to_wkt, to_geojson
>>> pt = Point(-169.910918, -18.997564)
>>> pt.wkb_hex
0101000000CF6A813D263D65C0BDAAB35A60FF32C0
>>> pt.wkt
POINT (-169.910918 -18.997564)
```

More output options can be found using using to_wkb(), to_wkt (), and to_geojson() functions.

```
>>> to_wkb(pt, hex=True, byte_order=0)
0000000001C0653D263D816ACFC032FF605AB3AABD
>>> to_wkt(pt, rounding_precision=3)
POINT (-169.911 -18.998)
>>> print(to_geojson(pt, indent=2))
{
    "type": "Point",
    "coordinates": [
        -169.910918,
        -18.997564
    ]
}
```

A format specification may also be used to control the format and precision.

```
>>> print(f"Cave near {pt:.3f}")
Cave near POINT (-169.911 -18.998)
>>> print(f"or hex-encoded as {pt:x}")
or hex-encoded as 0101000000cf6a813d263d65c0bdaab35a60ff32c0
```

Shapely has a format specification inspired from Python's Format Specification Mini-Language described next.

## Semantic for format specification

```
format_spec ::= [0][.precision][type]
precision ::= digit+
type ::= "f" | "F" | "g" | "G" | "x" | "X"
```

Format types ' f ' and ' F ' are to use a fixed-point notation, which is activated by setting GEOS' trim option off. The upper case variant converts nan to NAN and inf to INF.

Format types ' g ' and ' G ' are to use a "general format", where unnecessary digits are trimmed. This notation is activated by setting GEOS' trim option on. The upper case variant is similar to ' $\mathrm{F}^{\prime}$, and may also display an uppercase "E" if scientific notation is required. Note that this representation may be different for GEOS 3.10.0 and later, which does not use scientific notation.

For numeric outputs ' f ' and ' g ', the precision is optional, and if not specified, rounding precision will be disabled showing full precision.

Format types ' x ' and ' X ' show a hex-encoded string representation of WKB or Well-Known Binary, with the case of the output matched the case of the format type character.

### 5.7 Geometry properties

\{\% for function in get_module_functions("_geometry") \%\} \{\{function \}\}
$\{\%$ endfor \% \}

### 5.8 Geometry creation

\{ \% for function in get_module_functions("creation") $\%$ \} \{ \{ function \}\}
$\{\%$ endfor \% \}

### 5.9 Input/Output

\{\% for function in get_module_functions("io") \% \} \{ \{ function \}\}
$\{\%$ endfor \% \}

### 5.10 Measurement

\{ \% for function in get_module_functions("measurement") \% \} \{ \{ function \}\}
$\{\%$ endfor \% \}

### 5.11 Predicates

\{\% for function in get_module_functions("predicates") \%\} \{\{function \}\}
$\{\%$ endfor \% \}

### 5.12 Set operations

\{\% for function in get_module_functions("set_operations") \% \} \{\{ function \}\}
$\{\%$ endfor \% \}

### 5.13 Constructive operations

\{\% for function in get_module_functions("constructive") \%o\} \{\{ function \}\}
$\{\%$ endfor \% \}

### 5.14 Linestring operations

\{\% for function in get_module_functions("linear") $\%$ \} \{ \{ function \}\}
$\{\%$ endfor \% \}

### 5.15 Coordinate operations

\{\% for function in get_module_functions("coordinates") \% \} \{ \{ function \}\}
$\{\%$ endfor $\%$ \}

### 5.16 STRTree

class STRtree(geoms: Iterable[shapely.geometry.base.BaseGeometry], node_capacity: int =10)
A query-only R-tree spatial index created using the Sort-Tile-Recursive (STR) [1] algorithm.
The tree indexes the bounding boxes of each geometry. The tree is constructed directly at initialization and nodes cannot be added or removed after it has been created.

All operations return indices of the input geometries. These indices can be used to index into anything associated with the input geometries, including the input geometries themselves, or custom items stored in another object of the same length as the geometries.

Bounding boxes limited to two dimensions and are axis-aligned (equivalent to the bounds property of a geometry); any Z values present in geometries are ignored for purposes of indexing within the tree.

Any mixture of geometry types may be stored in the tree.
Note: the tree is more efficient for querying when there are fewer geometries that have overlapping bounding boxes and where there is greater similarity between the outer boundary of a geometry and its bounding box. For example, a MultiPolygon composed of widely-spaced individual Polygons will have a large overall bounding box compared to the boundaries of its individual Polygons, and the bounding box may also potentially overlap many other geometries within the tree. This means that the resulting tree may be less efficient to query than a tree constructed from individual Polygons.

## Parameters

geoms [sequence] A sequence of geometry objects.
node_capacity [int, default 10] The maximum number of child nodes per parent node in the tree.

## References

[1]

## property geometries

Geometries stored in the tree in the order used to construct the tree.
The order of this array corresponds to the tree indices returned by other STRtree methods.
Do not attempt to modify items in the returned array.

## Returns

ndarray of Geometry objects
nearest (geometry) $\rightarrow$ Optional[Any]
Return the index of the nearest geometry in the tree for each input geometry based on distance within two-dimensional Cartesian space.

Note: 'nearest' requires at least GEOS 3.6.0.

This distance will be 0 when input geometries intersect tree geometries.
If there are multiple equidistant or intersected geometries in the tree, only a single result is returned for each input geometry, based on the order that tree geometries are visited; this order may be nondeterministic.
If any input geometry is None or empty, an error is raised. Any Z values present in input geometries are ignored when finding nearest tree geometries.

## Parameters

geometry [Geometry or array_like] Input geometries to query the tree.

## Returns

scalar or ndarray Indices of geometries in tree. Return value will have the same shape as the input.

None is returned if this index is empty. This may change in version 2.0.

## See also:

query_nearest returns all equidistant geometries, exclusive geometries, and optional distances

## Examples

```
>>> from shapely.geometry import Point
>>> tree = STRtree([Point(i, i) for i in range(10)])
```

Query the tree for nearest using a scalar geometry:

```
>>> index = tree.nearest(Point(2.2, 2.2))
>>> index
2
>>> tree.geometries.take(index)
<POINT (2 2)>
```

Query the tree for nearest using an array of geometries:

```
>>> indices = tree.nearest([Point(2.2, 2.2), Point(4.4, 4.4)])
>>> indices.tolist()
[2, 4]
>>> tree.geometries.take(indices).tolist()
[<POINT (2 2)>, <POINT (4 4)>]
```

Nearest only return one object if there are multiple equidistant results:

```
>>> tree = STRtree ([Point(0, 0), Point(0, 0)])
>>> tree.nearest(Point(0, 0))
0
```

query (geometry, predicate $=$ None, distance $=$ None)
Return the integer indices of all combinations of each input geometry and tree geometries where the bounding box of each input geometry intersects the bounding box of a tree geometry.
If the input geometry is a scalar, this returns an array of shape ( n, ) with the indices of the matching tree geometries. If the input geometry is an array_like, this returns an array with shape $(2, n)$ where the subarrays correspond to the indices of the input geometries and indices of the tree geometries associated with each. To generate an array of pairs of input geometry index and tree geometry index, simply transpose the result.

If a predicate is provided, the tree geometries are first queried based on the bounding box of the input geometry and then are further filtered to those that meet the predicate when comparing the input geometry to the tree geometry: predicate(geometry, tree_geometry)

The 'dwithin' predicate requires GEOS $>=3.10$.

Bounding boxes are limited to two dimensions and are axis-aligned (equivalent to the bounds property of a geometry); any Z values present in input geometries are ignored when querying the tree.
Any input geometry that is None or empty will never match geometries in the tree.

## Parameters

geometry [Geometry or array_like] Input geometries to query the tree and filter results using the optional predicate.
predicate [ ${ }^{2}$ None, 'intersects', 'within', 'contains', 'overlaps', 'crosses','touches', 'covers', 'covered_by', 'contains_properly', 'dwithin' \}, optional] The predicate to use for testing geometries from the tree that are within the input geometry's bounding box.
distance [number or array_like, optional] Distances around each input geometry within which to query the tree for the 'dwithin' predicate. If array_like, shape must be broadcastable to shape of geometry. Required if predicate='dwithin'.

## Returns

ndarray with shape ( $\mathbf{n}$, ) if geometry is a scalar Contains tree geometry indices.
OR
ndarray with shape $(\mathbf{2}, \mathbf{n})$ if geometry is an array_like The first subarray contains input geometry indices. The second subarray contains tree geometry indices.

## Notes

In the context of a spatial join, input geometries are the "left" geometries that determine the order of the results, and tree geometries are "right" geometries that are joined against the left geometries. This effectively performs an inner join, where only those combinations of geometries that can be joined based on overlapping bounding boxes or optional predicate are returned.

## Examples

```
>>> from shapely import box, Point
>>> import numpy as np
>>> points = [Point(0, 0), Point(1, 1), Point(2,2), Point(3, 3)]
>>> tree = STRtree(points)
```

Query the tree using a scalar geometry:

```
>>> indices = tree.query(box(0, 0, 1, 1))
>>> indices.tolist()
[0, 1]
```

Query using an array of geometries:

```
>> boxes = np.array([box(0, 0, 1, 1), box(2, 2, 3, 3)])
>>> arr_indices = tree.query(boxes)
>>> arr_indices.tolist()
[[0, 0, 1, 1], [0, 1, 2, 3]]
```

Or transpose to get all pairs of input and tree indices:

```
>>> arr_indices.T.tolist()
[[0, 0], [0, 1], [1, 2], [1, 3]]
```

Retrieve the tree geometries by results of query:

```
>>> tree.geometries.take(indices).tolist()
[<POINT (0 0)>, <POINT (1 1)>]
```

Retrieve all pairs of input and tree geometries:

```
>>> np.array([boxes.take(arr_indices[0]),tree.geometries.take(arr_indices[1])]).
->T.tolist()
[[<POLYGON ((1 0, 1 1, 0 1, 0 0, 1 0))>, <POINT (0 0)>],
    [<POLYGON ((1 0, 1 1, 0 1, 0 0, 1 0))>, <POINT (1 1)>],
    [<POLYGON ((3 2, 3 3, 2 3, 2 2, 3 2))>, <POINT (2 2)>],
    [<POLYGON ((3 2, 3 3, 2 3, 2 2, 3 2))>, <POINT (3 3)>]]
```

Query using a predicate:

```
>>> tree = STRtree([box(0, 0, 0.5, 0.5), box(0.5, 0.5, 1, 1), box(1, 1, 2, 2)])
>>> tree.query(box(0, 0, 1, 1), predicate="contains").tolist()
[0, 1]
>>> tree.query(Point(0.75, 0.75), predicate="dwithin", distance=0.5).tolist()
[0, 1, 2]
```

```
>>> tree.query(boxes, predicate="contains").tolist()
[[0, 0], [0, 1]]
>>> tree.query(boxes, predicate="dwithin", distance=0.5).tolist()
[[0, 0, 0, 1], [0, 1, 2, 2]]
```

Retrieve custom items associated with tree geometries (records can be in whatever data structure so long as geometries and custom data can be extracted into arrays of the same length and order):

```
>>> records = [
... {"geometry": Point(0, 0), "value": "A"},
... {"geometry": Point(2, 2), "value": "B"}
...]
>>> tree = STRtree([record["geometry"] for record in records])
>>> items = np.array([record["value"] for record in records])
>>> items.take(tree.query(box(0, 0, 1, 1))).tolist()
['A']
```

query_nearest (geometry, max_distance=None, return_distance $=$ False, exclusive=False, all_matches=True)

Return the index of the nearest geometries in the tree for each input geometry based on distance within two-dimensional Cartesian space.

Note: 'query_nearest' requires at least GEOS 3.6.0.

This distance will be 0 when input geometries intersect tree geometries.
If there are multiple equidistant or intersected geometries in tree and all_matches is True (the default), all matching tree geometries are returned; otherwise only the first matching tree geometry is returned. Tree
indices are returned in the order they are visited for each input geometry and may not be in ascending index order; no meaningful order is implied.
The max_distance used to search for nearest items in the tree may have a significant impact on performance by reducing the number of input geometries that are evaluated for nearest items in the tree. Only those input geometries with at least one tree geometry within +/- max_distance beyond their envelope will be evaluated. However, using a large max_distance may have a negative performance impact because many tree geometries will be queried for each input geometry.

The distance, if returned, will be 0 for any intersected geometries in the tree.
Any geometry that is None or empty in the input geometries is omitted from the output. Any Z values present in input geometries are ignored when finding nearest tree geometries.

## Parameters

geometry [Geometry or array_like] Input geometries to query the tree.
max_distance [float, optional] Maximum distance within which to query for nearest items in tree. Must be greater than 0 .
return_distance [bool, default False] If True, will return distances in addition to indices.
exclusive [bool, default False] If True, the nearest tree geometries that are equal to the input geometry will not be returned.
all_matches [bool, default True] If True, all equidistant and intersected geometries will be returned for each input geometry. If False, only the first nearest geometry will be returned.

## Returns

tree indices or tuple of (tree indices, distances) if geometry is a scalar indices is an ndarray of shape ( n, ) and distances (if present) an ndarray of shape ( n, )

## OR

indices or tuple of (indices, distances) indices is an ndarray of shape (2,n) and distances (if present) an ndarray of shape (n). The first subarray of indices contains input geometry indices. The second subarray of indices contains tree geometry indices.

## See also:

nearest returns singular nearest geometry for each input

## Examples

```
>>> import numpy as np
>>> from shapely import box, Point
>>> points = [Point(0, 0), Point(1, 1), Point(2,2), Point(3, 3)]
>>> tree = STRtree(points)
```

Find the nearest tree geometries to a scalar geometry:

```
>>> indices = tree.query_nearest(Point(0.25, 0.25))
>>> indices.tolist()
[0]
```

Retrieve the tree geometries by results of query:

```
>>> tree.geometries.take(indices).tolist()
[<POINT (O O)>]
```

Find the nearest tree geometries to an array of geometries:

```
>>> query_points = np.array([Point(2.25, 2.25), Point(1, 1)])
>>> arr_indices = tree.query_nearest(query_points)
>>> arr_indices.tolist()
[[0, 1], [2, 1]]
```

Or transpose to get all pairs of input and tree indices:

```
>>> arr_indices.T.tolist()
[[0, 2], [1, 1]]
```

Retrieve all pairs of input and tree geometries:

```
>>> list(zip(query_points.take(arr_indices[0]), tree.geometries.take(arr_
\rightarrow \text { -indices[1])))}
[(<POINT (2.25 2.25)>, <POINT (2 2)>), (<POINT (1 1)>, <POINT (1 1)>)]
```

All intersecting geometries in the tree are returned by default:

```
>>> tree.query_nearest(box(1,1,3,3)).tolist()
[1, 2, 3]
```

Set all_matches to False to to return a single match per input geometry:

```
>>> tree.query_nearest(box(1,1,3,3), all_matches=False).tolist()
[1]
```

Return the distance to each nearest tree geometry:

```
>>> index, distance = tree.query_nearest(Point(0.5, 0.5), return_distance=True)
>>> index.tolist()
[0, 1]
>>> distance.round(4).tolist()
[0.7071, 0.7071]
```

Return the distance for each input and nearest tree geometry for an array of geometries:

```
>>> indices, distance = tree.query_nearest([Point(0.5, 0.5), Point(1, 1)],ь
\rightarrow \text { return_distance=True)}
>>> indices.tolist()
[[0, 0, 1], [0, 1, 1]]
>>> distance.round(4).tolist()
[0.7071, 0.7071, 0.0]
```

Retrieve custom items associated with tree geometries (records can be in whatever data structure so long as geometries and custom data can be extracted into arrays of the same length and order):

```
>>> records = [
... {"geometry": Point(0, 0), "value": "A"},
... {"geometry": Point(2, 2), "value": "B"}
```

```
... ]
>>> tree = STRtree([record["geometry"] for record in records])
>>> items = np.array([record["value"] for record in records])
>>> items.take(tree.query_nearest(Point(0.5, 0.5))).tolist()
['A']
```


### 5.17 Testing

The functions in this module are not directly importable from the root shapely module. Instead, import them from the submodule as follows:

```
>>> from shapely.testing import assert_geometries_equal
```

assert_geometries_equal $(x, y$, tolerance=1e-07, equal_none=True, equal_nan=True, normalize=False,
err_msg=", verbose=True)

Raises an AssertionError if two geometry array_like objects are not equal.
Given two array_like objects, check that the shape is equal and all elements of these objects are equal. An exception is raised at shape mismatch or conflicting values. In contrast to the standard usage in shapely, no assertion is raised if both objects have $\mathrm{NaNs} / \mathrm{Nones}$ in the same positions.

## Parameters

$\mathbf{x}$ [Geometry or array_like]
y [Geometry or array_like]
equal_none [bool, default True] Whether to consider None elements equal to other None elements.
equal_nan [bool, default True] Whether to consider nan coordinates as equal to other nan coordinates.
normalize [bool, default False] Whether to normalize geometries prior to comparison.
err_msg [str, optional] The error message to be printed in case of failure.
verbose [bool, optional] If True, the conflicting values are appended to the error message.

### 5.18 Indices and tables

- genindex
- modindex
- search


## BIBLIOGRAPHY

[1] Leutenegger, Scott T.; Edgington, Jeffrey M.; Lopez, Mario A. (February 1997). "STR: A Simple and Efficient Algorithm for R-Tree Packing". https://ia600900.us.archive.org/27/items/nasa_techdoc_19970016975/ 19970016975.pdf

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